

## Mathematical Modeling of Epidemic Spread with Vaccination and Awareness: A Reaction–Diffusion Approach

Amina Bessam, Said Kouachi

Department of Mathematics, College of Science and Technology, Khenchela University, Algeria

### INTRODUCTION & AIM

### RESULTS & DISCUSSION

- **Epidemic Modeling:** Mathematical models are essential tools for understanding the complex dynamics of infectious diseases and evaluating control strategies.
- **Intervention Impact:** Vaccination and individual awareness are critical factors in reducing transmission rates and managing outbreaks.
- **Proposed Model:** A reaction–diffusion PDE system is developed to investigate the spatial spread of diseases, incorporating two levels of awareness and a saturated treatment approach.
- **Research Focus:** This work analyzes how spatial diffusion influences Turing pattern formation and the long-term persistence of the disease.
- **Validation:** Extensive numerical simulations are performed to validate the theoretical stability results and illustrate the emergence of spatial structures.

- Theoretical analysis shows that the disease-free equilibrium is stable for  $R_0 < 1$ .
- Numerical simulations validate the analytical results.
- Diffusion induces spatial heterogeneity and pattern formation.
- Vaccination and awareness play a crucial role in reducing the transmission of infectious diseases.
- Turing instability may generate complex spatial epidemic patterns.

### METHOD

We propose a reaction–diffusion epidemic model incorporating vaccination and dual awareness dynamics.

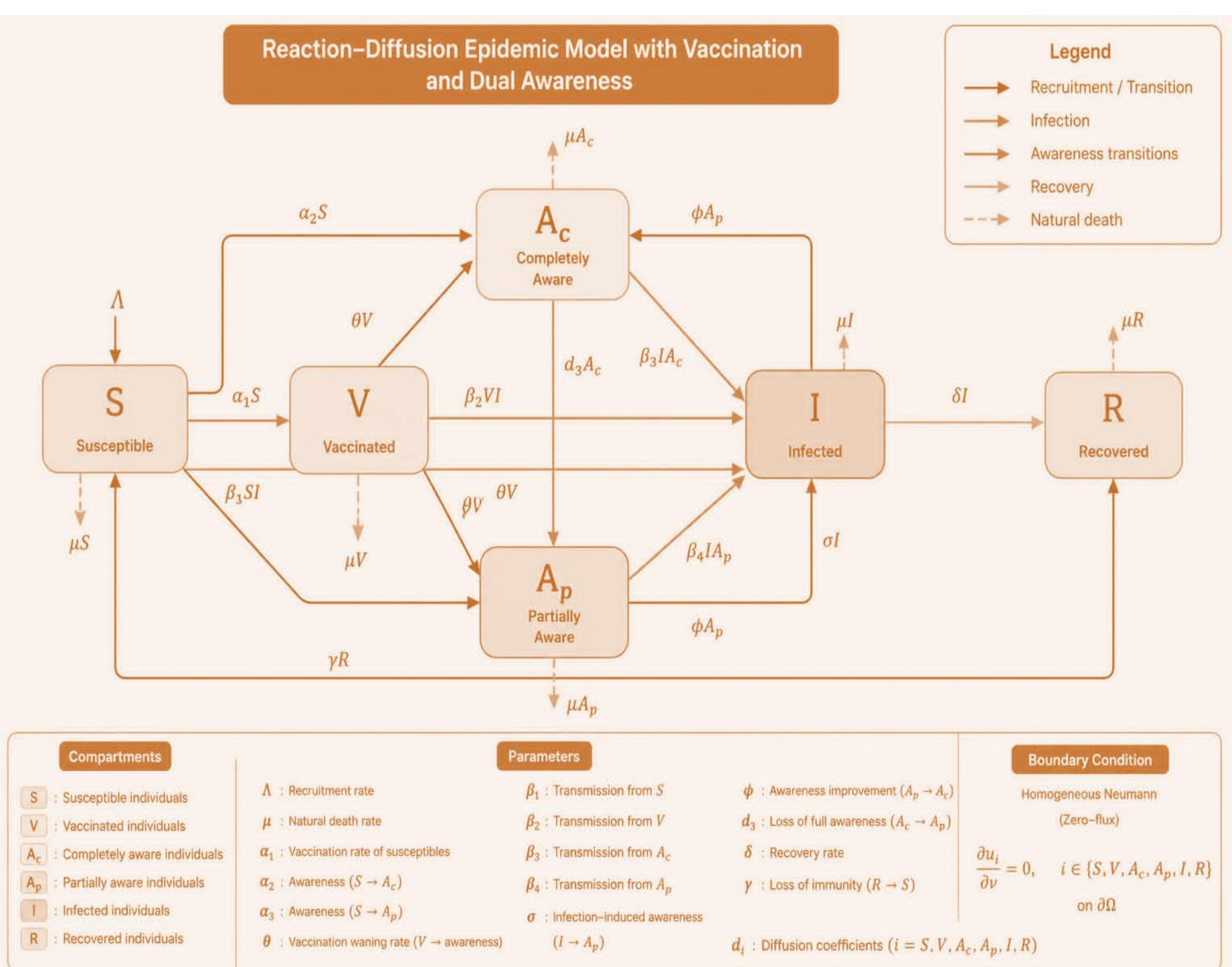


Figure 1: Schematic diagram of the proposed epidemic model

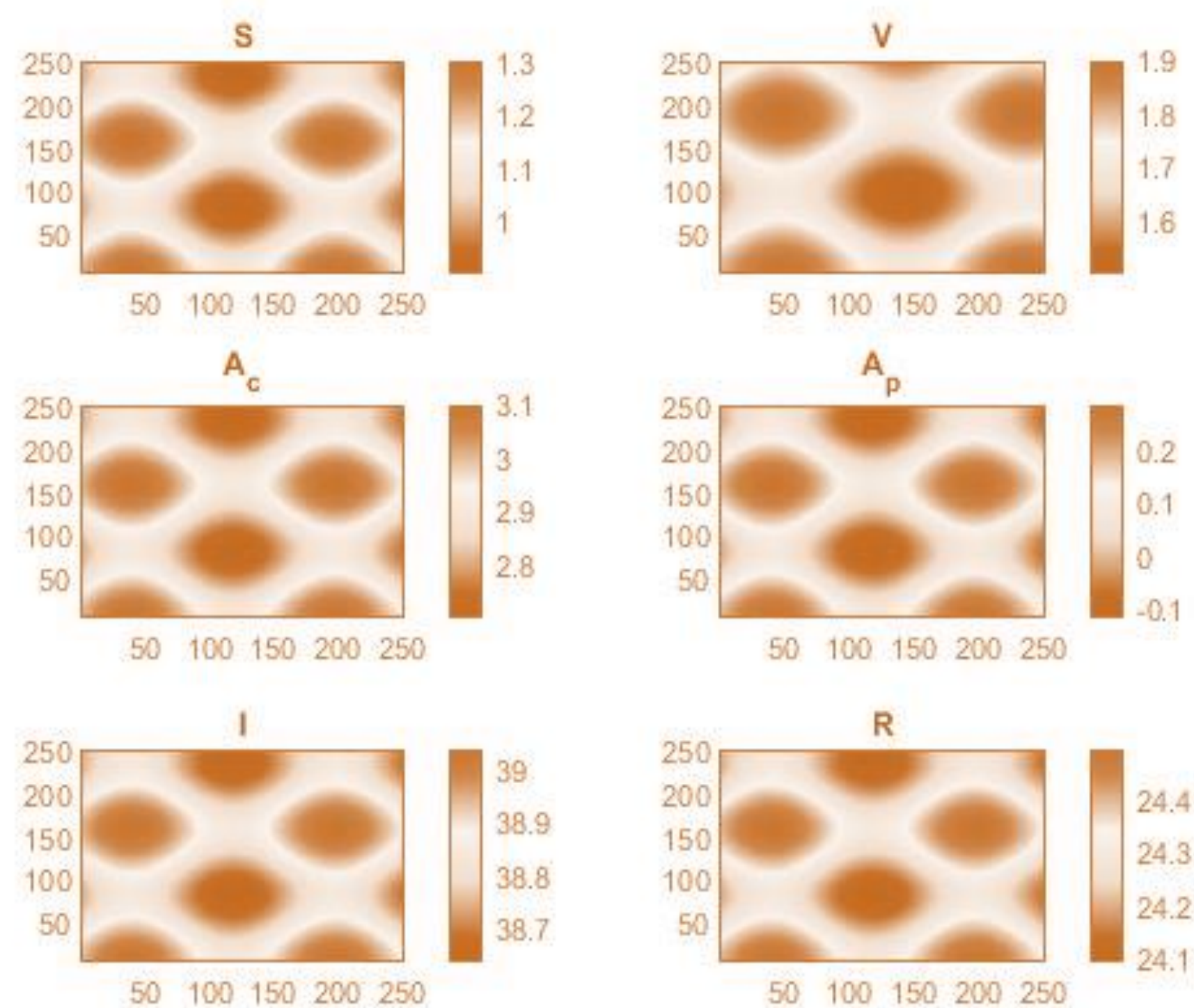


Figure 2: Spatial Turing patterns for the compartments

### CONCLUSION

Vaccination and awareness help control disease transmission, while diffusion effects may induce spatial epidemic patterns.

### FUTURE WORK / REFERENCES

Future work includes optimal control analysis and extensions of fractional-order reaction–diffusion models.