

1 *Proceedings*

# 2 **Precision Measuring Instrument and Method of** 3 **Fertilizer Shape Characteristics Based on Binocular** 4 **Vision <sup>†</sup>**

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16 **Abstract:** Aiming at the low precision of manual measurement which also impose heavy workload  
17 burdern, as well as the high cost and complex operation of high-precision measuring instruments,  
18 a precision measuring instrument and method of fertilizer shape characteristics are proposed. In  
19 this method, the fertilizer shape characteristics are calculated by image acquisition, gray and gamma  
20 correction, and edge detection. Firstly, the measuring instrument works in an intermittent collection  
21 mode, which can acquire the top and side images of fertilizer at the same time. Secondly, gamma  
22 correction is performed on the top and side grayscale images to improve the image contrast, after  
23 the fertilizer image collection is completed. Finally, the edge detection algorithm based on the  
24 orientation gradient is proposed to extract the top and side contour images of the fertilizer  
25 accurately, and the shape characteristics are calculated from the contour images. The shape  
26 characteristics of the compound fertilizer, the organic fertilizer, and the biological fertilizer are  
27 measured by using the three-dimensional scanning method and the measuring method proposed  
28 in this paper. The significant difference between the two methods is compared by the Grubbs test,  
29 F test, and t test. The results show that there is no significant difference between the two measuring  
30 methods of fertilizer shape characteristics. This precision measuring instrument as well as its  
31 measuring method proposed in this paper can measure the fertilizer shape characteristics quickly  
32 and accurately, which can lay a solid foundation for fertilizer production and quality inspection.

33 **Keywords:** fertilizer; shape characteristics; measuring instrument; measuring method; binocular  
34 vision  
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## 36 **1. Introduction**

37 Particle shape characteristics are a classic and increasingly popular research topic in many  
38 disciplines [1-5]. The particle shape characteristics affect the mechanical and flow behavior of the  
39 material. For example, the sand tends to have a high angle of shear strength [6-7], the contact stress  
40 concentration [8-9], resistance to flow and anti-liquefaction resistance [10-11]. In addition, particle  
41 shape characteristics also affect the interaction of particles with fluids and air, such as drag  
42 coefficients and mineral floatability [12-13]. Therefore, particle shape is an important characteristics  
43 for predicting and controlling the engineering properties of particle materials.

44 Fertilizer is one of the most important agricultural particles, and its shape characteristics affect  
45 the appearance quality, strength, fluidity, and the effect of machine fertilization, which is of great  
46 significance to the design and research of agricultural machinery [14-15]. Kan, Su, and Tang [16]  
47 demonstrated that the higher the sphericity of fertilizer is, the higher the strength of fertilizer is, and  
48 the more difficult the fertilizer is to be deformed and broken. Silverberg, Lehr, and Hoffmeister [17]  
49 investigated that the shape characteristics and the pore structure formed by the accumulation of  
50 fertilizer affect the salt ions diffusion, so as to affect the performance of fertilizer. Basu and Kumar  
51 [18] found that fertilizer granularity affects the nutrient release time of fertilizer.

52 Fertilizer is an irregular shape particle, so it is difficult to measure the shape characteristics  
53 accurately manually. With the rapid development of computer and software technology, it is possible  
54 to measure the particle shape with the help of computer technology. Fernlund [19] measured the axial  
55 length of the long axis, the middle axis, and the short axis of the coarse aggregate by the image  
56 analysis method. The results show that the measurement results of this method have a good  
57 correlation with the measurement results of the Danish box. Zhang, Huang, and Zhao [20] measured  
58 the length, width, height, and particle shape index of the basalt and limestone by the digital image  
59 processing technology. Mora and Kwan [21] measured the sphericity and concave convex ratio of  
60 coarse aggregate by the digital image processing technology. Liu, Xiang, Budhu, and Cui [22]  
61 calculated and quantified the shape characteristics of sand particles by digital image processing.  
62 Zhang, Ye, Chen, and Li [23] measured and evaluated the shape characteristics of gravel particles by  
63 the digital image processing technology. Xiao, Yang, Chen, and Gao [24] used the digital image  
64 processing technology to calculate the particle shape and angular characteristic parameters of the  
65 aggregate.

66 Based on the above researches, it is found that the fertilizer shape characteristics affect fertilizer  
67 quality and performance. At present, there is no special particle shape measuring instrument for  
68 fertilizer. The manual measurement has high work intensity and low accuracy. The existing non-  
69 contact measuring instruments are mainly monocular, and they are mostly used to measure the  
70 aggregate and other particles. To measure the fertilizer shape characteristics accurately and quickly,  
71 a precision measuring instrument of fertilizer shape characteristics based on binocular vision as well  
72 as its measuring method are proposed in this paper. The non-contact measuring instrument is used  
73 to collect fertilizer images, and the fertilizer shape characteristics are extracted by the digital image  
74 processing technology.

## 75 2. Materials and Methods

### 76 2.1. Description Method of Fertilizer Shape Characteristics

#### 77 2.1.1. Triaxial Characteristics

78 The macro profile of particles is usually represented by three mutually perpendicular axes,  
79 namely the long axis, the middle axis, and the short axis, which are equivalent to the length, width,  
80 and thickness of the particle. In a natural and stable state, the length refers to the maximum size of  
81 the particle in the plane projection graph, the width refers to the maximum size perpendicular to the  
82 length direction, and the thickness refers to the linear size perpendicular to the length and width  
83 direction. The relationship between the three axes of particles can be expressed by the equiaxed ratio  
84 and the flake ratio [25]:

$$K = b/a \quad (1)$$

$$\lambda = c/b \quad (2)$$

85 Where,  $k$  is the particle equiaxed ratio;  $\lambda$  is the particle flake ratio;  $a$  is the particle length, mm;  $b$  is the  
86 particle width, mm;  $c$  is the particle thickness, mm.

#### 87 2.1.2. Roundness

88 Roundness ( $\sigma$ ) reflects the sharpness of the particle edges and corners. Kuo and Freeman[26]  
89 define the particle roundness  $\sigma$  as follows:

$$\sigma = 4\pi A/L^2 \quad (3)$$

90 Where,  $L$  is the perimeter of the particle projection contour, mm;  $A$  is the projection area of the  
91 particle, mm<sup>2</sup>.

### 92 2.1.3. Sphericity

93 Sphericity ( $\varphi$ ) reflects how close the particle is to a sphere. Waddell defines the particle sphericity  
94  $\varphi$ [27] as follows:

$$\varphi = \sqrt[3]{v/v_s} \quad (4)$$

95 According to Waddell's definition of the particle sphericity, Krumbein equates the particle as an  
96 ellipsoid[28], so the particle equivalent volume  $v$  is:

$$v = (\pi/6)abc \quad (5)$$

97 Substitute into the formula (4) to obtain the formula for calculating the particle sphericity:

$$\varphi = \sqrt[3]{v/v_s} = \sqrt[3]{(\pi/6)abc / (\pi/6)a^3} = \sqrt[3]{bc/a^2} \quad (6)$$

98 Where,  $v$  is the equivalent volume of the particle, mm<sup>3</sup>;  $v_s$  is the volume of the smallest sphere  
99 circumscribed by the particle (sphere with a diameter as the diameter), mm<sup>3</sup>.

### 100 2.1.4. Granularity

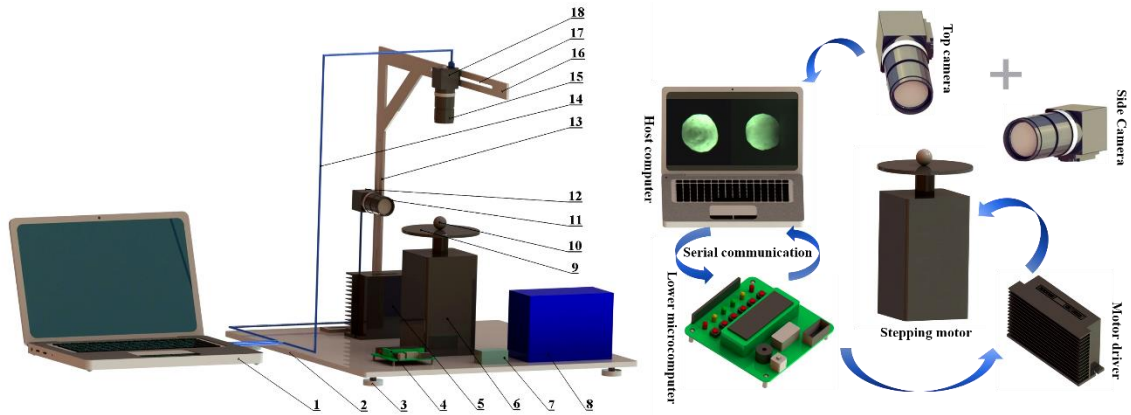
101 Granularity ( $d$ ) is used to indicate the size of the particle, which can be expressed as the single  
102 size of a particle or the average particle size of a particle group. The granularity ( $d$ ) of a single spheroid  
103 is as follows[29]:

$$d = \sqrt[3]{6v/\pi} = \sqrt[3]{abc} \quad (7)$$

104 Where,  $d$  is the particle granularity, mm.

## 105 2.2. Measuring Instrument of Fertilizer Shape Characteristics

106 The structure of the measuring instrument based on the binocular vision is shown in Figure 1. It  
107 is mainly composed of the base, the objective stage, the stepper motor, the top camera, the top lens,  
108 the side camera, the side lens, the upper computer, and the lower microcomputer. The main technical  
109 parameters of the instrument are shown in Table 1. The instrument adopts the intermittent static  
110 collection mode to collect the top and side images of single fertilizer at the same time. The objective  
111 stage is engraved with a cross calibration, and the fertilizer to be tested is placed at the center of the  
112 cross calibration. The objective stage is connected to the stepper motor through a semicircle key. The  
113 lower microcomputer controls the rotation of the stepping motor to achieve the rotation of the  
114 fertilizer. After the stepper motor turns the set angle, it stops rotating. The lower microcomputer  
115 sends the rotation completion command to the upper computer through the serial port. The upper  
116 computer controls the top and side cameras to collect the images of the fertilizer to be tested. After  
117 the image acquisition is completed, the upper computer sends the image acquisition completion  
118 command to the lower microcomputer through the serial port, and the lower microcomputer controls  
119 the stepping motor to rotate again. Repeat this process until the top and side images achieve the target  
120 number. The acquisition process is shown in Figure 1. After the top and side images of single fertilizer  
121 are all collected, the computer analyzes and processes the images respectively to obtain the fertilizer  
122 shape characteristics.



123  
124

125 **Figure 1.** Structure of instrument and fertilizer collection process: (1)Upper computer; (2)Base;  
126 (3)Adjusting foot; (4)Lower microcomputer; (5)Driver; (6)Stepping motor; (7)Power conversion  
127 module; (8)Power; (9)Loading platform; (10)Fertilizer to be tested; (11)Side lens; (12)Side camera;  
128 (13)Side notch; (14)Data transmission line; (15)Top lens; (16)Camera adjusting frame; (17)Top notch;  
129 (18)Top camera.

130

**Table 1.** Main technical parameters.

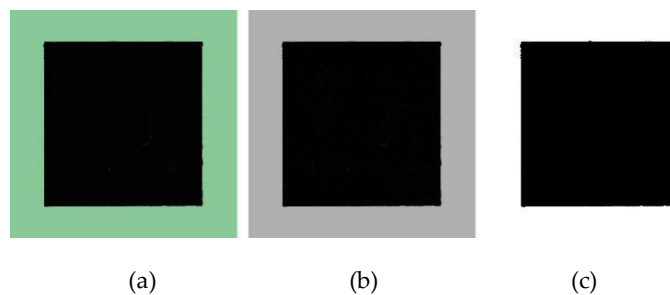
Parameters	Numerical value
Overall dimensions (length × width × height)/(mm×mm×mm)	450×450×435
Loading platform size (radius)/mm	115
Working voltage/ V	24
Stepper motor speed/ r·min <sup>-1</sup>	21
Single particle fertilizer collection time/ s	28
Fertilizer sampling interval/ s	16
Working distance of top camera/ mm	180
Side camera working distance/ mm	180

131 *2.3. Measuring Method of Fertilizer Shape Characteristics*

132 *2.3.1. Length Calibration*

133 To establish the relationship between the actual size of the fertilizer and the pixels, the image  
134 information of the calibration target (10mm×10mm black square) is collected, and the grayscale and  
135 binarization process is performed. The process is shown in Figure 2. In the threshold image, the target  
136 area is black, and the threshold value is 0. The threshold image is traversed by pointer scanning,  
137 and the number of rows of all pixels that meet the defined threshold is counted  $N_0=550$ . According to  
138 formula (8), the actual length represented by a single pixel ( $L_0$ ) is 0.018mm.

$$L_0 = 10 / N_0 \tag{8}$$



139

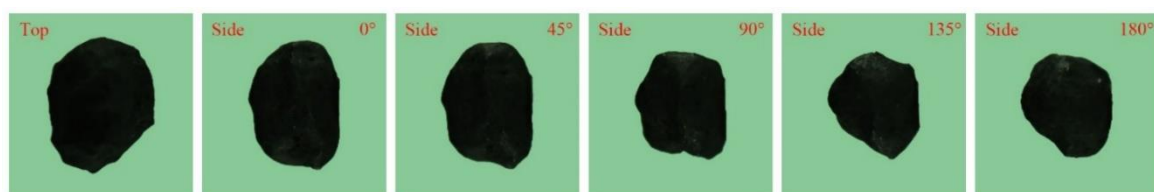
140

141

**Figure 2.** Length calibration: (a) Original image; (b) Grayscale image; (c) Threshold image.

142 2.3.2. Collection and Preprocessing of Fertilizer Images

143 Firstly, we should place a single fertilizer at the center of the cross calibration, and adjust the  
 144 positions of the cameras to ensure that the fertilizer is completely imaged in the two cameras.  
 145 Secondly, we should adjust the light intensity and focal length according to the imaging state of the  
 146 fertilizer in the top and side cameras to ensure that the top and side images are clear and stable.  
 147 Finally, to better get the whole side profile of the fertilizer, we should collect different sides profiles  
 148 of the fertilizer in different angles. Therefore, we control the stepper motor to rotate 9° for a step  
 149 and the stepper motor will rotate 20 steps in one time, and the top and side cameras respectively  
 150 collect the top and side images of the fertilizer [30]. In the process of rotation, the contour of the top  
 151 image is all the same, therefore, the top image is collected once, while the side image needs to be  
 152 collected many times. After the collection, a total of 1 top image and 20 side images are obtained. To  
 153 describe the fertilizer details more clearly, we crop the area containing the complete fertilizer image  
 154 to display in the paper. The top image and some side images of the fertilizer are shown in Figure 3.



155

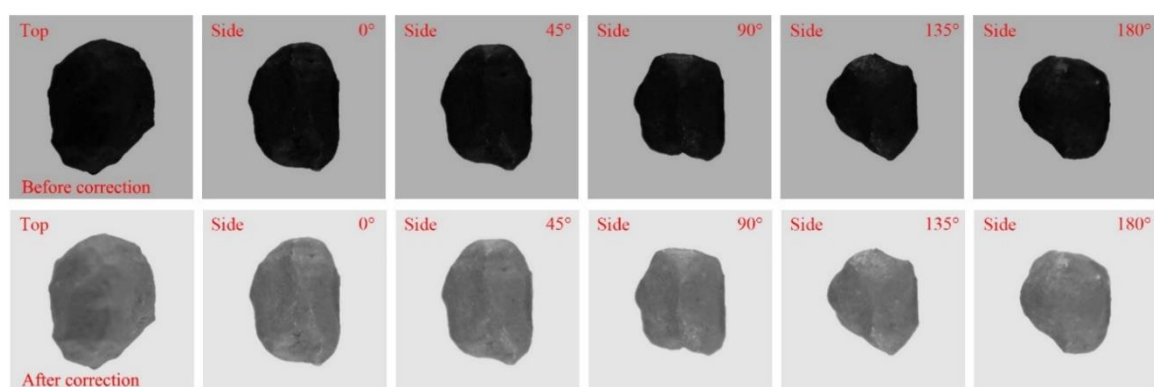
156

Figure 3. Original images of fertilizer top and side.

157 Gamma correction is a non-linear operation on the gray value of the input image, which makes  
 158 the gray value of the output image exponentially related to the gray value of the input image. It is  
 159 usually used for smoothing the extended dark details. In order to improve the extraction accuracy of  
 160 fertilizer contour, the collected fertilizer image is processed with greyscale first, and then the gray  
 161 image is corrected with gamma according to formula (9). The correction effect is shown in Figure 4.

$$Y(x,y) = I(x,y)^\gamma \tag{9}$$

162 Where,  $I(x, y)$  is the gray image;  $Y(x, y)$  is the corrected image;  $(x, y)$  is the pixel coordinates;  $\gamma$  is 0.5.



163

164

Figure 4. Gamma correction effect comparison.

165 2.3.3. Contour Extraction of Fertilizer Top and Side Images

166 During the image processing, the extraction of fertilizer contour is a key step, and its results  
 167 directly affect the calculation accuracy of fertilizer shape characteristics in the later stage. In the top  
 168 and side images of fertilizer after Gamma correction, fertilizer has strong boundary information. In  
 169 edge detection, the selection of high and low threshold is very important, which directly determines  
 170 the amount of edge information detected and the continuity of the edge. Since the high threshold  
 171 controls the starting point of edge detection, the smaller the high threshold is, the more edge  
 172 information will be retained, but the false edges will increase. On the contrary, if the high threshold

173 is larger, although the false edges can be effectively suppressed, some edge information will also be  
 174 lost. How to choose a suitable high and low threshold has an important influence on the selection of  
 175 the correct edge point in the stage of edge detection and connection. Therefore, the edge detection  
 176 algorithm based on the directional gradient is proposed to extract the contour of the fertilizer image  
 177 accurately. The main steps are as follows:

178 (1) Suppose the high and low thresholds are  $h$  and  $l$ , respectively. After suppressing the non-  
 179 maximum value of the gradient mode, the candidate edge points can be divided into three categories  
 180 according to the range of the gradient mode:  $B_1$ ,  $B_2$ , and  $B_3$ , which are defined as follows.

$$B_1 = \{(x, y) \mid 0 < |\text{grad } f(x, y)| < l\} \quad (10)$$

$$B_2 = \{(x, y) \mid l \leq |\text{grad } f(x, y)| \leq h\} \quad (11)$$

$$B_3 = \{(x, y) \mid |\text{grad } f(x, y)| \geq h\} \quad (12)$$

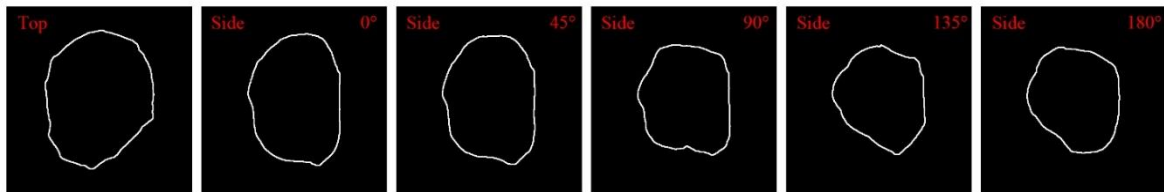
181 Where,  $B_1$  is the set of non-edge pixels;  $B_2$  is the set of possible edge pixels;  $B_3$  is the set of edge pixels  
 182 after non-maximum value suppression.

183 (2) Calculate the directional derivative of each pixel in the top and side image corrected with  
 184 gamma, and calculate the gradient modulus based on the result of the directional derivative.

185 (3) Perform non-maximum suppression on the top and side image based on the gradient mode  
 186 and determine the set of candidate edge points.

187 (4) Among the candidate edge points, the high and low thresholds are determined according to  
 188 the minimization of the three types of gradient modulus variance. The high threshold is 102 and the  
 189 low threshold is 44.

190 (5) Use recursive search for boundary point detection and edge connection and output image  
 191 edges. The top and side contours of fertilizer are shown in Figure 5.

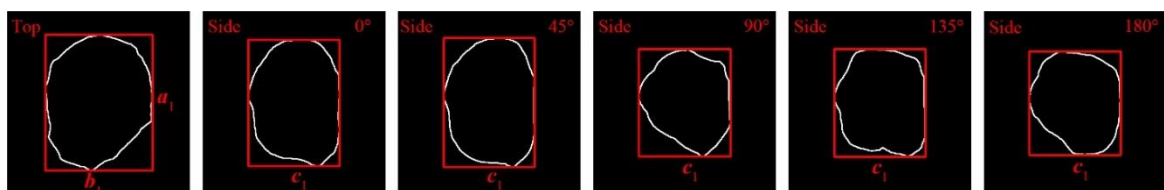


192  
 193 **Figure 5.** Top and side contour images of fertilizer.

194 2.3.4. Calculation of Fertilizer Particle Shape Parameters

195 In the top contour image, the parameters of fertilizer top contour perimeter  $L$ , area  $A$ , and the  
 196 minimum circumscribed rectangle are obtained. The length of the minimum circumscribed rectangle  
 197 represents the maximum size of the fertilizer in the top projection, and the width of the minimum  
 198 circumscribed rectangle represents the maximum size perpendicular to the length direction.  
 199 Therefore, the length and width of the minimum circumscribed rectangle are respectively equivalent  
 200 to the length  $a_1$  and width  $b_1$  of the fertilizer, and then the fertilizer equiaxed ratio  $k_1$  and roundness  
 201  $\sigma_1$  are calculated according to formulas (1) and (3).

202 In the side contour image, the parameters of the minimum circumscribed rectangle are obtained.  
 203 The width of the minimum circumscribed rectangle represents the line dimension of the fertilizer  
 204 perpendicular to the length and width direction. To reduce the error, the average value of the  
 205 minimum circumscribed rectangle width of all side contours is equivalent to the fertilizer thickness  
 206  $c_1$ , and then the fertilizer flake rate  $\lambda_1$ , sphericity  $\varphi_1$ , and granularity  $d_1$  are calculated according to  
 207 formulas (2), (6), and (7).



208

209 **Figure 6.** Fertilizer particle shape parameters.

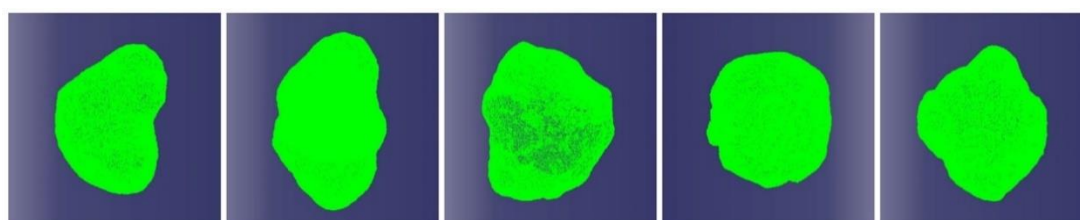
210 **3. Results and Discussion**

211 *3.1. Experiment Design*

212 The three-dimensional scanning technology can transform various irregular, complex or non-  
 213 standard target structure information into the data information, and then reconstruct the three-  
 214 dimensional model of the target structure to achieve a precision measurement, which can replace the  
 215 traditional measurement method [31]. To verify the measurement accuracy and speed of the fertilizer  
 216 shape characteristic measuring instrument, a control experiment was designed. In the same order,  
 217 the method proposed in the paper (FSI) and three-dimensional scanning method (TDS) were used to  
 218 obtain the fertilizer shape characteristics.

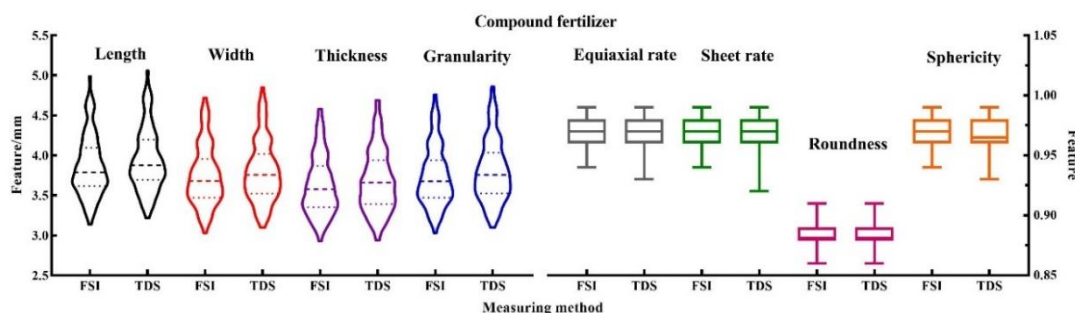
219 In this study, the three-dimensional scanner produced by Beijing Xunheng Technology Co., Ltd.  
 220 was used. The point cloud digital model of fertilizer was obtained by non-contact scanning, as shown  
 221 in Figure 7. Three-dimensional scanner measuring the fertilizer shape characteristics were as follows:

- 222 (1) Obtain the point cloud digital model of fertilizer by three-dimensional scanning technology.
- 223 (2) Obtain the length  $a_2$ , width  $b_2$ , thickness  $c_2$ , area  $A_2$ , and perimeter  $L_2$  of fertilizer by software.
- 224 (3) Calculate the equiaxed ratio  $k_2$ , flake ratio  $\lambda_2$ , roundness  $\sigma_2$ , and sphericity  $\varphi_2$  of the fertilizer  
 225 according to formula (1), (2), (3), and (6).

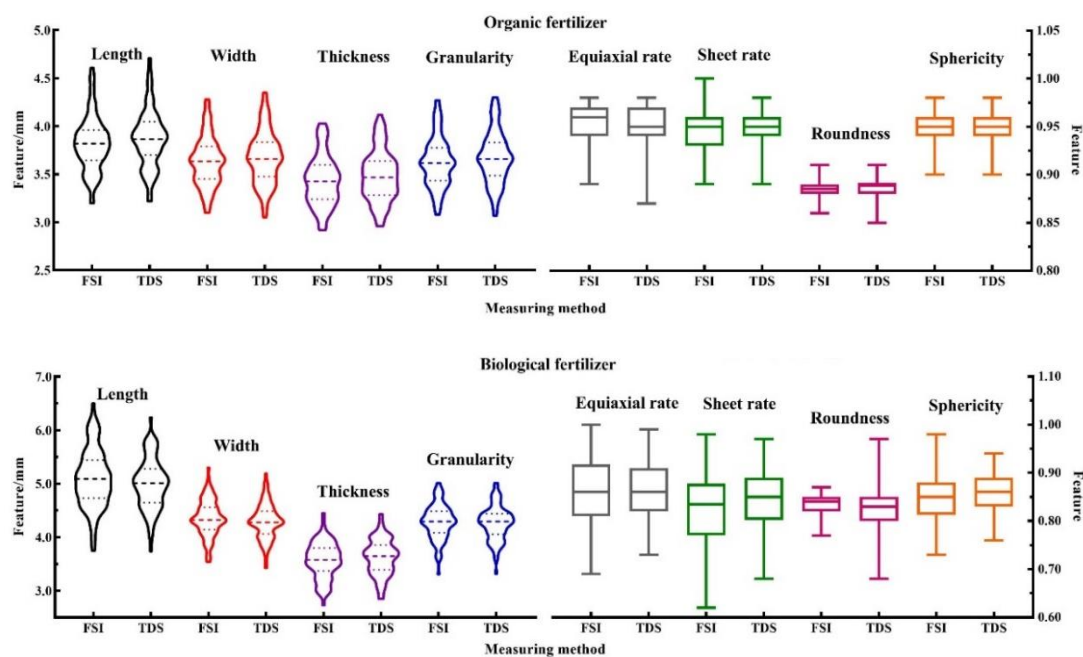


226  
 227 **Figure 7.** Three dimensional scanning of fertilizer.

228 According to the different material forms in fertilizers, fertilizers can be divided into the  
 229 compound fertilizer (CF), the organic fertilizer (OF), and the biological fertilizer (BF). To test the  
 230 applicability of the method proposed in this paper to different fertilizers, 100 compound fertilizers,  
 231 100 organic fertilizers, and 100 biological fertilizers produced by Shandong Guanxian Fufeng  
 232 fertilizer Co., Ltd. were collected as experimental samples by random sampling [32]. Taking this  
 233 sample as the research object, we measured the fertilizer shape characteristics. The distribution of  
 234 each parameter was shown in Figure 8. To verify the accuracy of measurement, the experiment data  
 235 were summarized, processed, and analyzed.



236



237

238

239

**Figure 8.** Distribution of fertilizer particle shape characteristic parameters.

240 It can be seen from Figure 8 that the length, width, thickness, and granularity of the fertilizers  
 241 were all approximately normal distribution under different measurement methods, with a bell-  
 242 shaped distribution of high in the middle and low at both ends. The length, width, thickness, median,  
 243 upper quartile, lower quartile, and the peak value of probability density function distribution among  
 244 the three fertilizers have small differences. Under different measuring methods, the differences of the  
 245 mean value, the upper quartile and the lower quartile of the equiaxed rate, the flake rate, the  
 246 roundness, and the sphericity of the three fertilizers were small. The results showed that the datas  
 247 measured by the two methods are evenly distributed, with small fluctuation, high stability, and no  
 248 significant difference.

249 *3.2. Basic Statistical Processing*

250 In order to further compare the measurement accuracy of the two measurement methods, the  
 251 experiment datas were calculated statistically. The maximum value, minimum value, average value,  
 252 range, and standard deviation of the fertilizer shape characteristics were calculated respectively, so  
 253 as to prepare for the Grubbs test, *F* test, *t* test, and test analysis. The specific results were shown in  
 254 Table 2. The average value and standard deviation respectively were:

$$\bar{x} = \frac{\sum_{i=1}^n x_i}{n} \tag{13}$$

$$S = \sqrt{\frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n-1}} \tag{14}$$

255 Where,  $x_i$  is the sample value;  $n$  is the sample total number;  $\bar{x}$  is the sample mean value;  $S$  is the  
 256 sample standard deviation.

257

**Table 2.** Basic statistical results.

Project	$a_1/a_2$	$b_1/b_2$	$c_1/c_2$	$k_1/k_2$	$\lambda_1/\lambda_2$	$\sigma_1/\sigma_2$	$\varphi_1/\varphi_2$	$d_1/d_2$
Maximum	4.99/5.06	4.72/4.85	4.58/4.69	0.99/0.99	0.99/0.99	0.91/0.91	0.99/0.99	4.76/4.86
CF Minimum	3.14/3.22	3.03/3.10	2.93/2.94	0.94/0.93	0.94/0.92	0.86/0.86	0.94/0.93	3.03/3.10
Average	3.86/3.94	3.74/3.81	3.62/3.67	0.97/0.97	0.97/0.96	0.89/0.88	0.97/0.97	3.74/3.80



	Standard deviation	0.38/0.39	0.38/0.39	0.38/0.39	0.01/0.01	0.01/0.02	0.01/0.01	0.01/0.01	0.38/0.39
	Maximum	4.61/4.71	4.28/4.35	4.03/4.12	0.98/0.98	1.00/0.98	0.91/0.91	0.98/0.98	4.27/4.30
	Minimum	3.20/3.22	3.10/3.05	2.92/2.96	0.89/0.87	0.89/0.89	0.86/0.85	0.90/0.90	3.08/3.07
OF	Average	3.82/3.87	3.63/3.67	3.43/3.48	0.95/0.95	0.94/0.95	0.88/0.89	0.95/0.95	3.62/3.67
	Standard deviation	0.28/0.30	0.26/0.28	0.26/0.27	0.02/0.03	0.02/0.02	0.01/0.01	0.02/0.02	0.26/0.27
	Maximum	6.50/6.24	5.30/5.19	4.45/4.43	1.00/0.99	0.98/0.97	0.87/0.97	0.98/0.94	5.01/5.01
	Minimum	3.75/3.74	3.54/3.43	2.73/2.85	0.69/0.73	0.62/0.68	0.77/0.68	0.73/0.76	3.31/3.32
BF	Average	5.10/5.00	4.36/4.29	3.57/3.63	0.86/0.86	0.83/0.85	0.84/0.83	0.85/0.86	4.29/4.26
	Standard deviation	0.54/0.47	0.34/0.32	0.34/0.34	0.08/0.06	0.07/0.07	0.04/0.05	0.05/0.04	0.32/0.32

258 3.3. Grubbs Test

259 In order to eliminate the abnormal data caused by negligent error, the Grubbs test is used in this  
 260 study. The specific process is as follows:

261 (1) Rank the original test data from small to large, and obtain the average value and the standard  
 262 deviation of the data.

263 (2) Calculate the statistic  $T_i$  according to formula (15), and the results are shown in Table 3.

264 (3) Compare the statistic  $T_i$  with the critical value  $T_{\alpha,n}$  in the Grubbs test table ( $\alpha$  is the significance  
 265 level,  $n$  is the sample size). If  $T_i \geq T_{\alpha,n}$ , it means that  $x_i$  is a discrete value, which must be discarded,  
 266 otherwise it should be reserved.

$$T_i = \frac{\bar{x} - x_i}{S} \quad (i=1, 2, 3, \dots, 100) \tag{15}$$

267 Where,  $x_i$  is sample value;  $\bar{x}$  is sample mean value;  $S$  is sample standard deviation.

268 **Table 3.** Grubbs test results.

	$T_i$	$a$	$b$	$c$	$k$	$\lambda$	$\sigma$	$\varphi$	$d$
CF	FSI	2.92	2.58	2.55	2.56	1.92	3.13	2.46	2.69
	TDS	2.87	2.69	2.61	2.36	2.89	2.78	2.99	2.74
OF	FSI	2.80	2.51	2.29	2.62	2.83	2.94	2.62	2.49
	TDS	2.80	2.42	2.37	3.04	3.17	3.10	2.52	2.30
BF	FSI	2.58	2.82	2.61	2.22	2.87	1.81	2.73	3.06
	TDS	2.70	2.79	2.39	2.21	2.54	3.14	2.44	2.98

269 Query the Grubbs test value table, take  $\alpha = 0.05$ ,  $n = 100$ ,  $T_{0.05,100} = 3.207$ . Comparing the maximum  
 270 value of each method in Table 3 with  $T_{0.05,100}$ , we find that each group of data is less than  $T_{0.05,100}$ . It  
 271 shows that there is no discrete value in the original data of the group, and the data is effective and  
 272 accurate.

273 3.4.F Test

274 The standard deviation can reflect the precision of a set of data. Different sets of data have  
 275 different precision.  $F$  test is needed to test whether there is a significant difference between the two  
 276 sets of data precision. To verify the data precision of the measurement methods, two evaluation  
 277 methods were taken as one set, and the  $F$  test was carried out. The specific process is as follows:

278 (1) Calculate the value of  $F$  according to the formula (16), and the result is shown in Table 4.

$$F = \frac{S_1^2}{S_2^2} \quad (S_1^2 \geq S_2^2) \tag{16}$$

279 (2) Query the critical value in the  $F$  distribution table, take  $\alpha = 0.05$ ,  $n_1 = 100$ ,  $n_2 = 100$ , and the  $F_{0.25}$   
 280  $(99,99) = 1.76$  is obtained. If  $F \leq F_{0.25}(99,99)$ , it means that there is no significant difference between the two  
 281 sets of data precision, otherwise, there is a significant difference.

282 (3) Combined with the  $F$  value of each set of data in Table 4, it is found that each set of data is  
 283 less than  $F_{0.25}(99,99)$ . Therefore, there was no significant difference in the measurement precision  
 284 between the two sets of data.

285 **Table 4.**  $F$  test results.

$F$ test	$a$	$b$	$c$	$k$	$\lambda$	$\sigma$	$\varphi$	$d$
CF	1.03	1.05	1.08	1.60	1.10	1.02	1.53	1.05
OF	1.13	1.16	1.04	1.32	1.07	1.45	1.25	1.10
BF	1.37	1.09	1.00	1.56	1.25	1.65	1.52	1.02

286 **3.5.  $T$  Test**

287 To verify whether there is a significant difference between the mean values of the two sets of  
 288 data, the  $t$  test is needed. Since the test datas of the two sets have same sample size, the  $t$  value is  
 289 calculated according to formula (17), and the results are shown in Table 5.

$$t = |\bar{x}_1 - \bar{x}_2| / \sqrt{\frac{n}{S_1^2 + S_2^2}} \tag{17}$$

290 **Table 5.**  $t$  test results.

$t$ test	$a$	$b$	$c$	$k$	$\lambda$	$\sigma$	$\varphi$	$d$
CF	1.38	1.13	0.97	1.61	0.96	0.99	1.67	1.16
OF	1.17	1.06	1.41	0.41	1.66	0.69	0.21	1.24
BF	1.38	1.37	1.14	0.19	1.91	1.93	1.59	0.56

291 Compare the calculated  $t$  value with  $t_{\alpha, (n_1+n_2-2)}$  in the table of  $t$  distribution, if  $t \leq t_{\alpha, (n_1+n_2-2)}$ , it  
 292 indicates that there is no significant difference between the average values of the two groups of data.  
 293 Taking  $\alpha = 0.05$ ,  $t_{0.05, 198} = 1.98$  and combining the data in Table 5, it is found that the data of each  
 294 group is less than  $t_{0.05, 198}$ . Therefore, there is no significant difference between the average values of  
 295 the data of each set.

296 **3.6. Results Analysis**

297 From the above results of the Grubbs test,  $F$  test, and  $t$  test, there is no significant difference  
 298 between the test data of each set measured by the two measurement methods, indicating that both  
 299 the two measurement methods can accurately measure the particle shape of fertilizer. The 3D  
 300 scanning method needs more professional knowledge, and the post-processing time is longer. The  
 301 instrument and method proposed in this paper can collect the top and side images of the fertilizer  
 302 automatically, which can measure the fertilizer shape characteristics non-destructively, efficiently,  
 303 accurately, and stably. So, it can replace the 3D scanning method to measure fertilizer shape  
 304 characteristics.

305 **4. Conclusions**

306 In order to measure the fertilizers shape characteristics accurately, we propose a precision  
 307 measuring instrument of fertilizer shape characteristics as well as its measuring method. The main  
 308 conclusions of this paper are listed in the following:

309 (1) A measuring instrument and method of fertilizer shape characteristics are developed based  
 310 on the binocular vision, which provided a theoretical basis for fertilizer production and quality  
 311 inspection. The instrument adopts the intermittent static collection mode to collect the top and side  
 312 images of the fertilizer at one time. The method adopts the edge detection algorithm based on the

313 directional gradient to extract the contour of the fertilizer image accurately.

314 (2) Fertilizer shape characteristics were measured by the three-dimensional scanning method  
 315 and the method proposed in this paper. The test data were tested by the Grubbs test,  $F$  test, and  $t$  test.  
 316 The results showed that  $T < T_{0.05,100}$ ,  $F < F_{0.025(99,99)}$ , and  $t < t_{0.05,198}$ . It indicated that no significant difference  
 317 was found between the measurement results, and the measuring instrument and method were  
 318 accurate and reliable.

319 (3) The measuring test of three fertilizers has been completed by the instrument and method  
 320 proposed in this paper. With the popularization of slow-release fertilizer and controlled-release  
 321 fertilizer, and the increasingly variety of fertilizers, the other fertilizers types also need to be tested  
 322 and verified.

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