

# Techno-economic evaluation and optimization of batch, fed-batch and multistage continuous crystallization processes<sup>†</sup>

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**Abstract:** Over the last decade, continuous manufacturing techniques have been widely used in the pharmaceutical manufacturing industry. However, despite the outstanding performance associated with the steady-state operation, continuous processes face common and important challenges of low efficiency and material waste during the start-up and shutdown. Considering that most pharmaceutical manufacturing is accomplished in a short operation window, an ideal start-up and shut down strategy will have a significant impact on the economic and environmental performance of the continuous pharmaceutical process. In this study, a combined start-up, steady-state, and shutdown optimization of a three-stage mixed suspension mixed product removal (MSMPR) crystallizer was compared against optimized batch and fed-batch crystallizers. The crystallization of aspirin (acetylsalicylic acid, ASA) in ethanol (solvent) and water (antisolvent) was used as a case study. The optimization problems were solved using a hybrid method, which combines a genetic algorithm and a sequential quadratic programming (SQP) method. The multistage continuous crystallizer was designed and optimized to maximize on-spec production over a total operating window of 800 min. It was shown that a max on-spec production of 5510 g can be achieved with the continuous process. A batch and a fed-batch crystallizer were designed and optimized to achieve the same production rate and help establish a reliable basis for rigorous techno-economic analysis and comparison.

**Keywords:** Crystallization, Dynamic optimization, Continuous Crystallization, Fed-batch, Decision making

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## 1. Introduction

Over the past decade, the pharmaceutical industry has witnessed a clear trend towards the adoption of continuous manufacturing instead of the traditional batch processing which is commonly adopted in the pharmaceutical and biopharmaceutical industries. Compared to the traditional batch operation, continuous processing shows several advantages such as enhanced flexibility, efficiency, and higher product quality. Moreover, there is an expectation that moving from batch to continuous will reduce scale-up efforts and costs and prevent the risks of out-of-specification products due to batch-to-batch variations.

Crystallization is the critical purification unit in most pharmaceutical manufacturing processes. The successful development of continuous crystallization is an essential step when moving from batch to continuous process due to its significant impact on the product quality of the drug such as safety and efficacy which can be determined by crystal size distribution and purity. In addition, these critical properties have a clear impact on downstream processability such as filterability. To achieve the targeted quality performance, a typical optimization objective in crystallization is to maximize the mean crystal

size [1,2]. The driving force of the crystallization is supersaturation, which can be generated by cooling, solvent evaporation or antisolvent addition. Various approaches have been adopted to design and control batch crystallization processes in the literature. For continuous process, most literature focused on three main types of continuous crystallizers (MSMPR, Plug flow reactor and continuous oscillatory baffled crystallizers). The most popular crystallizers in the pharma industry are based on stirred tank design and as such, many experimental and modelling efforts have been devoted to the continuous MSMPR crystallizers, in the recent years. Several studies were particularly devoted to the optimization of single, multistage MSMPR, crystallization network and integrated end-to-end continuous pharmaceutical plant with a series of MSMPR crystallizers [3–5].

Most recently, a systematic optimization of a multistage continuous crystallization, which combines start-up, steady-state and shut down process, has been developed in the case Aspirin (ASA) antisolvent crystallization [6]. With the optimized start-up and shut down strategy, 5510.2 g (417  $\mu\text{m}$ ) of ASA crystals are produced. To compare the performance of the continuous process against the batch or fed batch process, a series of batch process optimization were developed in this study. to produce the same product with the same mean crystal size. Several alternative batch capacities and batch times were evaluated discussed to provide precious insights to the decision maker when it comes to select a batch or continuous crystallization process.

## 2. Method

The crystallization of ASA in a mixture of ethanol and water is considered in this work. The dynamic mathematical model of a fed-batch process was built based on several assumptions, including:

- All vessels are assumed to be well mixing
- Crystal breakage and agglomeration are negligible
- Mixing solvent and antisolvent, crystallization do not affect the total volume

The fed-batch process setup and a three-stage MSMPR crystallizer are illustrated in figure 1.

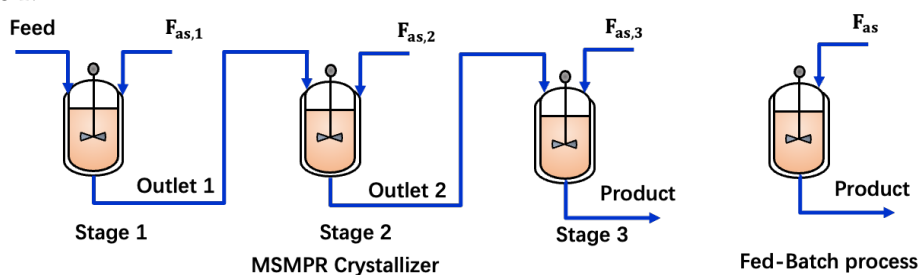


Figure 1. The setup of fed-batch crystallizer and MSMPR crystallizer.

The model of the ASA crystallization process is developed including a population balanced model solved using the standard method of moments. The details of the continuous process with a three-stage MSMPR have been thoroughly discussed in the previous work[6]. For the batch process, with the standard method of moments, the moments of the fed-batch process are shown in Eq 1 and Eq 2.

$$\frac{d\mu_0}{dt} = B \quad (1)$$

$$V \frac{d\mu_j}{dt} = G j \mu_{j-1} V - \mu_j F_{AS}, j = 1, 2, 3 \quad (2)$$

where B is the nucleation rate, and G is the growth rate. Both are adopted from the literature [7]. The V is the volume of the solution. The  $F_{AS}$  is the addition antisolvent flow rate.

The fed-batch process is first prepared with prefilled solution, which is saturated at 40 °C with 25% antisolvent (water) and 75% solvent (ethanol) in mass. When the crystallization starts, the additional antisolvent is added to the vessel, and the temperature of the jacket is controlled to generate supersaturation, which is the driving force for the crystallization process. As such, the mass balance can be developed as follow (Eq 3 and Eq 4):

$$\frac{dM_{ASA}}{dt} = -3\rho_c k_v G \mu_2 V \quad (3)$$

$$\frac{dM_{AS}}{dt} = F_{AS} \quad (4)$$

$M_{ASA}$  and  $M_{AS}$  are the mass of ASA and antisolvent in the vessel. There is no additional solvent. The mass of solvent will remain constant during the process. The  $\rho_c$  is the density of crystals and  $k_v$  is the shape factor.

Besides, the energy balance is also considered in this work. The energy balance equation is shown below:

$$\frac{dT}{dt} = (UA(T_j - T) - 3\Delta H k_v \rho_c \mu_2 G) / (C_{p,mix} M_T) \quad (5)$$

$$C_{p,mix} = \frac{M_S C_{p,S} + M_{AS} C_{p,AS} + M_{ASA} C_{p,ASA}}{M_S + M_{AS} + M_{ASA}} \quad (6)$$

U is the overall heat transfer coefficient, and A is the heat transfer area.  $T_j$  is the jacket temperature and T is the temperature of the solution.  $C_{p,S}$ ,  $C_{p,AS}$  and  $C_{p,ASA}$  are the capacity of the solution, antisolvent and ASA respectively.

With the developed model, an optimization scenario of the fed-batch crystallization is developed. The mathematical formulation of the optimization problem is shown below:

$$\text{Max}_{T_{j,i}, F_{AS,i}, t_i} \text{ time} \quad (7)$$

$$\text{s.t. } \dot{x} = f(x, y, u, p, t) \quad x_{t=0} = x_0$$

$$0 = g(x, y, u, p, t)$$

$$C1: 25 \leq T_{j,i} \leq 40$$

$$C2: 0 \leq F_{AS,i} \leq 20$$

$$C3: 0.5 \leq t_i \leq 10$$

$$C4: T_{j,i+1} \leq T_{j,i}$$

$$C5: \sum_{i=1}^5 F_{AS,i} \times t_i = 555$$

$$C6: \text{Yield} \geq 75\%$$

$$C7: \frac{|d_b - d_c|}{d_c} \leq 1\%$$

In this scenario, the batch time is divided into 6 intervals, and the jacket temperature, antisolvent flow rate and time interval length of the first five-time intervals are regarded as decision variables to minimize the manufacturing batch time. The temperature is cooled linearly in each time interval, and the corresponding decision variable is the jacket temperature at the endpoint of each time interval.

C1 to C3 are the upper bound and lower bound of the decision variables. C4 is a linear constraint used to ensure cooling and avoid heating at any time. C5 is a nonlinear constraint that is used to force the antisolvent ratio to stay within 70%. Both C4 and C5 come from the requirement of the solubility polynomial [8]. C6 is also the nonlinear constraint, which is used to ensure a final yield over 75%. C7 is used to ensure that the difference of the product quality from fed batch is within 1% variation of the targeted quality also obtained with the continuous process. With these settings, the whole process manufacturing time is minimized.

### 3. Results and Discussion

The optimization problem is solved using a hybrid optimization method, which combines a genetic algorithm (ga function in MATLAB) and sqp (fmincon function in MATLAB). With the optimal operation profile, the manufacturing time is minimized to 28.26 minutes. In the continuous process, 5510.2 g on-spec product production is collected when start-up and shut down of MSMPR crystallizer considered. The same output can be obtained with several batches with different volumes. Assuming that the draining, cleaning and refilling of vessels will take 20 minutes, the batch capacities and manufacturing batch times are shown in table 1.

**Table 1.** Optimized batch number, Manufacturing time and batch capacity

Scenario	Manufacturing time (mins)	Volume (L)
1 batch	28.26	50
2 batches	76.51	25
4 batches	173.03	10
9 batches	414.31	5
14 batches	655.60	2.5
20 batches	945.14	2
Continuous process	800	0.2/0.5/0.5

Based on the optimized results, a short-cut evaluation of the different fed-batch alternatives and continuous process was developed. The costs, including equipment, material cost, maintenance, environmental footprint, and labour cost, were used to evaluate the overall score and rank all possible alternatives [9].

In table 2, the equipment and maintenance costs received the largest weighting factor. The score associated with the equipment and maintenance is determined by the vessel (batch) capacity and the number of vessels. For example, the continuous process consists in three MSMPR vessels. Although the total volume is only around 1.2 L, three vessels generated lower scores than the scenarios with 20 batches. Material cost and environmental footprints are largely determined by the yield, whereas the direct labour cost is inherent to the total manufacturing time. It is worth mentioning that the labour cost in a continuous process is significantly lower than the fed-batch process due the limited operator intervention. Based on the methodology outlined above, the continuous process outperformed all batch scenarios.

**Table 2.** Performance indicators of different fed-batch scenarios vs a 3-stage continuous process.

	Weighting Factor	1	2	4	9	12	20	Continuous
Equipment and Maintenance	20	0	1	2	3	5	6	4
Material	8	1	1	1	1	1	1	0
Direct labour cost	6	5	4	3	2	1	0	7
Energy	2.5	1	1	1	1	1	1	0
Environmental Footprint	2.5	0	0	0	0	0	0	1
Cleaning	6	6	5	4	3	2	1	4
Score		76.5	84.5	92.5	100.5	128.5	136.5	148.5
Rank		7	6	5	4	3	2	1

#### 4. Conclusion

Several optimization scenarios of fed batch and continuous crystallization of ASA in ethanol and water were developed and solved to establish a technoeconomic analysis for batch vs continuous. The fed-batch systems were designed to achieve the same targeted product quality, here the mean crystal size, with minimum operation time by manipulating the jacket temperature, antisolvent flow rate and by using different discretization methods. The techno-economic analysis and comparison were developed based on the batch capacity and the batch operation time to help allocated score and rank the optimized fed-batch process and optimized continuous process including its systematic start-up and shut down optimization. Based on this method the continuous process outperformed the remaining batch alternatives particularly in on the labour, material, and cleaning costs.

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