

Nondipole laser-assisted photoionization: the streaking regime

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INTRODUCTION & AIM

What is a “Nondipole” laser?

Dipole approx.

$$\mathbf{A}(\mathbf{r}, t) = \mathbf{A}_0(t)$$

$$\mathbf{B} = \nabla \times \mathbf{A} = 0$$

$$E = \hbar\omega$$

$$\mathbf{p} = 0$$

$\beta_0 < 1 < \lambda$

\mathbf{e} oscillates in polarization direction

Nondipole

$$\mathbf{A}(\mathbf{r}, t)$$

$$E = \hbar\omega$$

$$\mathbf{p} = \frac{E}{c} \hat{\mathbf{K}}$$

\mathbf{e} oscillates in polarization direction and propagation direction

β_0

propagation

Let us consider a space-dependent IR laser field at the lowest order in $1/c$,

$$\mathbf{A}(\eta) \simeq \mathbf{A}(\eta)|_{r=0} + [(\mathbf{r} \cdot \nabla) \mathbf{A}(\eta)]|_{r=0}$$

$$\simeq \mathbf{A}_0(t) + \frac{\hat{\mathbf{z}} \cdot \mathbf{r}}{c} \mathbf{E}_0(t)$$

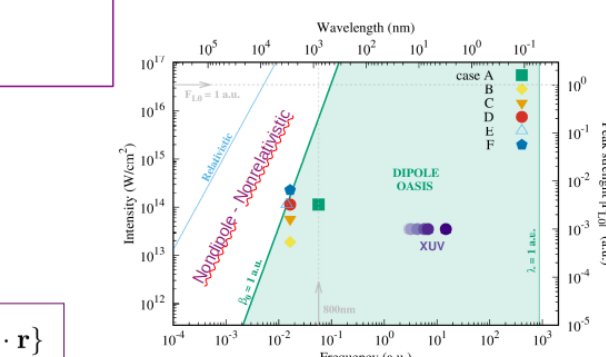
DIPOLE approximation (1st term only)

NONDIPOLE nonrelativistic approximation: both terms

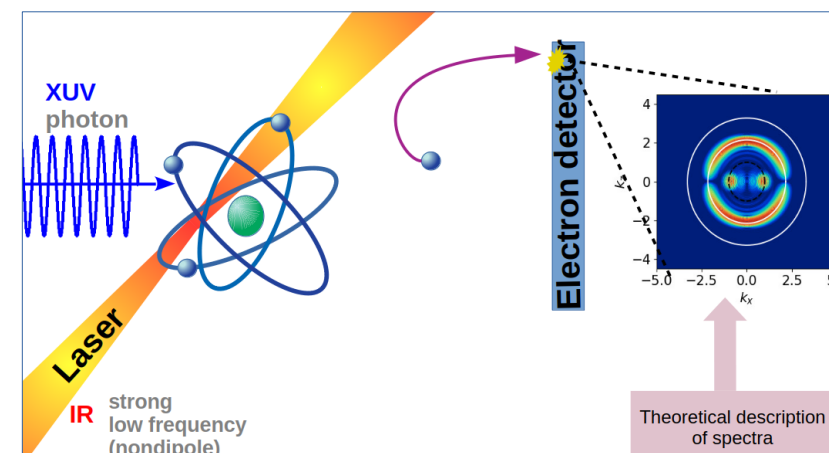
$$\chi_f^{VND}(\mathbf{r}, t) = (2\pi)^{-3/2} \exp(i\mathbf{\Pi}(\mathbf{k}, t) \cdot \mathbf{r})$$

$$\times \exp\left\{i \int_t^\infty \mathbf{\Pi}^2(\mathbf{k}, t') dt'\right\}$$

Nondipole Gordon Volkov wave function describes a free electron in a **nondipole** IR laser field



Laser-assisted photoionization



METHOD

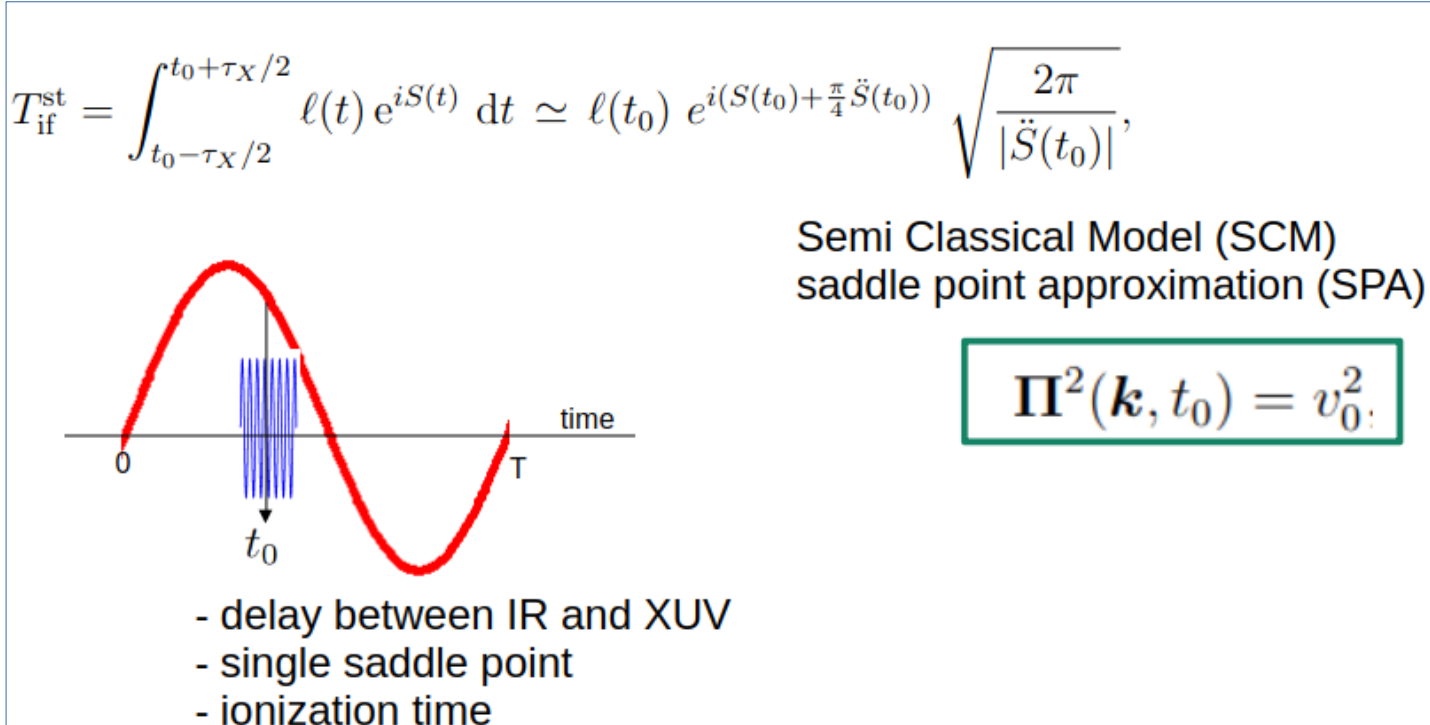
XUV + IR LAPE

Laser Assisted Photoionization Emission

$$T_{if} = -i \int_{-\infty}^{+\infty} dt \langle \chi_f^-(\mathbf{r}, t) | H_{int}(\mathbf{r}, t) | \phi_i(\mathbf{r}, t) \rangle,$$

$$T_{if} \simeq T_{if}^{IR}(\text{Direct Ioniz.}) + T_{if}^{XUV}(\text{LAPE})$$

XUV ionization assisted by IR



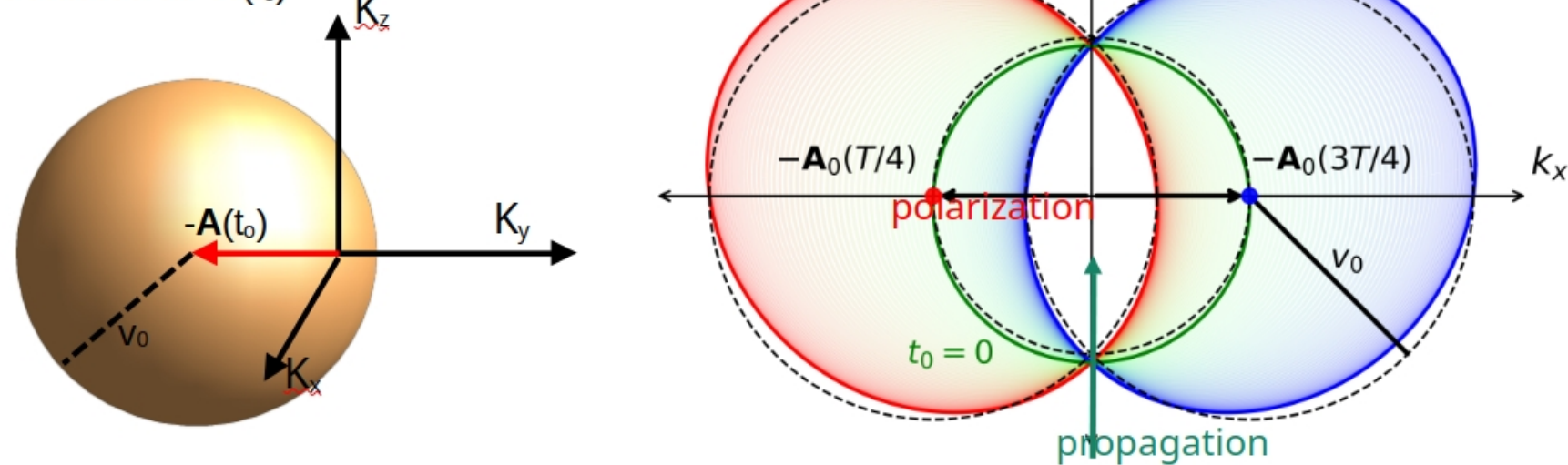
$$\mathbf{\Pi}^2(\mathbf{k}, t_0) = v_0^2$$

$$v_0^2 = 2(\omega_X - I_p)$$

$$[\mathbf{k} + \mathbf{A}(t_0) + (\dots)/c]^2 = v_0^2$$

Nondipole: forward-deformed spheres

Semiclassical allowed momenta
VOID-shaped shell in 3D k-space
Centered at $-\mathbf{A}(t_0)$



In streaking conditions the stationary time t_s is the same as t_0 , the delay between the IR and the short pulse XUV.

Those values of \mathbf{k} satisfying its equation for real values of t_s define a quasi-sphere [centered at $-\mathbf{A}(t_0)$ and radius v_0], of classically allowed momenta

Dipole approximation: dashed lines determine the spheres centered at $-\mathbf{A}(t_0)$.

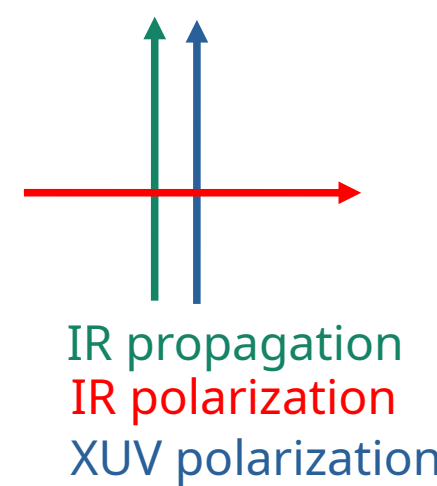
As it rotates for circularly polarized IR laser, the sphere also rotates in the plane perpendicular to z axis.

REFERENCES

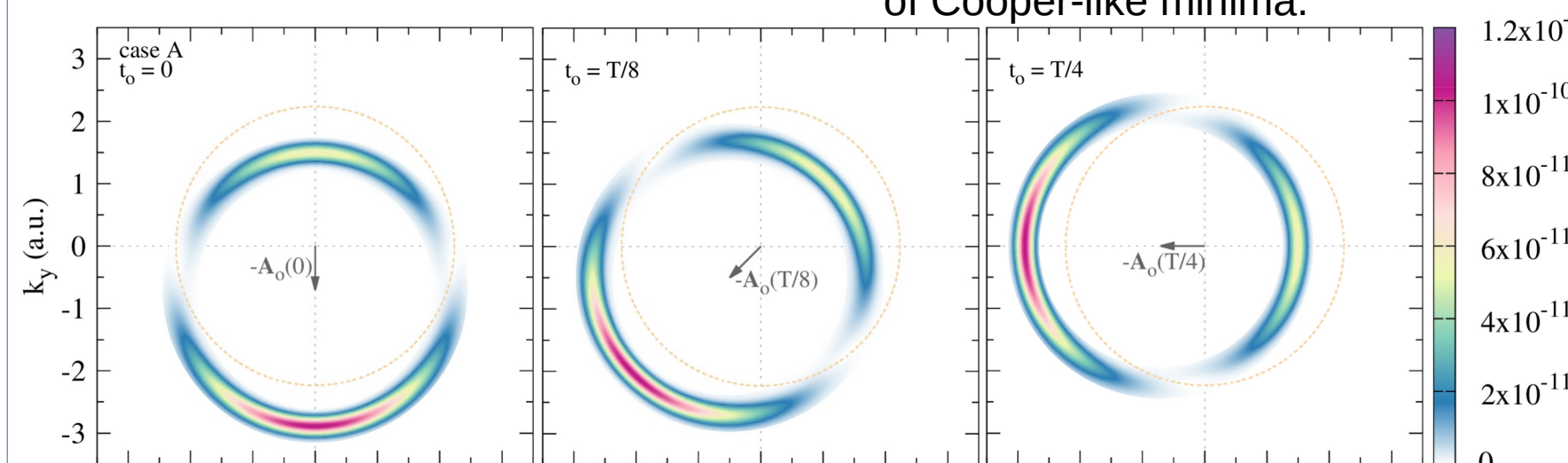
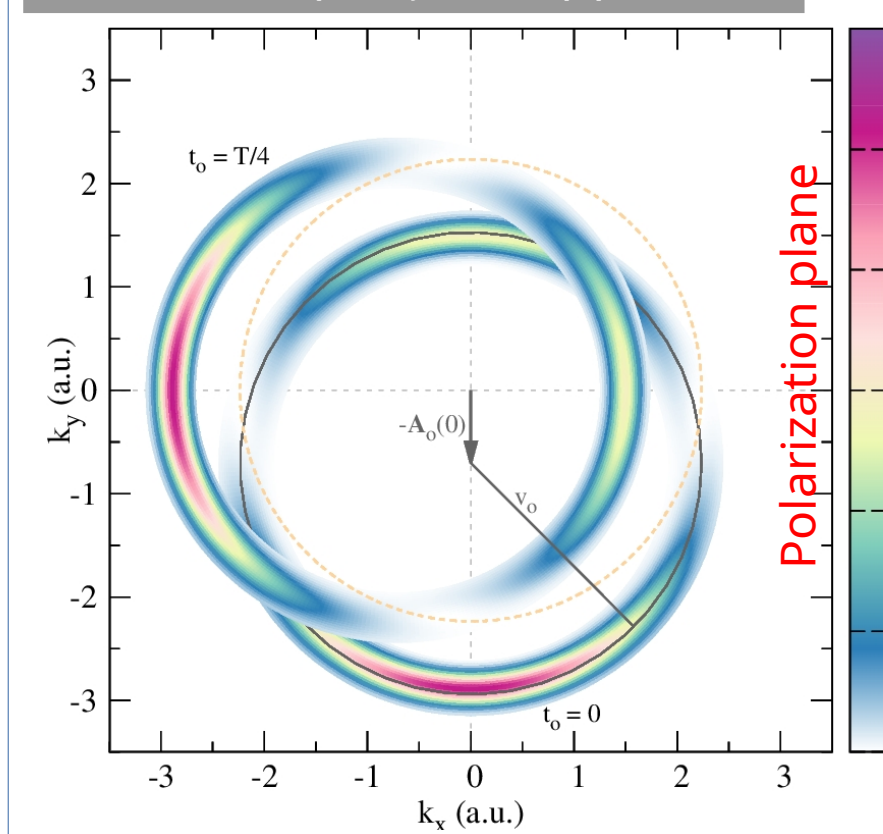
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RESULTS & DISCUSSION

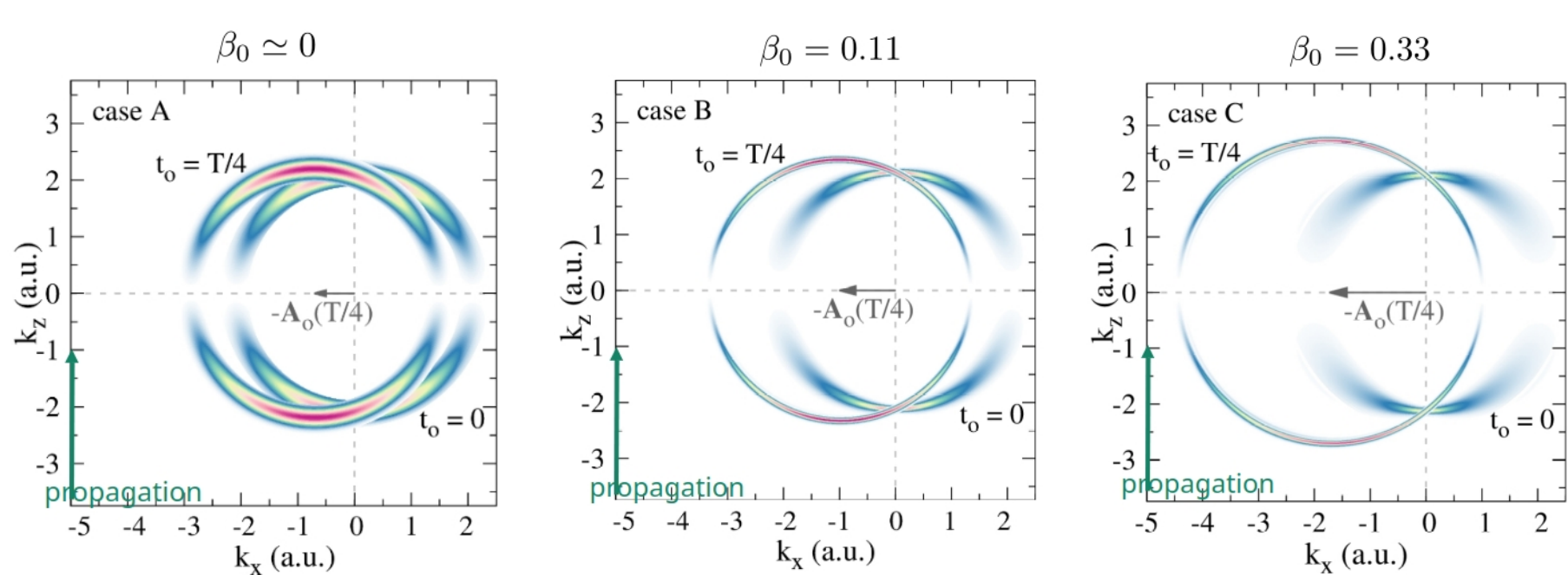
Streaking H(1s)
XUV \sin^2 envelope
Circular IR



Polarization ($k_x, k_y, k_z = 0$) plane

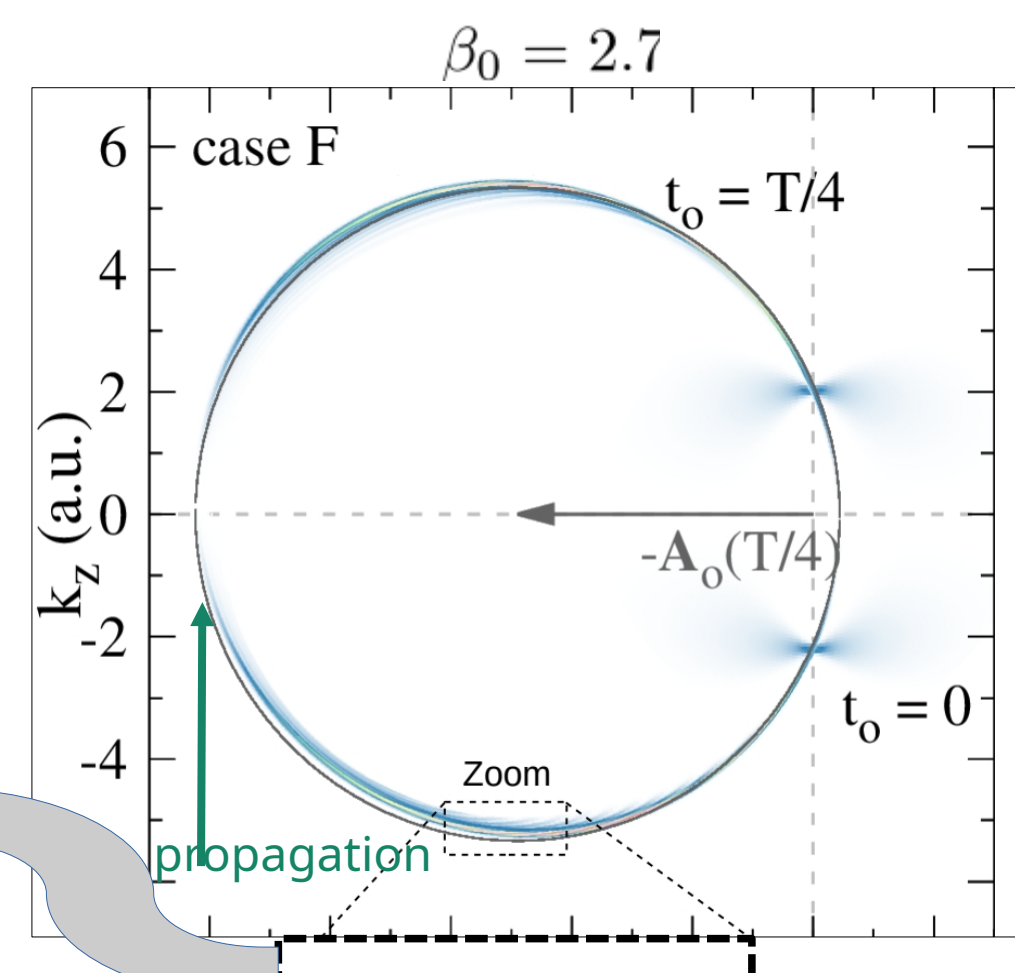
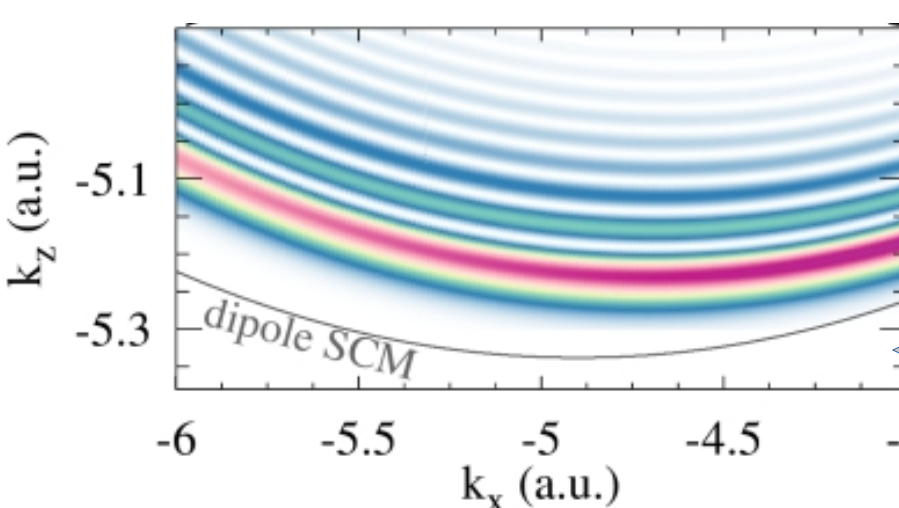


Propagation ($k_x, k_y = 0, k_z$) plane



SCM: rings with radius v_0 , centered at $-\mathbf{A}(t_0)$

Nondipole: shifted forward rings



CONCLUSION

- We have studied LAPE process in a nondipole nonrelativistic SFA description. As particular case, we consider H(1s) ionized by circularly polarized IR laser and train of short XUV pulses.
- The STREAKING PMD is predominantly distributed on a surface predicted by the semiclassical model in momentum space.
- PMD is non-zero in the dipole forbidden $k_z=0$ plane; where Cooper-like minima are observed along the $E = v_0^2/2$ line.
- STREAKING pattern shifts in the direction opposite to the instantaneous IR polarization vector; changing the ionization times t_0 , the PMD rotates as in attoclock process.