OPTIMIZED CHLORINE BULK DECAY MODELS AND A MACHINE-LEARNING-GUIDED WATER QUALITY RESPONSIVE KINETIC MODEL FOR RESIDUAL CHLORINE PREDICTION

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• *Chlorine is one* of the most commonly used *disinfectants* for water *disinfection*.

• **Bulk decay:** Due to the reaction of chlorine with the substances available in the bulk water

• *Wall Decay:* Related to the reaction of the chlorine with the pipeline walls and the biofilms and corrosion products which are attached to them

Chlorine Decay

Water Disinfection

Adding more chlorine to compensate its decay

- *If the initial chlorine dosing concentration is too low:* There may not be a residual left at the end of the distribution system to protect water against reoccurrence of any potential contamination
- *If the dosing rate is too high:* 1- Customer complaints, 2- Corrosion of the pipe network, 3- Formation of carcinogenic by-products









***** The trade-off between model complexity and performance:

- More parameters can improve accuracy, but increase complexity and overfitting risk
- > Overfitting leads to poor performance on new, unseen data
- > A higher number of parameters may not necessarily lead to better performance on new data
- > Additional parameters may fit to noise or random fluctuations, rather than underlying trends
- > More complex models may not be practical or reliable for predicting new data
- > Carefully consider the trade-off when choosing a model for a particular application



First Order Model (FOM) Parallel First Order Model (PFOM) Second Order Model (SOM) Parallel Second Order Model (PSOM)







Research Outlines

Modifying currently existing decay models from first order to parallel second order model

- Introducing a new parameter in the equations as "Chlorine Demand"
- Were assessed against their accuracy in explaining chlorine bulk decay behaviour in an attempt to correct the flaws of existing models
- Regarded as a noteworthy achievement that will add to the novelty of the current study

Predicting bulk decay coefficients based on water quality parameters through an analytical process instead of running bulk decay experiments in a laboratory environment

- To robust the predicting chlorine decay model to cover expected changes in source water, demands, or system operation over the ensuing weeks, months, or seasons
- The system assigns new values for the rates for each water sample with different water quality properties using a trained machine learning model

Implementation plan in real water distribution networks • In this proposed methodology the system automatically updates the values for decay rate coefficients based on the changes in water quality parameters in an online manner



1. Sample Preparation:



Date		Tir	ne	
	S1 S2 S3	S4	S5 S6	S 7
8/9/2020	9 am	11 am	2 pm	4pm
	(27°C)	(28°C)	(28.6°C)	(29.2°C)
22/9/2020	9 am (27.2°C)	10 am (29.9°C)	2 pm (31.2°C)	3pm (30.4°C)
13/10/2020	9 am	10 am	2 pm	3pm
	(27.0°C)	(30.3°C)	(31.3°C)	(30.6°C)
26/1/2021	9:40 am	10:20 am	Under	2 pm
	(27.5°C)	(30.0°C)	maintenance	(30.0°C)
9/2/2021	9:30 am	10:40 am	Under	2:20 pm
	(28.2°C)	(28.9°C)	maintenance	(28.9°C)



2. Water Quality Parameter Measurements

Parameter	Unit	Method/Instrument
TRC	mg/L Cl ₂	Method 867 (DPD method)
NH ₂ Cl	mg/L Cl ₂	Method 10171 (Indophenol method)
TOC	mg/L	TOC analyzer (Shimadzu TOC-L)
pH / Temperature	No unit / °C	pH meter (Horiba Scientific pH1100)
UV254	cm ⁻¹	HACH Spectrophotometer (DR6000)
Total NH ₃	mg/L NH ₃ –N	HACH Spectrophotometer (DR6000)
Free NH ₃	mg/L NH ₃ –N	HACH Spectrophotometer (DR6000)
fDOM	a.u. Ex 365 Em 480	Fluorescence Spectrophotometer (Agilent Technologies Cary Eclipse)

✤ In this study the time intervals that were selected to measure the above-mentioned water quality parameters are 1h, 2h, 4h, 8h, 12h, 24h, 48h, 72h, 96h, and 168h after collection time

3. Modified Kinetic Bulk Decay Models

Model	Original Equation	Modified Equation	Description on new parameters
First Order Model (FOM)	$Cl(t) = Cl_0 \times e^{-k \times t}$	$Cl(t) = TCD_0 \times e^{-k_d \times t} + (Cl_0 - TCD_0)$	TCD_0 : Initial Total Chlorine demand K _d : First Order decay rate associated with initial total chlorine demand
Parallel First Order Model (PFOM)	$Cl(t) = f(Cl_0, t) = Cl_0 \times x \times e^{-k_1 \times t} + Cl_0 \times (1 - x) \times e^{-k_2 \times t}$	$Cl(t) = TCD_0 \times x \times e^{k_{1d} \times t} + TCD_0 \times (1 - x)e^{k_{2d} \times t} + (Cl_0 - TCD_0)$	$ \begin{array}{llllllllllllllllllllllllllllllllllll$
Second Order Model (SOM)	$C_{CI}(t) = \frac{C_{CI_0} - C_{A_0}}{1 - \frac{C_{A_0}}{C_{CI_0}} \times e^{-(C_{CI_0} - C_{A_0}) \times k \times t}}$	$Cl(t) = \frac{TCD_0 - C_{A_0}}{1 - \frac{C_{A_0}}{TCD_0} \times e^{-(TCD_0 - C_{A_0}) \times k_d \times t}} + (Cl_0 - TCD_0)$	$K_d:$ Second order decay rate associated with initial total chlorine demand (TCD_0) and initial notional reactant (C_{A_0})
Parallel Second Order Model (PSOM)	$Cl(t) = \frac{Cl_0 Z (1 - R_1)}{1 - R_1 \times e^{-(1 - R_1) \times k_1 \times t}} + \frac{Cl_0 (1 - Z)(1 - R_2)}{1 - R_2 \times e^{-(1 - R_2) \times k_2 \times t}}$	$Cl(t) = \frac{TCD_0Z (1 - R_1)}{1 - R_1 \times e^{-(1 - R_1) \times k_{d_1} \times t}} + \frac{TCD_0 (1 - Z)(1 - R_2)}{1 - R_2 \times e^{-(1 - R_2) \times k_{d_2} \times t}} + (Cl_0 - TCD_0)$	k_{d1} : Second order fast reaction rate constant of the chlorine decay associated with $TCD_0\times Z$ and $(1-R_1)$ k_{d2} : Second order slow reaction rate constant of the chlorine decay associated with $TCD_0\times(1-Z)$ and $(1-R_2)$

11

4. Responsive Kinetic Model





This technique could increase the number of datasets from 31 to 217

Time	Total					Total	Free					
(h)	Cl ₂	NH ₂ Cl	тос	pН	uv254	NH ₃	NH ₃	fDOM	Тетр	k,	k _d	Cl _d
0	2.17	1.97	1.509	8.01	0.025	0.562	0.08	8.851	27	0.001658	0.010020	0.5622
1	2.16	2.05	1 /01	8.01	0.026	0.533	0.09	11.162	27	0.001625	0.000649	0.5605
-	2.10	2.03	1.491	0.01	0.020	0.555	0.09	11.102	27	0.001023	0.009049	0.5005
5	2.15	1.99	1.272	7.94	0.026	0.551	0.06	11.57	27	0.001638	0.010832	0.5258
9	2.14	2	1.047	7.79	0.021	0.465	0.005	9.442	27	0.001649	0.011887	0.4996
21	2.04	1.89	1.352	7.65	0.025	0.537	0.11	10.843	27	0.001310	0.007489	0.4938
45	1.98	1.81	1 308	7 57	0.011	0.515	0.11	9 214	27	0.001302	0.014377	0 3189
10	1.90	1.52	1.001	7.57	0.011	0.515	0.11	0.0.61	27	0.001102	0.025201	0.1072
69	1.9	1.73	1.021	7.41	0.016	0.515	0.11	9.061	27	0.001103	0.025391	0.1972
93	1.81	1.69	0.944	7.38	0.016	0.505	0.005	8.915	27			
165	1.72	1.44	0.854	7.29	0.015	0.512	0.005	8.114	27			



12



1. Data Visualization of Key Water Quality Parameters



- ✓ The level of total chlorine concentration in this part of distribution network is in an acceptable range recommended by many organizations such as <u>American Water Works Association (AWWA).</u>
- ✓ TOC levels lower than 2 mg/L is showing the full consistency with regulations that can reduce the formation of DBP to comply with the requirements for a safe tap water delivery
- ✓ The total residual chlorine is entirely contributed by monochloramines, and there is almost no contribution from free chlorine.
- ✓ This indicates that the entire distribution network has optimal chlorine dosage sufficient to oxidise all organic compounds whilst reacting with all free ammonia present, leaving the latter remaining to be as close to 0
- ✓ The total free ammonia concentration depletes further down the distribution network, which reinforces the fact that whatever free chlorine present (residual free chlorine) was used to react with ammonia to form monochloramines



2. Bulk Decay Experiments



The bulk decay rate was generally increasing by moving from MNSR towards Jellico Rd

The major reason of this increment in bulk decay rate coefficients can be explained by the Arrhenius theory (Equation 3-1) due to the increase in temperature by moving from MNSR towards Jellico Rd and also the reverse effect of initial chlorine on bulk decay rate as TRC is decreasing from MNSR to Jellico Rd.

 $K_{\rm T} = K_{\rm base} * e^{\frac{-\frac{E}{R}*(base-T)}{(273 + base)*(273 + T)}}$ (Equation 3-1)



Assumption: Water samples collected in the same day having the same activation coefficients

E/R can be estimated for each day by considering the lowest temperature of the collected samples as the base temperature and estimating the bulk decay rate of this sample with the lowest temperature and also another sample with different temperature.



2. Bulk Decay Experiments

- To explain the variations in activation coefficients (E/R) estimated for 5 different days, the correlation between E/R with different water quality parameters was calculated
- ✤ A parallel Component Analysis (PCA) was carried out to obtain a single variable (component) out of seven variables for each water quality parameter by which most of the data variability is explained

	TRC	NH ₂ Cl	тос	рН	UV254	TNH ₃	FNH ₃	fDOM	Temp			
		Percenta	ge of da	ta varial	vility explained by each component							
Comp1	83.86	90.36	89.33	73.42	83.52	79.48	68.25	68.00	97.89			
Comp2	13.44	6.89	7.02	23.78	10.45	16.36	16.33	21.92	2.11			
Comp3	2.44	2.36	3.14	1.58	5.60	3.81	10.49	6.14	0.00			
Comp4	0.17	0.38	0.49	1.06	0.42	0.31	4.89	3.91	0.00			
Comp5	0.08	0.00	0.01	0.16	0.00	0.03	0.05	0.03	0.00			



✓ As can be seen, there is a high correlation between activation coefficients with TRC, NH2Cl, TNH3, and temperature with correlation coefficients equal to 0.6995, 0.7883, 0.9450 and 0.7637, respectively.

0.8

0.6

0.4

0.2

-0.2

-0.4

-0.6



2. Bulk Decay Experiments

- The exponential term in the Arrhenius equation implies that the rate constant of a reaction increases exponentially when E/R decreases.
- ✓ Accordingly, it can be concluded that bulk decay coefficients are inversely proportional to TRC, NH_2Cl , TNH_3 as those water qualities have a significant positive linear correlation with E/R.
- However, the significant positive correlation between temperature and E/R is not fundamentally valid as the activation energy is not affected by temperature.
- To confirm these results, the Pearson correlation between bulk decay rate coefficients with water quality parameters were also reported:

0.8

0.6

0.4

0.2

0

-0.2

-0.4

-0.6

-0.8



- *i.* The results are consistent with the previous results
- *ii. pH also showed a significant negative correlation with bulk decay rate coefficient:* can be due to the higher concentration of mono-chloramine in the pH levels >7 which is contributing to lower reaction rates of TRC in bulk water.
- *iii. Temperature also had a significant positive linear correlation with bulk decay rate as expected.*



3. Modified bulk Decay Kinetic Models

Collection	Site			First O	rder Mod	el (FOM)			
Date			Origina	I	Modified				
		k	MSE	R	TCD ₀	k _d	MSE	R	
08.Sep.2020	MNSR1	0.0017	0.0014	0.9774	0.5622	0.0100	0.0002	0.9963	
	MNSR2	0.0028	0.0040	0.9760	0.7480	0.0124	0.0008	0.9934	
	MNSR3	0.0021	0.0022	0.9767	0.6379	0.0097	0.0010	0.9846	
	BTWW	0.0072	0.0037	0.9880	1.0662	0.0131	0.0014	0.9939	
	FCSR1	0.0132	0.0012	0.9957	1.0180	0.0168	0.0006	0.9977	
	FCSR2	0.0103	0.0015	0.9951	1.2570	0.0101	0.0014	0.9952	
	Jellico	0.0588	0.0008	0.9899	0.3055	0.0825	0.0002	0.9927	
	Rd								

Collection	Site		Parallel First Order Model (PFOM)											
Date				Origina	I		Modified							
		x	k ₁	k ₂	MSE	R	x	k _{d1}	k _{d2}	TCD ₀	MSE	R		
08.Sep.2020	MNSR1	0.2637	0.0097	0.0000	0.0002	0.9962	0.4073	0.0100	0.0000	1.3815	0.0002	0.9963		
	MNSR2	0.6369	0.0000	0.0124	0.0008	0.9934	0.5347	0.0000	0.0126	1.5997	0.0008	0.9934		
	MNSR3	0.9517	0.0015	0.1219	0.0006	0.9898	0.0719	0.1576	0.0038	1.0424	0.0006	0.9902		
	BTWW	0.7061	0.0131	0.0000	0.0014	0.9939	0.2486	0.0135	0.0129	1.0704	0.0014	0.9940		
	FCSR1	0.4257	0.0063	0.0226	0.0005	0.9979	0.5000	0.0176	0.0176	0.9973	0.0006	0.9977		
	FCSR2	0.0478	0.5253	0.0095	0.0007	0.9970	0.9880	0.0106	0.0090	1.2208	0.0015	0.9949		
	Jellico Rd	0.5000	0.0588	0.0588	0.0008	0.9899	0.4659	0.2104	0.0315	0.3225	0.0001	0.9977		

Collection	Site						Para	llel Seco	nd Orde	r Mode	I (PSOM)				
Date					Origina	al			Modified							
		Z	R_1	R ₂	K ₁	K ₂	MSE	R	TCD ₀	Z	R_1	R ₂	K _{d1}	K _{d2}	MSE	R
08.Sep.2020	MNSR1	0.3646	0.2181	0.3192	0.0105	0.0092	0.0002	0.9962	4.9147	0.5692	0.1177	0.1154	0.0101	0.0101	0.0002	0.9963
	MNSR2	0.7929	0.4006	0.4006	0.0121	0.0121	0.0008	0.9928	8.9858	0.5673	0.0863	0.0805	0.0128	0.0125	0.0008	0.9932
	MNSR3	0.5788	2.8707	0.0873	0.0011	0.1626	0.0006	0.9901	1.6058	0.7777	2.2945	0.1994	0.0013	0.1691	0.0006	0.9899
	BTWW	0.2261	0.0000	2.3667	0.0027	0.0055	0.0015	0.9933	18.220	0.5141	0.0586	0.0586	0.0133	0.0135	0.0014	0.9938
	FCSR1	0.3632	1.2680	6.6334	0.0073	0.0029	0.0005	0.9979	4.8686	0.3265	0.0975	0.2779	0.0248	0.0159	0.0005	0.9979
	FCSR2	0.0448	14.420	14.734	0.0388	0.0007	0.0008	0.9967	1.6084	0.0514	12.275	6.3691	0.0344	0.0010	0.0004	0.9982
	Jellico Rd	0.3421	1.3619	1.0100	0.1865	0.0580	0.0001	0.9981	0.3345	0.2725	1.3920	1.1259	0.2104	0.0608	0.0001	0.9981

Collection	Site				Second O	rder Mode	el (SOM)			
Date			Ori	ginal				Modified		
		C _{A0}	k	MSE	R	TCD ₀	C _{A0}	k _d	MSE	R
08.Sep.2020	MNSR1	0.6116	0.0044	0.0002	0.9962	0.6041	20.178	0.0004	0.0002	0.9960
	MNSR2	0.8260	0.0058	0.0008	0.9928	0.8004	76.527	0.0001	0.0008	0.9938
	MNSR3	0.7041	0.0046	0.0009	0.9850	0.9293	0.9371	0.0078	0.0009	0.9852
	BTWW	1.5358	0.0067	0.0015	0.9930	1.1069	76.992	0.0002	0.0014	0.9940
	FCSR1	2.0702	0.0080	0.0006	0.9978	1.0586	4.1442	0.0042	0.0005	0.9979
	FCSR2	9.8056	0.0011	0.0014	0.9948	1.6149	1.6137	0.0059	0.0015	0.9939
	Jellico Rd	0.3374	0.3168	0.0001	0.9980	0.3407	0.3393	0.3224	0.0001	0.9979



3. Modified bulk Decay Kinetic Models





- As can be seen, generally, all of the models are performing almost similar except FOM which is showing lower accuracy in fitting the chloring decay data
- □ Although FOM is very simple to use and therefore it has always been popular, it has not provided a good data fitting for various chlorine decay data and modelling applications.
- ✓ However, as can be seen, adding only one additional parameter to the original FOM equation as initial total chlorine demand (TCD₀) can considerably increase its accuracy in MFOM so that the performance of this widely used and simple model will be similar to other existing models with higher complexity.



4. Responsive Bulk Decay Kinetic Model





Fold Number	Number of	Number of	Correlation	MSE	Correlation	MSE
	data in	data in test set	coefficient	(Training)	coefficient	(Test)
	training set		(Training)		(Test)	
1	207	10	0.99982	5.91E-08	0.75361	2.80E-05
2	206	11	0.99983	5.65E-08	0.98028	5.45E-06
3	206	11	0.99982	6.06E-08	0.98242	1.50E-05
4	206	11	0.99982	5.89E-08	0.96544	9.91E-06
5	206	11	0.99978	7.02E-08	0.85615	6.70E-05
6	206	11	0.99983	5.32E-08	0.96840	2.02E-05
7	206	11	0.99983	5.86E-08	0.59104	2.79E-05
8	206	11	0.99981	6.01E-08	0.87296	8.93E-05
9	206	11	0.99983	5.65E-08	0.97362	3.90E-06
10	206	11	0.99983	5.84E-08	0.90646	1.34E-05
11	206	11	0.99985	5.15E-08	0.99063	3.58E-06
12	206	11	0.99986	4.93E-08	0.98703	4.08E-06
13	206	11	0.99983	5.64E-08	0.95560	2.78E-06
14	206	11	0.99980	6.41E-08	0.96299	2.47E-05
15	206	11	0.99980	6.31E-08	0.83063	7.68E-05
16	206	11	0.99977	7.04E-08	0.74933	1.36E-04
17	206	11	0.99983	5.37E-08	0.97595	1.55E-05
18	206	11	0.99983	5.65E-08	0.99002	1.41E-06
19	207	10	0.99981	5.85E-08	0.94507	3.13E-05
20	207	10	0.97390	7.45E-06	0.66907	1.71E-04
Average	206	11	0.998524	4.28E-07	0.895335	3.74E-05



Bulk Decay Rate (Measured) 0.03 Bulk Decay Rate (Measure **3. Modified bulk Decay Kinetic Models** Bulk Decay Rate (Predicted) MSE (before or m) = 1.4144e-06 Bulk Decay Rate (Predicted) Bulk Decay Rate (Predicted-Opt MSE (before optimization) = 5.7072e-07 Bulk Decay Rate (MSE (after o = 1.2512e-06 - 5 6478-06 0.025 (a) **(a)** 1H) 0.05 ଞ୍ଚଁ 0.02 9 0.04 ŏ _{0.015} å 0.03 Bulk 0.01 D 0 02 0.005 **Test Set** FOM **Predicted-FOM Optimized-Predicted-FOM** 250 Record Numbe 200 0.03 R (before optimization) = 0.99002 Data MAE MAE R R R MAE R (before optimization) = 0.99983 Data Fitted curve (before optimization R (after optimization) = 0.99126 Fitted curve R (after optimization) = 0.99838 Data 0.025 Data Fitted curve (after opti 0.05 Fitted 0.9587 0.9588 0.9783 0.0316 0.0342 0.0346 **(b)** а **(b)** 0.02 0.04 0.9910 0.9754 0.0427 b 0.0380 0.0568 0.9761 B 0.015 Predict 0.9729 0.0350 0.9597 0.1352 0.9560 0.0684 с 0.01 0.02 d 0.9550 0.0269 0.9885 0.0280 0.9885 0.0278 0.005 0.01 e 0.9989 0.0147 0.9707 0.0268 0.9702 0.0203 0.005 0.01 0.015 0.02 0.025 0.01 0.02 0.03 0.04 0.05 0.06 Measure 0.0588 0.9591 0.0354 0.9873 0.9874 0.0521 (d) **(b)** (c) **(a)** (T) 1.8)ĝ 0.9831 0.0192 0.9518 0.0330 0.9518 0.0235 σ ⊑) 01.5 21.5 02 1.6 ည္က 1.6 TRC 0.0509 h 0.9945 0.0238 0.9800 0.9797 0.0310 14 50 100 150 200 50 100 150 200 50 100 150 200 50 100 150 200 0 0 0 0 Time (h) Time (h) Time (h) Time (h) 0.9196 0.0262 0.9906 0.0304 0.9905 0.0296 (g) (h) **(f) (e)** <u>__</u> 1. (T) 1.8 (m) (mg/L) (T)Bui b 1.8 0.9837 0.0021 0.9970 0.1320 0.9973 0.1106 ບິກ 1.6 Q 0.5 Q 0.5 <u>2</u> 1.7 0.9639 0.0063 0.9694 0.1334 0.0849 k 0.9667 50 100 150 200 50 100 150 200 50 100 150 200 50 100 150 0 0 0 0 Time (h) Time (h) Time (h) Time (h) 0.9727 0.0236 0.9754 0.0654 0.9748 0.0478 Average (i) (j) (k) Observed () 1.6 () 1.5 () 1.5 - First Order Model (mg/L) Predicted-FO Optimized-Predicted-FO 0.5 22 22 1.4 요 1.4 20

1.3

ŏ

50

Time (h)

150

100

Time (h)

1.2

0

50

Time (h)

100

100

Test Set



4. Implementation in Real Water Distribution Networks



$$K_{b1}(n+1) = \frac{\sum_{i=1}^{n} Qi * Kb1i}{\sum_{i=1}^{n} Qi} \qquad Clo (n+1) = \sum_{i=1}^{n} Cli \left(\frac{Li}{Vi}\right)$$

$$K_{b2}(n+1) = \frac{\sum_{i=1}^{n} Qi * Kb2i}{\sum_{i=1}^{n} Qi} \qquad NOM_{10} (n+1) = \sum_{i=1}^{n} NOM_{10} i \left(\frac{Li}{Vi}\right)$$

$$NOM_{20} (n+1) = \sum_{i=1}^{n} NOM_{20} i \left(\frac{Li}{Vi}\right)$$

$$K1 (n+1) = \frac{\sum_{i=1}^{n} Qi * K1i}{\sum_{i=1}^{n} Qi}$$

$$K2 (n+1) = \frac{\sum_{i=1}^{n} Qi * K2i}{\sum_{i=1}^{n} Qi}$$

> $\frac{Li}{Vi}$ is a time duration that water segment (i) travels it's corresponding pipeline length until the junction.

In this proposed methodology the system automatically updates the values for the parameters in kinetic model based on the changes in water quality





All water quality parameters in the studied portion of distribution network were in an optimal range to maintain safe and highquality water and preserving drinking water quality from the point-of-entry to the point-of-use



Bulk decay coefficients were inversely proportional to TRC, NH₂Cl, TNH₃, pH and directly proportional to Temperature



By applying the proposed modification in this study on all four nominated models, the MSE values were decreased by 38.03%, 28.02%, 23.11%, and 33.29% for FOM, PFOM, SOM and PSOM, respectively.



A new methodology is used in this study to predict bulk decay coefficients based on water quality parameters through an analytical process instead of running bulk decay experiments in a laboratory environment.



Robust Prediction of Disinfectant Degradation in Drinking Water Distribution Systems Integrating Water Quality Sensing and Digital Twin Technologies





