

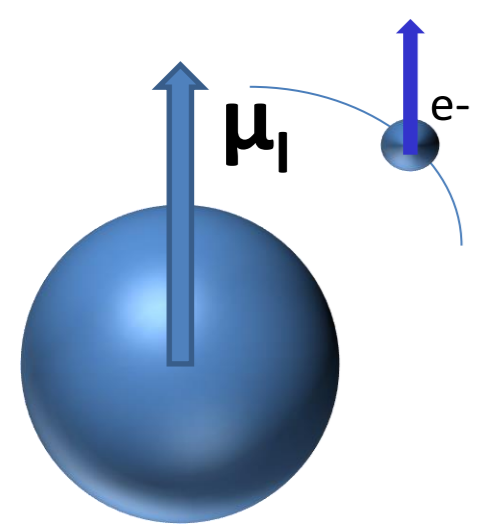
## Nuclear magnetization distribution effect in molecules and atoms

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### INTRODUCTION & AIM

Hyperfine structure and the nuclear magnetization distribution effect in molecules and atoms



$$\Delta E_{HFS} \sim \mathbf{I} \cdot \mathbf{A} \cdot \mathbf{S}$$

$$A = A^{(0)} - A^{BW}$$

$$\Delta E = \Delta E_0 - \Delta E_{BW}$$

HFS within the point magnetic dipole approximation

Contribution from finite nuclear magnetization distribution: Bohr – Weisskopf effect (BW)

Why do we need HFS?

- ✓ Probe the accuracy of calculated atomic and molecular constants characterizing symmetry-violating effects in searches for New physics

$$\text{electron EDM} = \frac{\Delta E}{\mathcal{E}_{\text{eff}}}$$

- ✓ Probe of bound-state QED methods

- ✓ Study of the nuclear structure: valence nucleon configuration, nuclear many-body effects, etc.

### METHOD

Hyperfine interaction in the point magnetic dipole approximation:

$$H_{HFI} = \boldsymbol{\mu} \cdot \frac{[\mathbf{r} \times \boldsymbol{\alpha}]}{r^3} \quad \longrightarrow \quad A^{(0)} = \frac{\mu}{I\Omega} \left\langle \Psi_{\Omega} \left| \frac{[\mathbf{r} \times \boldsymbol{\alpha}]_z}{r^3} \right| \Psi_{\Omega} \right\rangle$$

Hyperfine interaction with finite nuclear magnetization distribution:

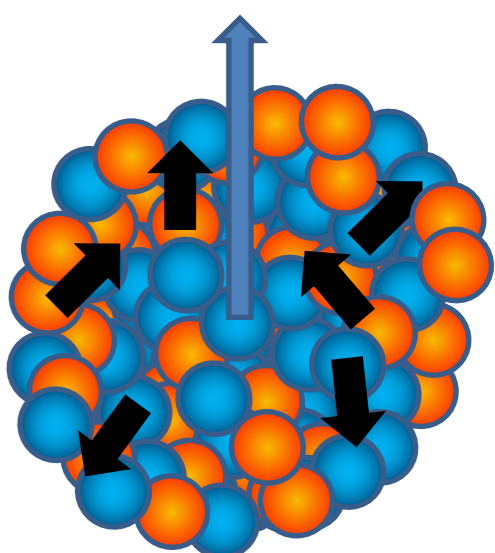
$$H_{HFI} = \boldsymbol{\mu} \mathbf{F}(\mathbf{r}) \cdot \frac{[\mathbf{r} \times \boldsymbol{\alpha}]}{r^3} \quad \longrightarrow \quad A = A^{(0)} - A^{BW}$$

$$A^{(BW)} = \frac{\mu}{I\Omega} \left\langle \Psi_{\Omega} \left| \frac{[\mathbf{r} \times \boldsymbol{\alpha}]_z}{r^3} (1 - F(\mathbf{r})) \right| \Psi_{\Omega} \right\rangle$$

➤  $F(\mathbf{r})$  is the nuclear magnetization distribution function.

➤  $1 - F(\mathbf{r})$  is localized inside the nucleus

➤ We do not know  $F(\mathbf{r})$  accurately, but this is not important!



Factorization of the BW effect contribution to the hyperfine structure constant [1]:

$$A^{BW} = \frac{\mu}{I\Omega} (\mathcal{P}_s + \beta \mathcal{P}_p) B_s$$

Pure electronic part      Universal nuclear-model-dependent parameter for a given heavy element

$$B_s = \frac{1}{2\mu} A_{BW}(\text{H-like ion})$$

The BW effect  $A^{BW}$  can be factorized into purely electronic and nuclear-dependent parts  $B_s$  due to [1]:

- 1.) only  $s_{1/2}$  and  $p_{1/2}$  states contribute to the BW effect.
- 2.) all  $ns_{1/2}$ -type functions are proportional to the  $1s_{1/2}$  H function within the nucleus; all  $np_{1/2}$ -type functions are proportional to the  $2p_{1/2}$  H function within the nucleus.
- 3.) Special symmetry properties of the hyperfine interaction operator  $A^{BW}(2p_{1/2}) \sim A^{BW}(1s_{1/2})$ .

### RESULTS & DISCUSSION

I. We combine electronic-structure coupled-cluster theory (CCSDT(Q)) with experiment to extract the  $B_s$  parameter (the BW effect for H-like  $^{225}\text{Ra}$ ) [1]

$$A^{BW} = A_{theory}^{(0)} - A(\text{Ra}^+)_{exp}$$

$$B_s(^{225}\text{Ra}) [F(\mathbf{r}) \text{ for } ^{225}\text{Ra}]$$

TABLE II. BW contributions  $A^{BW}$ ,  $A^{BW,s}$ , and  $A^{BW,p}$  and the final values of the hyperfine structure constants (in MHz) for the ground and excited states of the  $^{225}\text{Ra}^+$  cation. For the ground state,  $A^{BW}$  has been obtained as a difference between the theoretical value of the HFS constant calculated in the point magnetic dipole approximation and the experimental value taking into account QED and Breit effects.

	$7s \ ^2S_{1/2}$	$7p \ ^2P_{1/2}$	$7p \ ^2P_{3/2}$
$-A^{BW,s}$	1214	−5	3
$-A^{BW,p}$	1	80	0
$-A^{BW}$	1215	75	2
$A^{(0)}$ (see Table I)	−29012	−5526	−463
Breit+QED, <sup>a</sup> Ref. 3	66(23)	−11(1)	−1(1)
Final	−27731	−5451	−461
Experiment <sup>85–87</sup>	−27731(13)	−5446.0(7)	−466.4(4.6)

<sup>a</sup>Extracted from Ref. 3: Breit: −93 MHz; QED: 159(23) MHz; Electron+Breit: −29113 MHz.

II. We predict the hyperfine structure constant for the RaF molecule without and with the finite nuclear magnetization distribution effect, using a universal  $B_s$  parameter and highly accurate CC methods [1]

TABLE III. Hyperfine structure constants  $A_{||}$  and  $A_{\perp}$  (in MHz) for the ground  $X^2\Sigma_{1/2}$  and excited  $A^2\Pi_{1/2}$  states of the  $^{225}\text{RaF}$  molecule induced by the  $^{225}\text{Ra}$  nucleus.

Method	$X^2\Sigma_{1/2}$		$A^2\Pi_{1/2}$	
	$A_{  }$	$A_{\perp}$	$A_{  }$	$A_{\perp}$
$-A_{  }^{BW} / \perp$	730	720 <sup>a</sup>	44	26 <sup>a</sup>
Final	−17049	−16403	−2852	−2204

III. Observation of the nuclear magnetization distribution in a molecule: the first highly accurate measurement by the CRIS collaboration [2] in a molecule containing an unstable nucleus

	Theory [1], no BW, MHz	Theory [1], with BW, MHz	Experiment 2025 [2], MHz
$A_{  }(^{225}\text{RaF})$	−17780	−17049(170)	−17064(62)
$A_{\text{perp}}(^{225}\text{RaF})$	−17123	−16403(164)	−16324(25)

### CONCLUSION

- ✓ Molecules can be used to probe the distribution of nuclear magnetization.
- ✓ The excellent agreement between theory and experiment validates the molecular parameter values characterizing T,P-odd violation effects ( $E_{\text{eff}}$ ,  $W_S$ ,  $W_{T,P}$ ,  $W_A$ ), which will be used in a future RaF experiment to probe New physics beyond the Standard model.

### REFERENCES

- [1] L.V. Skripnikov, J. Chem. Phys. **153**, 114114 (2020)
- [2] S.G. Wilkins et al, Science, **390**, 386 (2025)