

1st International Electronic Conference on Applied Sciences

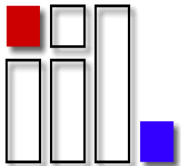
# Deep Anomaly Detection via Morphological Transformations

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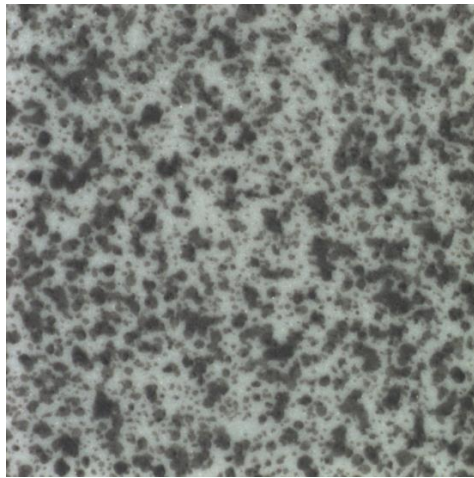
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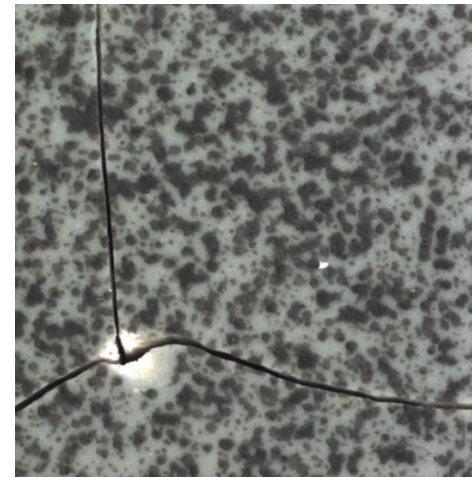


# Real-world industrial anomaly detection

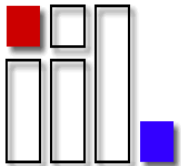
- The goal of deep anomaly detection is to identify abnormal data by utilizing a deep neural network trained by a normal training dataset
- Industrial visual anomaly detection problems generally **distinguish normal and abnormal data through small morphological differences**, such as crack and stain.



normal



abnormal



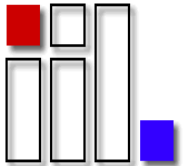
# Semantic differences VS Morphological differences

- Nevertheless, **most existing algorithms focused on capturing not morphological features but semantic features of normal data.**

**Semantic difference**



**Morphological difference**

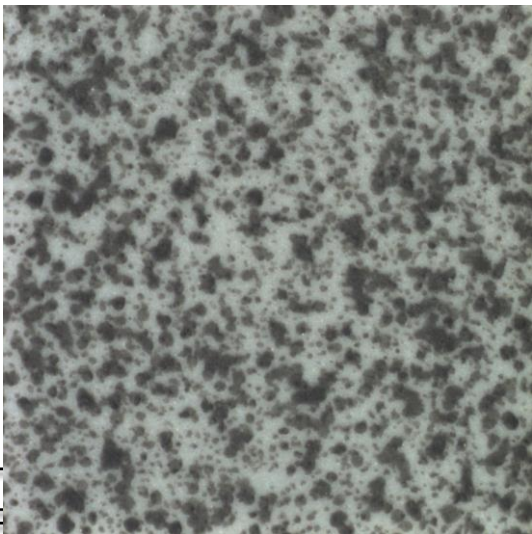


# Morphological transformations - Erosion

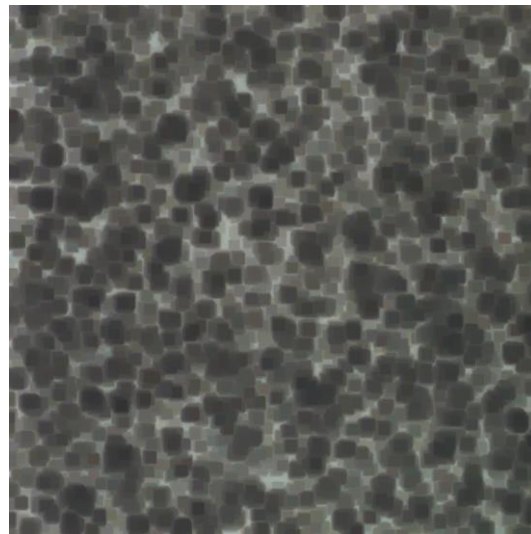
- Erosion computes the minimum pixel value of image  $i$  in every neighborhood of  $(x, y)$ , coincident with kernel  $b$ , it is expected that the size of bright features in  $i$  will be reduced

$$[i \ominus b](x, y) = \min_{(s,t) \in b} i(x + s, y + t)$$

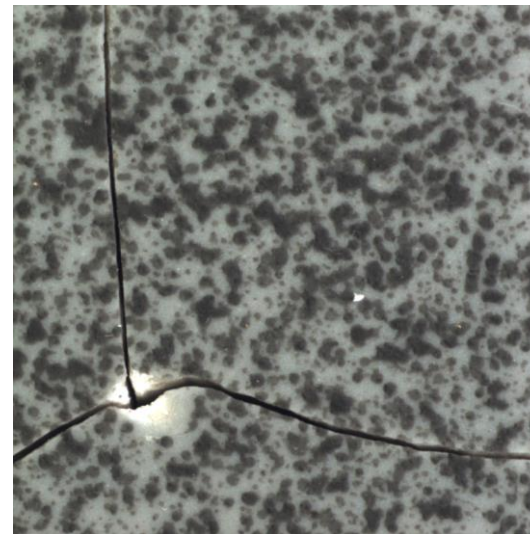
**Normal**



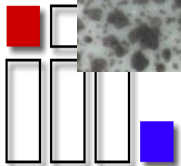
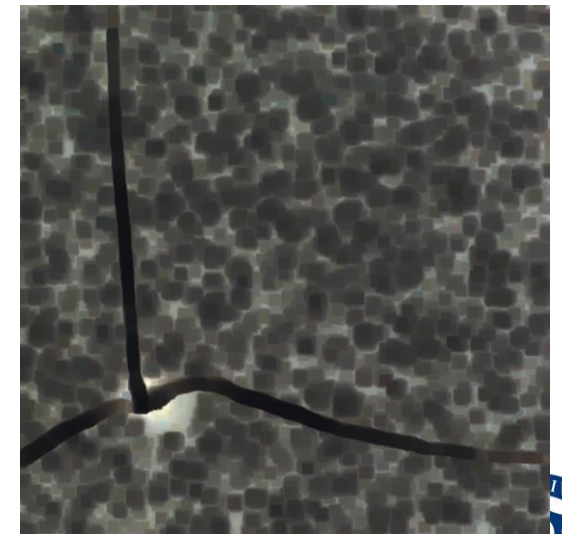
**Eroded normal**



**Abnormal**



**Eroded abnormal**

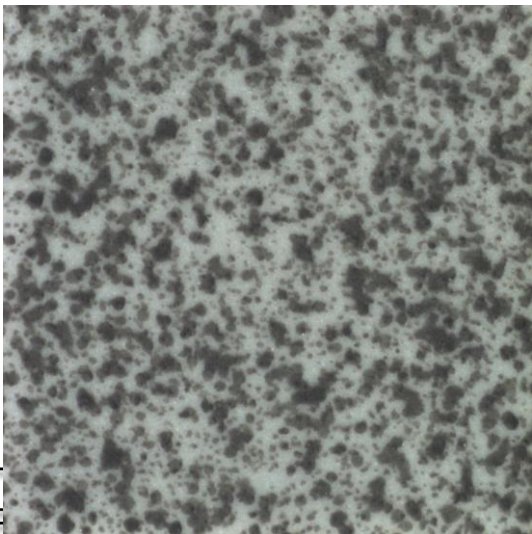


# Morphological transformations - Dilation

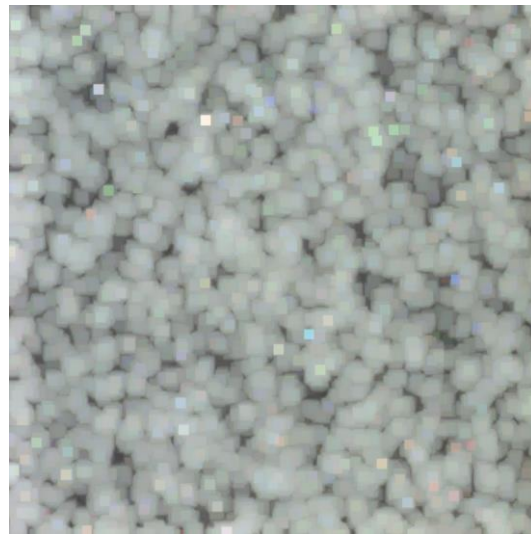
- Dilation computes the maximum pixel value of image  $i$  in every neighborhood of  $(x, y)$ , coincident with kernel  $b$ , it is expected that the size of darker features in  $i$  will be reduced

$$[i \oplus b](x, y) = \max_{(s,t) \in b} i(x + s, y + t)$$

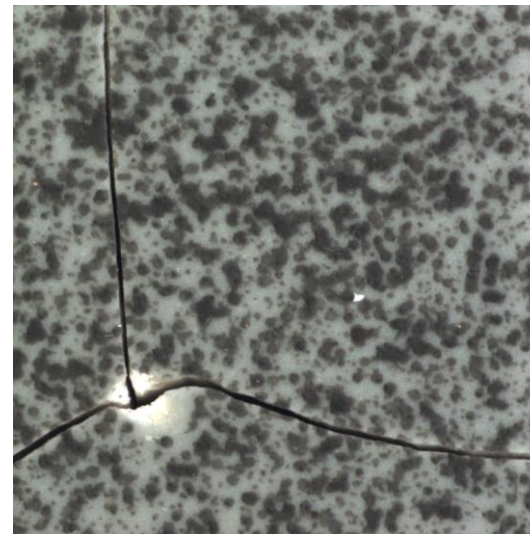
**Normal**



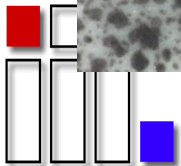
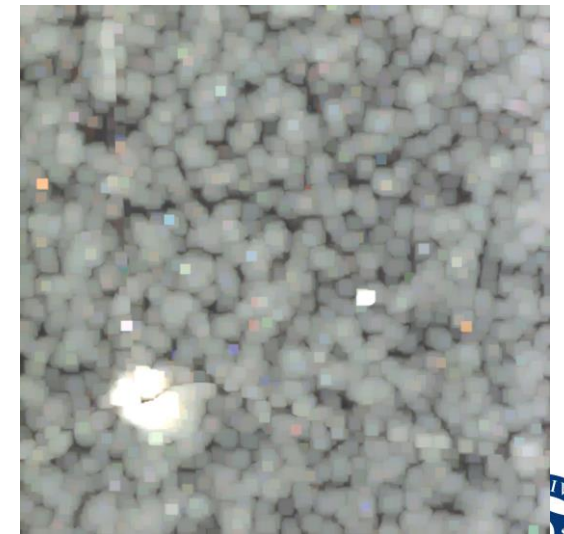
**Dilated normal**



**Abnormal**



**Dilated abnormal**

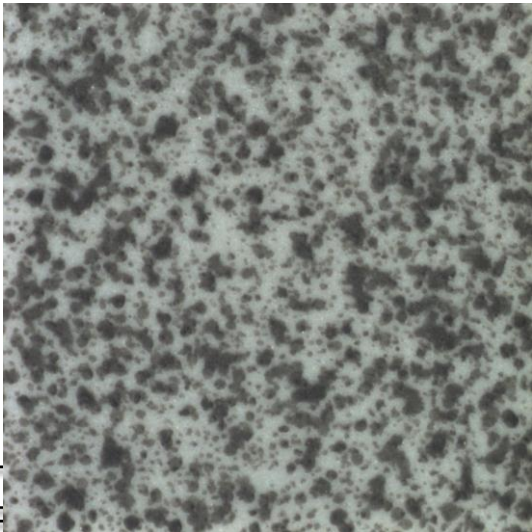


# Morphological transformations – Morphological gradient

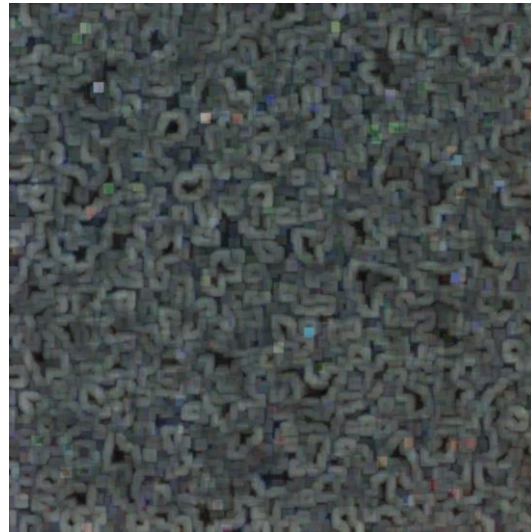
- To obtain the morphological gradient of an image, dilation and erosion can be used in combination with image subtraction.

$$i \odot b = (i \oplus b) - (i \ominus b)$$

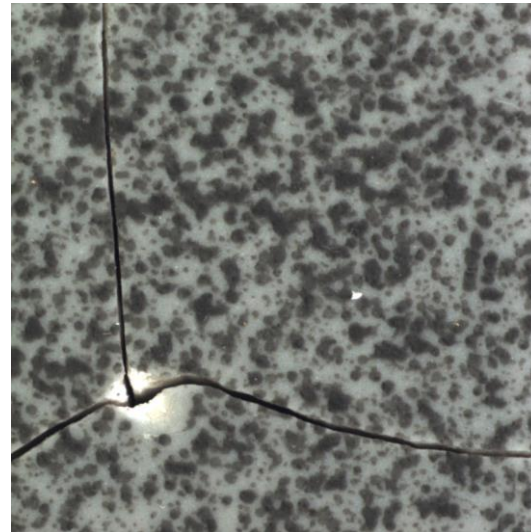
**Normal**



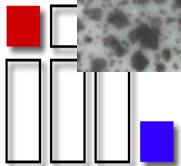
**Dilated normal**



**Abnormal**

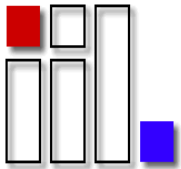
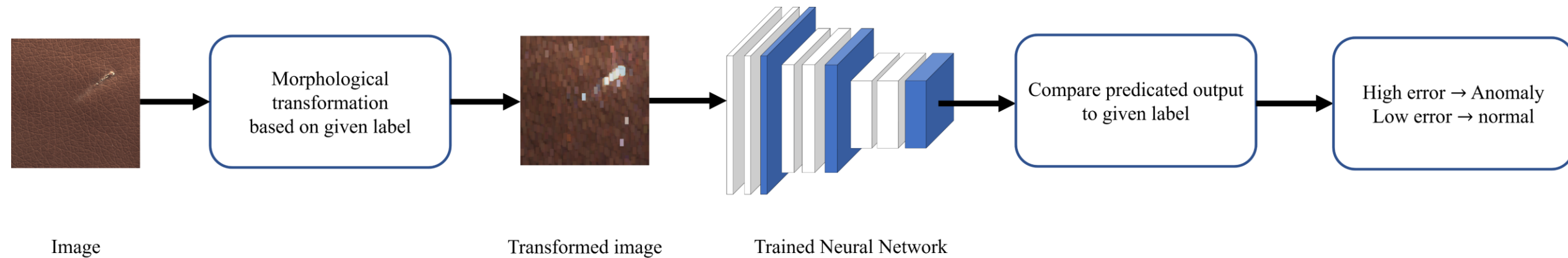


**Dilated abnormal**



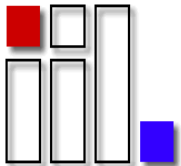
# The proposed deep anomaly detection

- The proposed deep anomaly detection aims to discriminate the abnormal data using the acquired morphological features of normal data in the training procedure.
- Therefore, if a given morphological transformed data generates a high prediction error, it can be considered abnormal.



# Objective function

- The proposed algorithm aims to train deep neural network-based morphological features in a self-supervised learning manner.
- To achieve this goal, we propose to train a deep neural network  $F$  to discriminate the morphological transformation types applied to an image that is given to it as input.
- Specifically, we define a set of  $N_1$  **discrete morphological transformations**,  $N_2$  **discrete values for kernel width**, and  $N_3$  **discrete values for kernel height**.





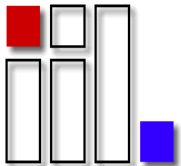
# Objective function

- We define a set of  $N_1 N_2 N_3$  discrete morphological transformations as follows:

$$G = \{g(\cdot | n_1, n_2, n_3)\}_{n_1=1, n_2=1, n_3=1}^{N_1, N_2, N_3},$$

where  $g(\cdot | n_1, n_2, n_3)$  denotes that applies to image  $i$  the morphological transformation with multi-class label  $\{n_1, n_2, n_3\}$  that produces the transformed image  $i^{n_1, n_2, n_3} = g(i | n_1, n_2, n_3)$ .

- The deep neural network  $F$  takes an input as transformed image  $i^{n_1^*, n_2^*, n_3^*}$  where the label  $\{n_1^*, n_2^*, n_3^*\}$  is unknown to  $F$ .

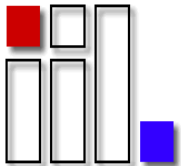


# Objective function

- The deep neural network  $F$  takes an input as transformed image  $i^{n_1^*, n_2^*, n_3^*}$  where the label  $\{n_1^*, n_2^*, n_3^*\}$  is unknown to  $F$ .
- It produces a probability distribution of softmax response over all possible morphological transformations, which is denoted as follows:

$$F(i^{n_1^*, n_2^*, n_3^*} | \theta) = \{F^{n_1, n_2, n_3}(i^{n_1^*, n_2^*, n_3^*} | \theta)\}_{n_1=1, n_2=1, n_3=1}^{N_1, N_2, N_3}$$

where  $F^{n_1, n_2, n_3}(i^{n_1^*, n_2^*, n_3^*} | \theta)$  is the predicted probability for morphological transformation with  $\{n_1^*, n_2^*, n_3^*\}$  and  $\theta$  denotes the parameters of  $F$ .



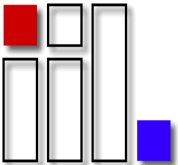
# Objective function

- Consequently, the proposed self-supervised objective function to capture morphological features of normal data is as follows:

$$\min_{\theta} \frac{1}{3T} \sum_{j=1}^T \left( -\frac{1}{N_1} \sum_{n_1=1}^{N_1} \log \left( F^{n_1}(i^{n_1^*, n_2^*, n_3^*} | \theta) \right) - \frac{1}{N_2} \sum_{n_2=1}^{N_2} \log \left( F^{n_2}(i^{n_1^*, n_2^*, n_3^*} | \theta) \right) - \frac{1}{N_3} \sum_{n_3=1}^{N_3} \log \left( F^{n_3}(i^{n_1^*, n_2^*, n_3^*} | \theta) \right) \right)$$

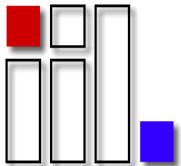
where  $F^{n_1}(i^{n_1^*, n_2^*, n_3^*} | \theta)$ ,  $F^{n_2}(i^{n_1^*, n_2^*, n_3^*} | \theta)$ , and  $F^{n_3}(i^{n_1^*, n_2^*, n_3^*} | \theta)$  denote predicted probability for  $n_1^*$ ,  $n_2^*$ , and  $n_3^*$ , respectively.

- Through the above formulation, we enforce the deep neural networks to learn morphological features of normal by predicting both transformation type and kernel size simultaneously.



# Experimental results – implementation details

- In the experimental results, there are three types of the proposed method to **verify kernel size learning's influence**;
  - **Type 1:**  $n_1 \in \{Erosion, Dilation, Gradient\}$ ,  $n_2 \in \{1, 28, 56\}$ ,  $n_3 \in \{1, 28, 56\}$
  - **Type 2:**  $n_1 \in \{Erosion, Dilation, Gradient\}$ ,  $n_2 \in \{8, 28, 56\}$ ,  $n_3 \in \{8, 28, 56\}$
  - **Type 3:**  $n_1 \in \{Erosion, Dilation, Gradient\}$ ,  $n_2 \in \{1, 8, 28, 56\}$ ,  $n_3 \in \{1, 8, 28, 56\}$
- PyTorch with RTX 2080Ti 11GB GPU and Intel i7 CPU.

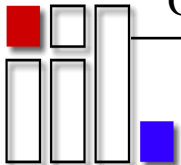


# Experimental results

- Comparison of AUROC (area under the receiver operating characteristic, %) performance between [1] and the proposed algorithm in MVTec dataset.

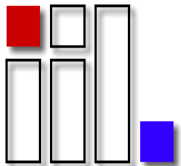
Class	bottle	cable	capsule	carpet	grid	hazelnut	leather
[1]	83.10	77.81	75.31	38.12	<b>31.47</b>	67.14	64.10
Ours-type 1	87.86	76.89	<b>77.50</b>	57.22	15.62	68.71	39.67
Ours-type 2	88.41	77.55	69.92	53.97	29.91	62.29	66.58
Ours-type 3	<b>95.16</b>	<b>80.34</b>	73.08	<b>57.91</b>	29.99	<b>68.04</b>	<b>82.88</b>
Class	pill	screw	tile	toothbrush	transistor	wood	average
[1]	62.17	27.73	52.13	82.73	<b>88.25</b>	84.30	64.18
Ours-type 1	50.60	28.06	84.70	<b>93.33</b>	77.92	85.44	63.17
Ours-type 2	51.72	46.96	92.71	70.22	84.04	<b>90.96</b>	66.19
Ours-type 3	<b>57.23</b>	<b>61.86</b>	<b>93.58</b>	91.67	83.29	87.37	<b>72.92</b>

[1] Golan, Izhak, and Ran El-Yaniv. "Deep anomaly detection using geometric transformations." *Advances in Neural Information Processing Systems*. 2018.



# Conclusion

- The proposed method achieves superior performance in deep anomaly detection on industrial inspection by training the deep neural network to capture salient morphological features of normal data.
- The proposed algorithm can flexibly adapt to various real-world deep anomaly detection problem by choosing the adequate morphological transformation in image processing technology.
- Because the proposed methodology utilizes self-supervised learning, it has low computational complexity than other deep anomaly detection methods such as reconstruction-based algorithm.



**Thank You!**

**Deep Anomaly Detection  
via Morphological Transformations**

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