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## 2 **Diurnal dynamics of the reduced turbulent kinetic** 3 **energy in the atmospheric boundary layer from** 4 **minisodar measurements**

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11 **Abstract:** Based on acoustic remote measurements of the diurnal dynamics of three wind velocity  
12 components and their variances in the lower 200-meter layer of the atmosphere, the kinetic energy  
13 of the atmosphere reduced to unit mass is estimated, with a particular emphasis on the turbulent  
14 kinetic energy component. For a 24-h period of continuous minisodar observations, the turbulent  
15 energy in the surface layer was very low to altitudes of ~50 m. With increase in altitude from 50 to  
16 100 m, the turbulent kinetic energy quickly increased, and at altitudes exceeding 100 m, its fast  
17 growth is observed, with a maximum at altitudes of 150–200 m. Essential influence of time of the  
18 day on the results of observations was established. Thus, at night at the same altitudes the kinetic  
19 energy density first did not exceed 20 J/kg, and its moderate growth (from 20 to 50 J/kg) was  
20 observed with increasing time. In the morning, the maximum energy density of air masses was  
21 observed. After sunrise, the turbulent component of the kinetic energy density rapidly decreased.  
22 It is essential that the system the Earth surface – the near-ground air layer tends to an equilibrium  
23 state. As a consequence, the spread of values of the turbulent energy is reduced. The most significant  
24 changes were observed at altitudes in the range 100–200 m. It is essential that at altitudes up to 50–  
25 100 m, time of the day had no significant effect, because at these altitudes the turbulent energy was  
26 low and remained practically unchanged with time. Irrespective of time of the day, the maximum  
27 turbulent energy was observed at altitudes in the range 100–200 m that pose the greatest danger to  
28 small flying objects. The corresponding estimations are presented.

29 **Keywords:** atmospheric boundary layer; reduced kinetic energy of the atmosphere; turbulence  
30 kinetic energy; diurnal dynamics; acoustic sounding; minisodar  
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### 32 **1. Introduction**

33 The kinetic energy plays an important role in physics of the atmospheric boundary layer (ABL),  
34 investigation of its structure and dynamics, development of adequate physical representations, and  
35 construction of realistic mathematical models [1–3]. It is one of the main characteristics of the ABL,  
36 defining both global and local circulations in the atmosphere and momentum, heat, and mass  
37 transfer. Moreover, it is necessary for the forecasting and calculating fields of meteorological  
38 parameters and diffusion of pollutants and for analyzing and forecasting conditions of acoustic  
39 radiation propagation. The importance of ABL investigations has significantly increased recently in  
40 connection with revolutionary development and application of unmanned aerial vehicles (UAVs),

41 especially mini and micro dimensional UAVs made of light materials and subject to strong influence  
42 of the turbulent kinetic energy [4].

43 A number of lidar, sodar, and radar methods are being developed for measuring and forecasting  
44 average values and variances of the wind velocity components in the ABL (for example, see [5–8]).  
45 Each of them has its own advantages and disadvantages. For example, the refractive index of sound  
46 waves is about  $10^6$  times higher than of radio or optical waves. Strong interaction of sound waves  
47 with the atmosphere and the ability to obtain information in real time and round the clock with much  
48 higher spatial and temporal resolution make sodars unique tools for investigation of the wind  
49 velocity vector field in the ABL. The application of the Doppler acoustic radars (sodars) allows  
50 simultaneously long time series of continuous observations of vertical profiles of both average values  
51 and variances of three wind velocity components to be obtained in real time [3, 7, 9]. The data with  
52 high spatial (up to several meters) and temporal resolution (statistically reliable profiles of wind  
53 velocity components with averaging from 1 to 30 min) can be obtained, and their spatiotemporal  
54 dynamics can be analyzed. As a result, this allows the data of minisodar measurements to be used  
55 for estimating the kinetic energy of both average and turbulent motions of air masses in the ABL.  
56 Thus, in [9] results of preliminary analysis of the spatiotemporal dynamics of the kinetic energy of  
57 the atmosphere reduced to unit air mass retrieved from data of minisodar measurements were  
58 presented.

59 The paper presents the results of investigations of the kinetic energy  $E(z, t)$  of the ABL at the  
60 altitudes  $z = 5\text{--}200$  m from minisodar measurements with the spatial resolution  $\Delta z = 5$  m in the  
61 morning, daytime, and evening hours and also its diurnal hourly dynamics. The relative  
62 contributions of the energy of average motion and of the turbulent kinetic energy are also analyzed.

## 63 2. Applied methods and approaches

64 The kinetic energy of the ABL  $E_{\Sigma} = mV^2 / 2$  is defined by the energy of motion of air masses –  
65 the wind energy. Below we consider the kinetic energy of the ABL reduced to unit air mass  
66  $E = E_{\Sigma} / m$  and measured in  $\text{m}^2/\text{s}^2$  ( $\text{m}^2/\text{s}^2 = \text{J}/\text{kg}$ ). It is natural that the regularities in the  
67 spatiotemporal behavior of the reduced kinetic energy will fully concern the total kinetic energy. For  
68 this reason, below we use the term *kinetic energy* for the kinetic energy per unit air mass. It is equal to  
69 the sum of two components: the kinetic energy of ordered motion  $E_{\text{MKE}}$ , associated with the average  
70 wind velocity, and the kinetic energy of turbulent motion of air masses  $E_{\text{TKE}}$ , associated with the wind  
71 velocity variance, and can be written as [1–3]

$$72 \quad E = (E_{\text{MKE}} + E_{\text{TKE}}) / m. \quad (1)$$

73 A Doppler acoustic radar (sodar) allows long-term continuous observations to be performed of the  
74 spatiotemporal dynamics of both average values and variances of the three wind velocity  
75 components in the ABL and hence the spatiotemporal dynamics of the kinetic energy of the  
76 atmosphere to be investigated. The kinetic energy components  $E_{\text{MKE}}$  and  $E_{\text{TKE}}$  were calculated from  
77 the data of minisodar measurements using the formulas [9, 10]:

$$\begin{aligned}
 E_{\text{MKE}}(z_j, t_k) &= \left[ \langle V_x(z_j, t_k) \rangle^2 + \langle V_y(z_j, t_k) \rangle^2 + \langle V_z(z_j, t_k) \rangle^2 \right] / 2 \\
 &= \frac{1}{N^2} \left[ \left( \sum_{i=1}^N V_{xij}(z_j, t_k) \right)^2 + \left( \sum_{i=1}^N V_{yij}(z_j, t_k) \right)^2 + \left( \sum_{i=1}^N V_{zij}(z_j, t_k) \right)^2 \right] / 2,
 \end{aligned} \tag{2}$$

$$\begin{aligned}
 E_{\text{TKE}}(z_j, t_k) &= (\sigma_x^2(z_j, t_k) + \sigma_y^2(z_j, t_k) + \sigma_z^2(z_j, t_k)) / 2 = \frac{1}{N^2} \\
 &\times \left[ \left( \sum_{i=1}^N V_{xij}(z_j, t_k) - \langle V_x(z_j, t_k) \rangle \right)^2 + \sum_{i=1}^N \left( (V_{yij}(t_k) - \langle V_y(z_j, t_k) \rangle)^2 + \sum_{i=1}^N \left( (V_{zij}(t_k) - \langle V_z(z_j, t_k) \rangle)^2 \right) \right) \right] / 2,
 \end{aligned} \tag{3}$$

where  $V_{mij}(z_j, t_k)$ ,  $m = x, y, z$  are the wind velocity components measured with a minisodar in the  $j$ th range gate at altitude  $z_j$  in the  $k$ th series of minisodar measurements started at time  $t_k$ ,  $\langle V_m(z_j, t_k) \rangle$  are their 10-min averages, and  $\sigma_m^2(z_j, t_k)$  are their variances.

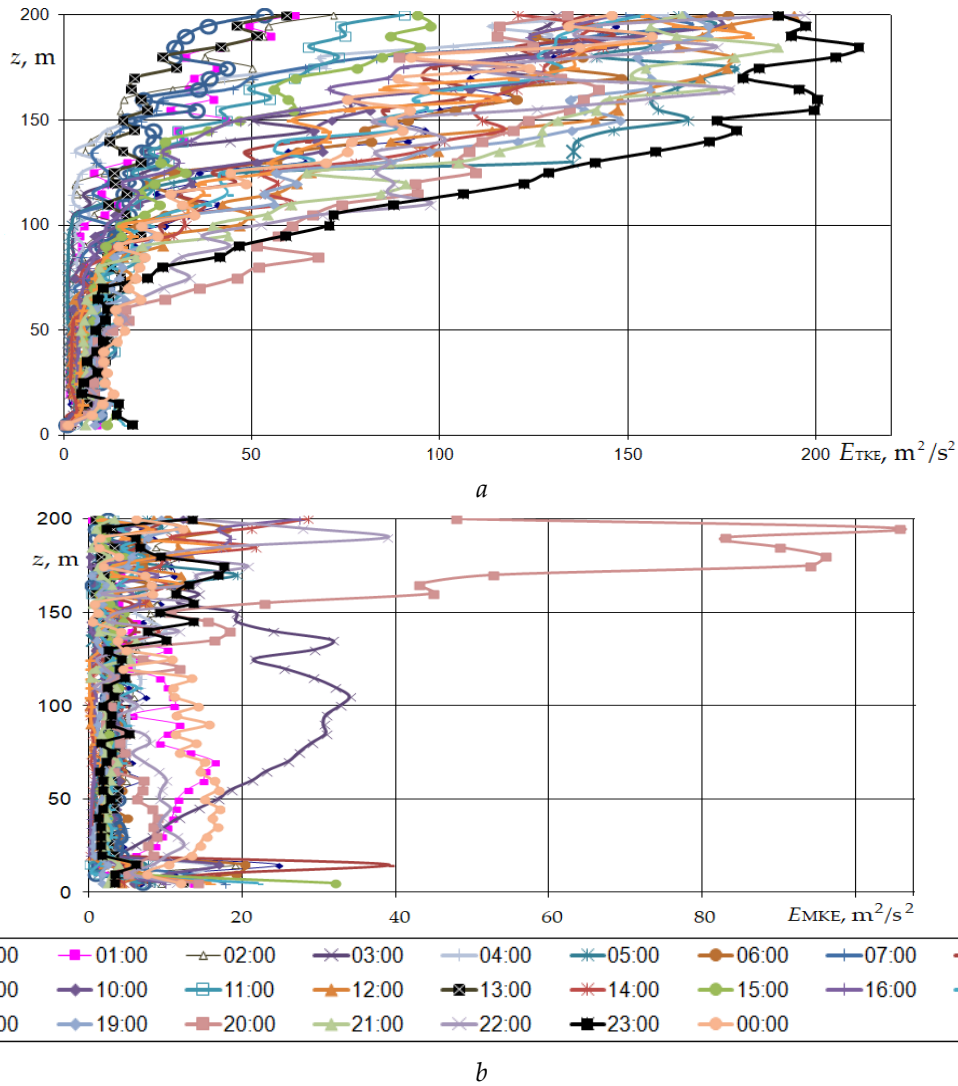
### 3. Results and discussion

We processed the results of measurements performed in the vicinity of Santa Clarita, California, USA, with an AV4000 minisodar from 12 till 17 September, 2006 [11]. The working frequency of the minisodar was 4900 Hz, its pulse duration was  $\tau = 60$  ms, and pulse repetition period was 4 s. Acoustic radiation was periodically transmitted in three directions – vertical and at elevation angles of  $76^\circ$  in two mutually orthogonal planes. The vertical profiles of three wind velocity components  $V_{mij}(z_k)$ ,  $m = x, y, z$  were measured in 43 range gates  $z_k$  with  $\Delta z = 5$  m in the altitude range 5–200 m. The measurement site was relatively level, with no pronounced highs or lows, without high vegetation. The weather was dry, warm, and sunny. Measurement series from  $N$  profiles ( $N = 150, 300$ , and 450) were processed that provided from 10 to 30 min averaging of the results obtained.

Results of investigations of the spatiotemporal dynamics of the kinetic energy  $E(z, t)$  and their diurnal hourly dynamics are presented below. A special attention is given to the turbulent kinetic energy component. Figure 1 shows the vertical profiles of the kinetic energy components from the results of processing of the minisodar data. It illustrates the diurnal hourly dynamics of the kinetic energy components on September 14. The start times  $t_k$  of 10-minute measurement series are indicated under the figure. Attention is drawn to a small spread of  $E_{\text{TKE}}$  values up to altitudes  $z \approx 50$  m, and their largest spread from  $E_{\text{TKE min}} = 50 \text{ m}^2/\text{s}^2$  at 09:00 to  $E_{\text{TKE max}} = 200 \text{ m}^2/\text{s}^2$  at 23:00 at  $z \approx 200$  m. From 10:00 till 12:00, the contribution of the kinetic energy of average motion in the lower 100-meter layer exceeded the contribution of the turbulent kinetic energy component, which was probably caused by the presence of wind shears in the corresponding vertical profiles of the horizontal wind velocity components. From the figure it is also seen that  $E_{\text{MKE}}$  increases in the morning from 05:00, reaches maximum values at 12:00, and then decreases till the midnight. The maximum value of the turbulent kinetic energy at the altitude  $z = 200$  m was observed at 05:00, and the minimum one in the morning at 07:00, local time. The analogous behavior of the kinetic energy was also pointed out in [3] from measurements with a FAS64 sodar at three altitude ranges  $z = 20\text{--}50, 50\text{--}80$ , and  $80\text{--}110$  m. According

109 to [3], the diurnal behavior of the turbulent kinetic energy was also characterized by the presence of  
 110 minima and maxima. It is obvious that the time of their occurrence and their values depend on the  
 111 meteorological conditions of observations, the presence and characteristics of cloudiness, and solar  
 112 radiation.

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118 Fig. 1. Diurnal hourly dynamics of the kinetic energy components on September, 14 with 10-minute  
 119 averaging:  $a$  – turbulent kinetic energy  $E_{TKE}$  and  $b$  - kinetic energy of ordered motion  $E_{MKE}$  (associated  
 120 with the average wind velocity).

121 During three days of continuous sodar measurements (on September 12, 14, and 15), the total  
 122 kinetic energy changed from several ten to several hundred  $m^2/s^2$ , which is in agreement with the  
 123 available literature data [3, 12]. From the figure it can also be seen that the turbulent kinetic energy  
 124 increased with altitude  $z$ . In the near-surface layer to altitudes of 25–50 m, it weakly depends on  $z$ .  
 125 Thus, on September 12, it changed from 10 to 90  $m^2/s^2$  at  $z = 25$  m; on September 14 and 15, it remained  
 126 practically unchanged to  $z = 50$  m. From Fig. 1 it is also seen that the diurnal spread of the kinetic  
 127 energy increases with  $z$ , and at an altitude of 200 m,  $E_{TKE}$  changes already from 70 to 200  $m^2/s^2$ , that  
 128 is, almost triples during the day. Analogous behavior of the turbulent kinetic energy was observed  
 129 in [3, 12]. It should be noted that our analysis of the influence of the averaging period (10, 20, or 30

130 min) on the  $E$  values performed in [9] demonstrated that they were practically independent of the  
131 averaging time for these averaging periods. The same is true for the case under consideration. The  
132 general peculiarities retained for other averaging periods; therefore, we do not consider them here.  
133 Thus, based on the data presented above we can conclude that the kinetic energy in the surface layer  
134 to altitudes of 25–100 m weakly depends on the observation altitude  $z$  (which we explain by the  
135 presence of the mixing layer at these altitudes) and increases with further increase in  $z$ . The diurnal  
136 behavior of the radiative heating of the Earth's surface causes the presence of minima and maxima of  
137 the total kinetic energy, whose observation times depend on the local weather conditions.

#### 138 4. Conclusions

139 Based on acoustic remote measurements of the diurnal dynamics of the three wind velocity components  
140 and their variances in the lower 200-meter layer of the atmosphere, the kinetic energy of the atmosphere reduced  
141 to unit mass has been estimated, with a particular emphasis on the turbulent kinetic energy component. For a  
142 24-h period of continuous minisodar observations, the turbulent kinetic energy in the surface layer was very  
143 low to altitudes of ~50 m. With increase in altitude from 50 to 100 m, the turbulent kinetic energy quickly  
144 increased, and at altitudes exceeding 100 m, its fast growth was observed, with a maximum at altitudes of 150–  
145 200 m.

146 Essential influence of time of the day on the results of observations was established. Thus, the kinetic  
147 energy at night at the same altitudes first did not exceed 20 J/kg, and its moderate growth (from 20 to 50 J/kg)  
148 was observed with increasing time. In the morning, the maximum kinetic energy was observed. After sunrise,  
149 the turbulent component of the kinetic energy rapidly decreased. It is essential that the system the Earth surface  
150 – the near-ground air layer tends to an equilibrium state. As a consequence, the spread of values of the turbulent  
151 energy is reduced. The most significant changes were observed at altitudes in the range 100–200 m. It is  
152 important that at altitudes up to 50–100 m, the time of the day had no significant effect, because at these altitudes  
153 the turbulent kinetic energy was low and remained practically unchanged with time. Irrespective of the time of  
154 the day, the maximum turbulent energy was observed at altitudes in the range 100–200 m. This suggests that  
155 this altitude range poses the greatest danger to light UAOs.

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157 L.Sh., A.P. and V.K.; validation, L.Sh., A.P. and V.K.; formal analysis, L.Sh., A.P. and V.K.; investigation, L.Sh.,  
158 A.P. and V.K.; resources, L.Sh., A.P. and V.K.; data curation, L.Sh., A.P. and V.K.; writing—original draft  
159 preparation, L.Sh., A.P. and V.K.; writing—review and editing, L.Sh., A.P. and V.K.; visualization, L.Sh., A.P.  
160 and V.K.; supervision, L.Sh., A.P. and V.K.; project administration, L.Sh., A.P. and V.K.; funding acquisition,  
161 L.Sh., A.P. and V.K. All authors have read and agreed to the published version of the manuscript.

162 **Conflicts of Interest:** The authors declare no conflict of interest.

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