

ECEA
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18–30 November 2019

Chaired by Prof. Geert Verdoolaege

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Multispecies Emergence of **Collective Behavior:** Microbiome **Connectome, Diversity and Services**

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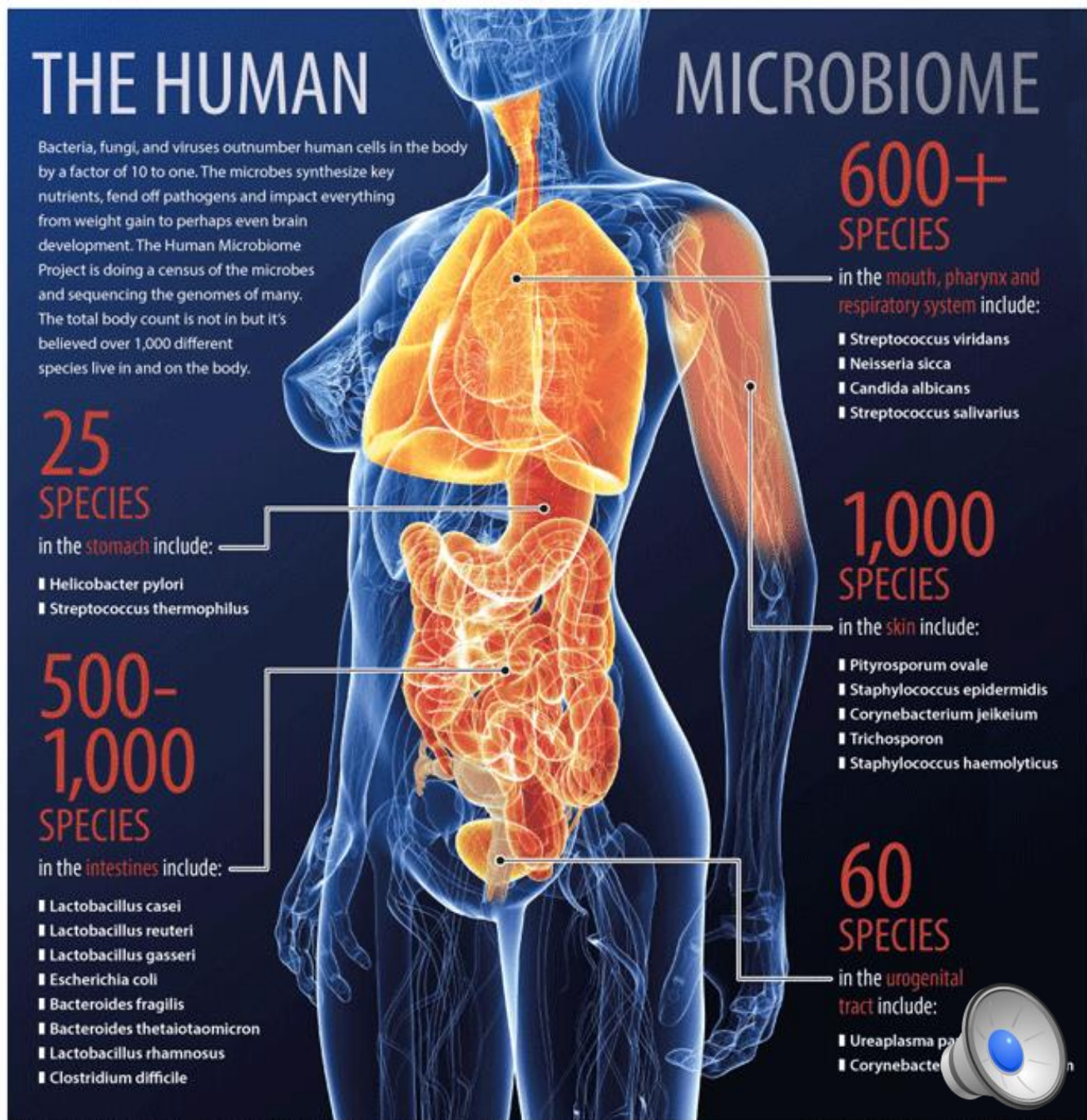
PI Nexus Group

IST Graduate School

Hokkaido University, Sapporo, JP



Microbiome Diversity (1.5 kg of Bacteria!): Unknown Connectome with the Environment & Health Outcomes -> an Entropic Challenge 😊



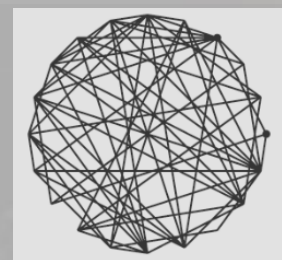
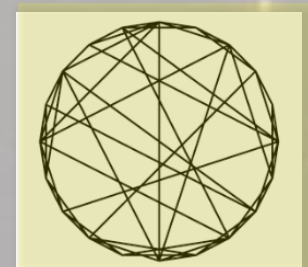
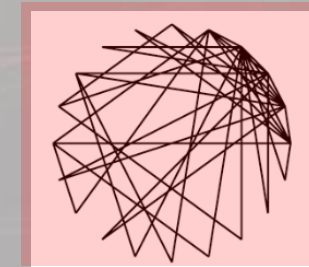
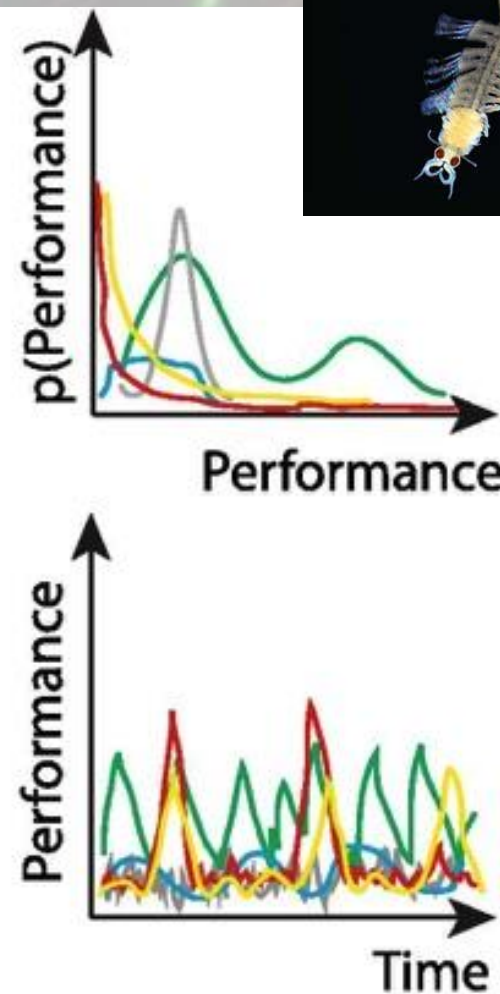
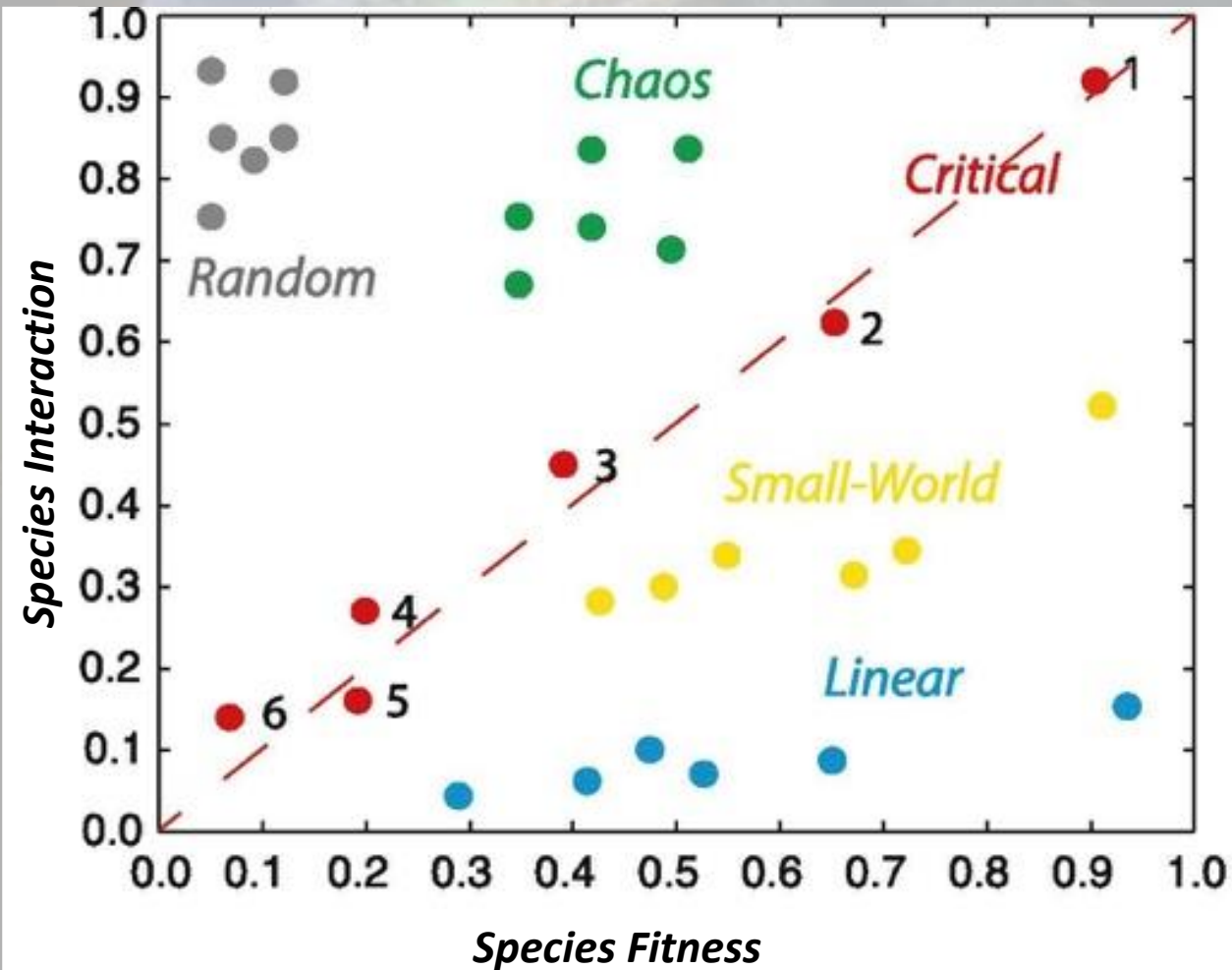


*or better... the Holobiont
(Humans & the Environment)...
a much bigger Entropic Challenge 😊!*

*the **best symbiosis** is determined
by an **optimal cooperation** that
maximizes biodiversity growth!*



"Health" Imprinted into the Dynamics of Complex Systems



3 Pillars

Collective Information -> *OTE* as a measure of *node importance* for *Topology Transitions* ~ *Metabolic Rate*
(*Kleiber's Law* connected top *Zipf's* and *Taylor's Law*)

Highly Interactive/Critical Nodes (high *OTE* and low *k*) are *The Least Abundant*; those promote *State Transitions & Evolution*

Network Topology -> *Extreme "Positive" Interactions* (*Cooperative Bio-sensu* <-> *weakly Predictable*), caused by *External Multiplicative Noise* affecting *Microbiome Functional Network (SF/SW)* -> *Lead to Unstable Multimodal Dysbiotic States* (*Karenina principle*) with *Random Networks*

Diversity -> *Healthy States* correspond to *Max Diversity Growth*
(*Principle of Optimal Heap's Evolution and Innovation Dec*)



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Article Menu

Open Access Article

Optimal Microbiome Networks: Macroecology and Criticality

by Jie Li^{1,2} and Matteo Convertino^{1,2,*}

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* Author to whom correspondence should be addressed: **RESEARCH ARTICLE** NETWORK SCIENCE

Entropy 2019, 21(5), 506; <https://doi.org/10.3390>

Optimal information networks: Application for data-driven integrated health in populations

Joseph L. Servadio¹ and Matteo Convertino^{2,3,4,*}

+ See all authors and affiliations

Science Advances 02 Feb 2018:
Vol. 4, no. 2, e1701088
DOI: 10.1126/sciadv.1701088

Environmental Modelling & Software
Volume 51, January 2014, Pages 296-309

Untangling drivers of species distributions: Global sensitivity and uncertainty analyses of MAXENT

M. Convertino^{a,b,c,d,e}, R. Muñoz-Carpena^d, M.L. Chu-Agor^e, G.A. Kiker^d, I. Linkov^{f,g}

Ecological Indicators
Volume 107, December 2019, 105510

Original Articles

Toward a pluralistic conception of resilience

Matteo Convertino^{a,b}, L. James Valverde Jr.^c

Taming Network Inference: Optimal Transfer Entropy Model

Jie Li^a, Matteo Convertino^{a,b*}

Macroecology, Epigenetic Landscape, and Phase Transitions in the Gut Microbiome

M Convertino^{a,b*}, J Li^a

Regular Article | Free Access

On neutral metacommunity patterns of river basins at different scales of aggregation

Matteo Convertino, Rachata Muneeppeerakul, Sandro Azaele, Enrico Bertuzzo, Andrea Rinaldo, Ignacio Rodriguez-Iturbe

First published: 15 August 2009 | <https://doi.org/10.1029/2009WR007799> | Cited by: 11

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Health and Disease Imprinted in the Time Variability of the Human Microbiome

Jose Manuel Marti, Daniel Martinez-Martinez, Teresa Rubio, César Gracia, Manuel Peña, Amparo Latorre, Andrés Moya, Carlos P. Garay Jack A. Gilbert, Editor

DOI: 10.1126/mSystems.00144-16 Check for updates

Cooperation, competition and the emergence of criticality in communities of adaptive systems

Jorge Hidalgo^{1,2}, Jacopo Grilli^{2,3}, Samir Suweis², Amos Maritan² and Miguel A Muñoz¹

Published 17 March 2016 • © 2016 IOP Publishing Ltd and SISSA Medialab srl

[Journal of Statistical Mechanics: Theory and Experiment, Volume 2016, March 2016](#)

Open Access

Neutral Theory and Scale-Free Neural Dynamics

Matteo Martinello, Jorge Hidalgo, Amos Maritan, Serena di Santo, Dietmar Plenz, and Miguel A. Muñoz
Phys. Rev. X 7, 041071 – Published 26 December 2017

Stochastic models of evolution in genetics, ecology and linguistics

R A Blythe¹ and A J McKane²

Published 23 July 2007 • IOP Publishing Ltd

[Journal of Statistical Mechanics: Theory and Experiment, Volume 2007, July 2007](#)



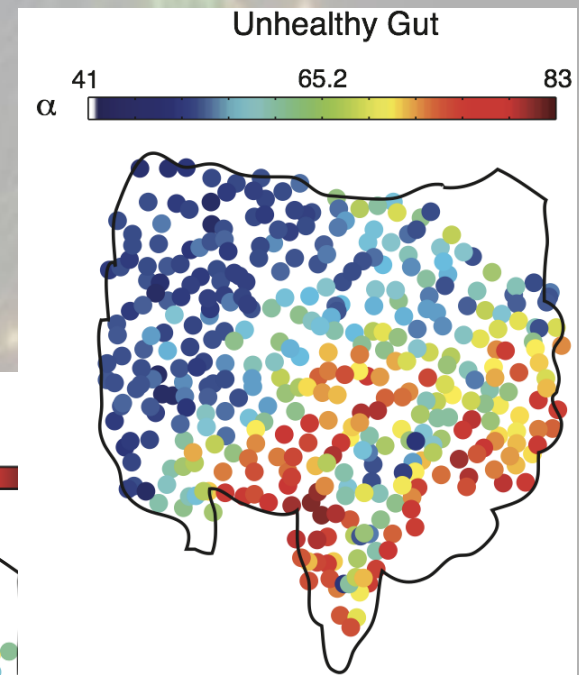
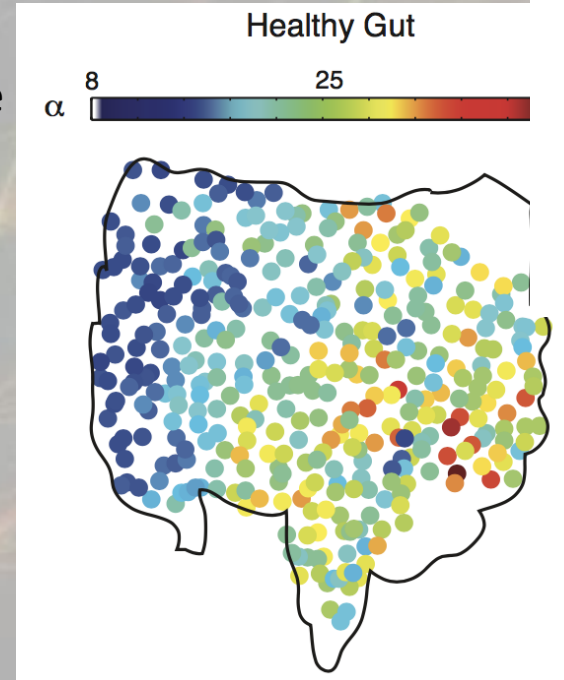
Inflammatory bowel disease (IBD)

Inflammatory bowel disease (IBD) is an **umbrella term** used to describe disorders that involve **chronic inflammation of your digestive tract**.

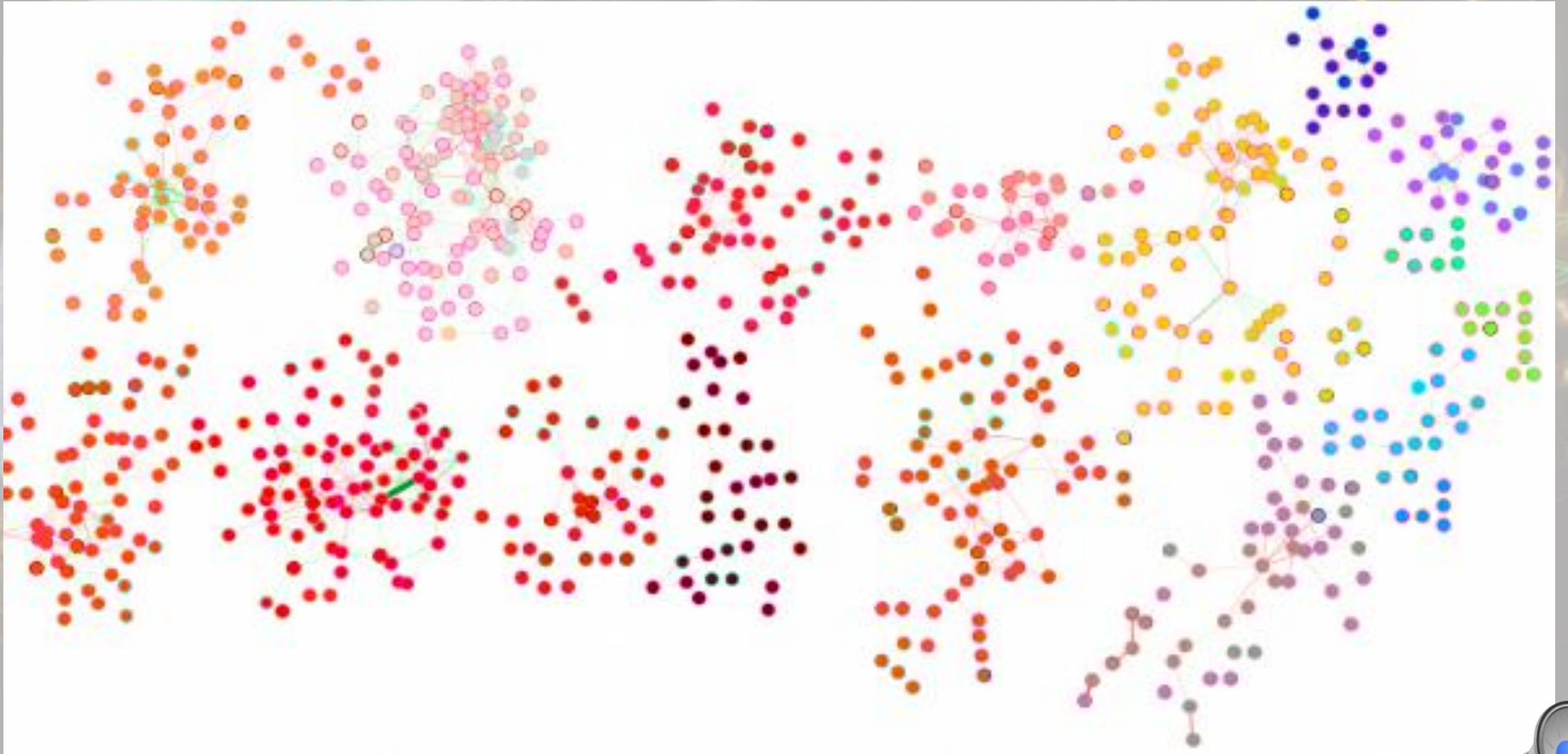
Symptoms:

- Diarrhea
- Fever and fatigue
- Abdominal pain and cramping
- Blood in your stool
- Reduced appetite
- Unintended weight loss

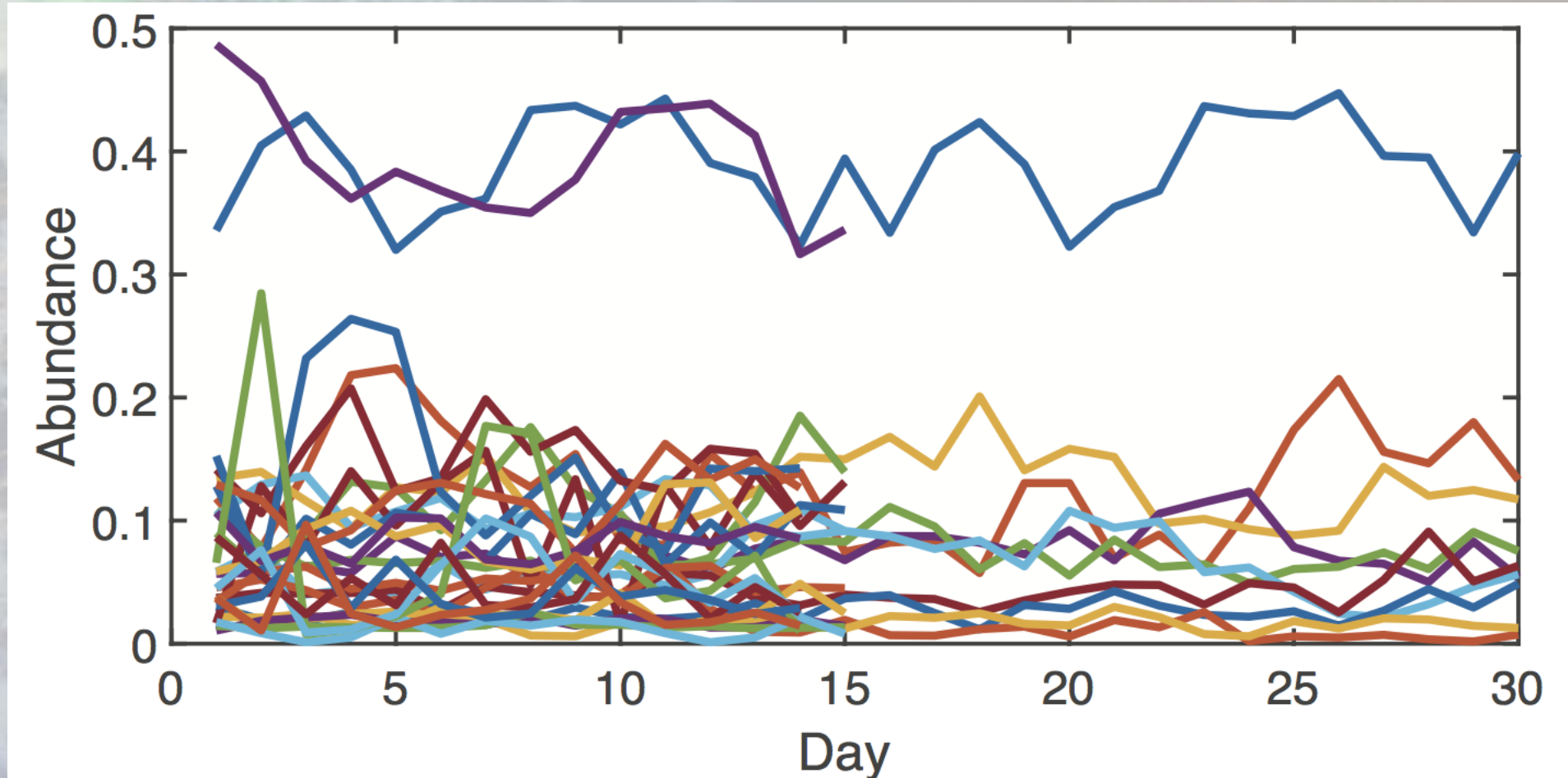
The **“exact cause”** of inflammatory bowel disease remains **unknown**. One possible “cause” is an **immune system malfunction**. When your immune system tries to fight off an invading virus or bacterium, *an abnormal immune response causes the immune system to attack the cells in the digestive tract*, too. However, the origin of this abnormal immune response is a *complex network of environmental factors...*



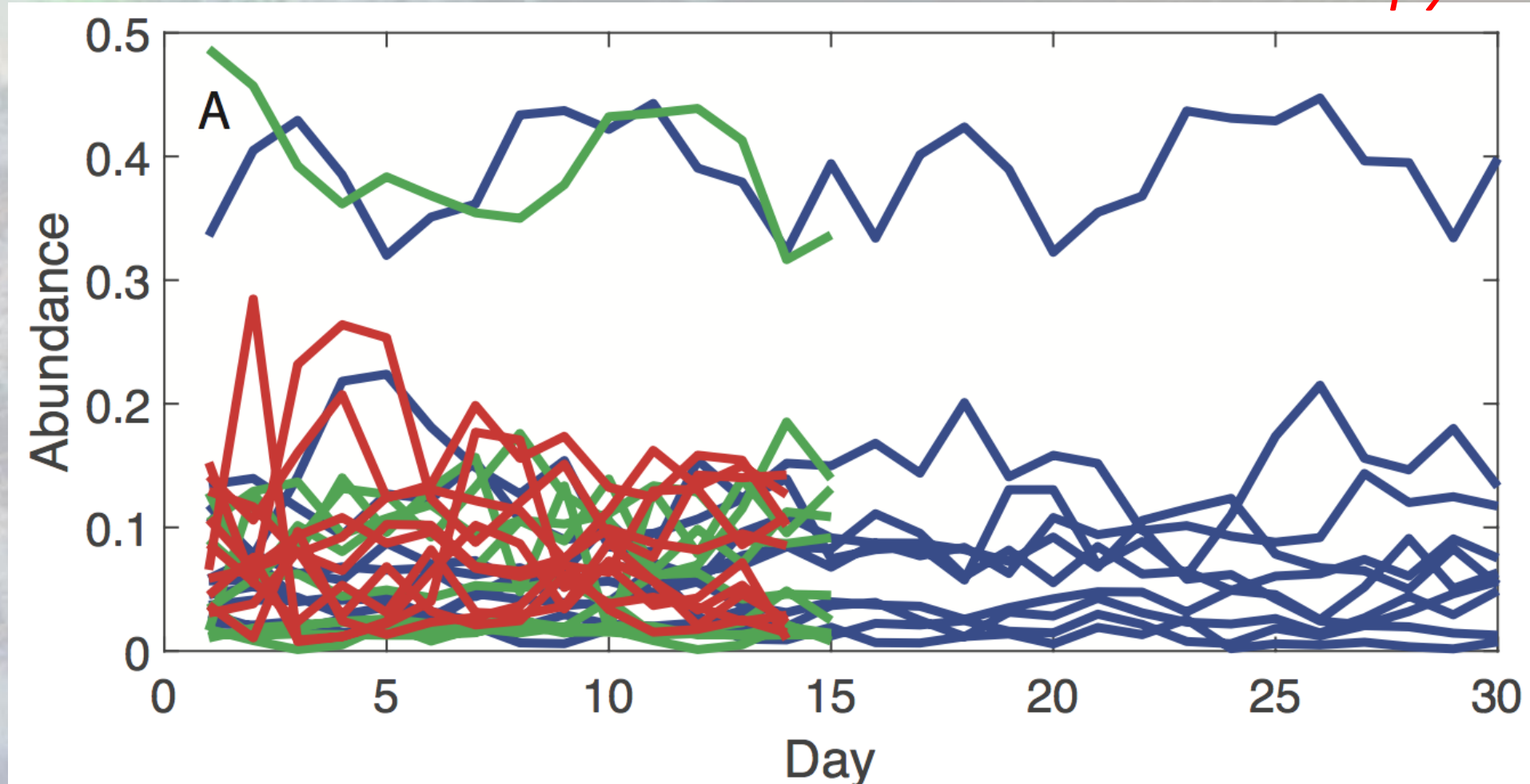
Old Statistical Approach does lead to poor Pattern Detection...

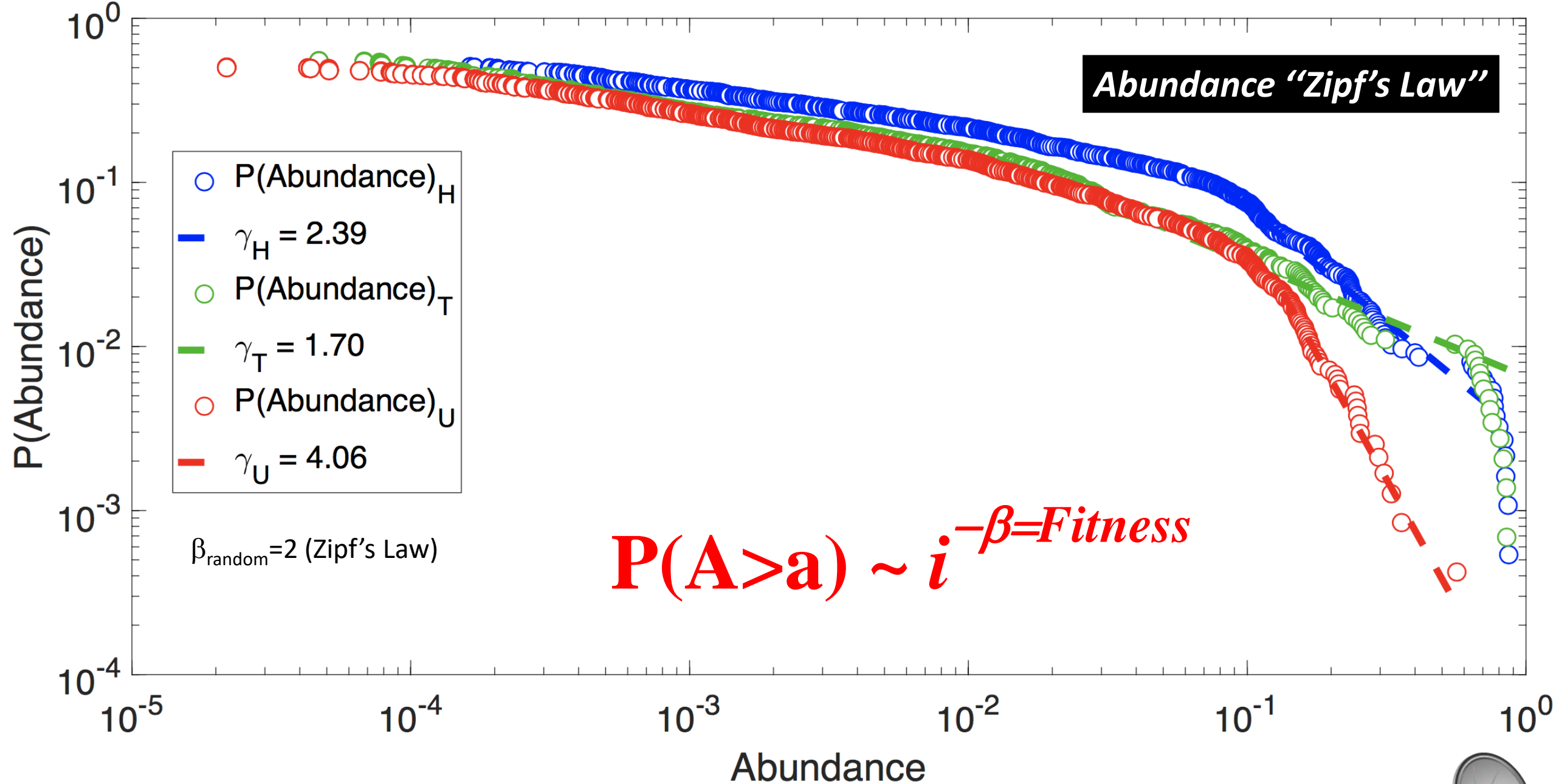


Species "Speech": basic Information



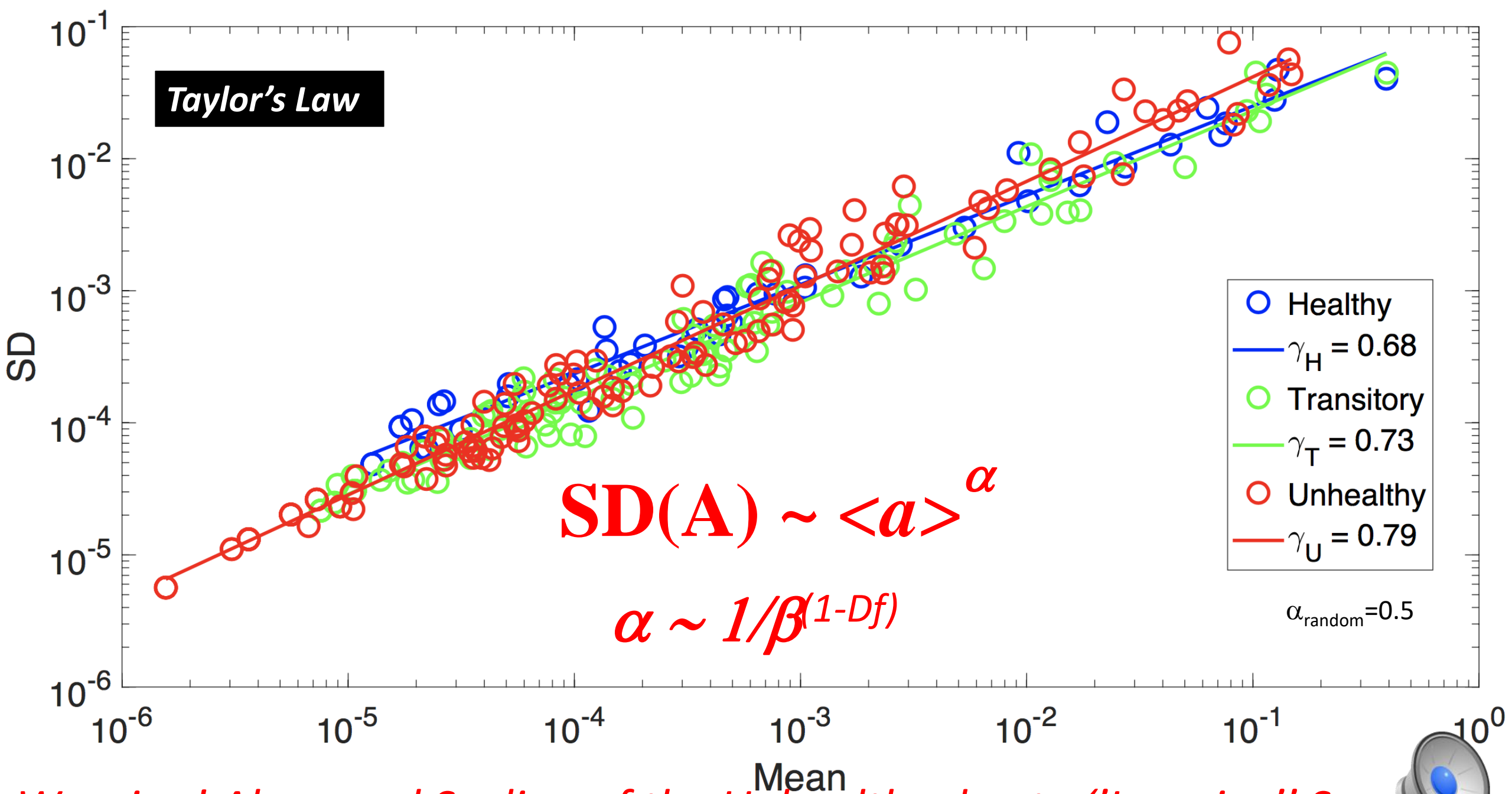
Species "Speech": clustering based on pdf of species abundance -> Entropy clustering





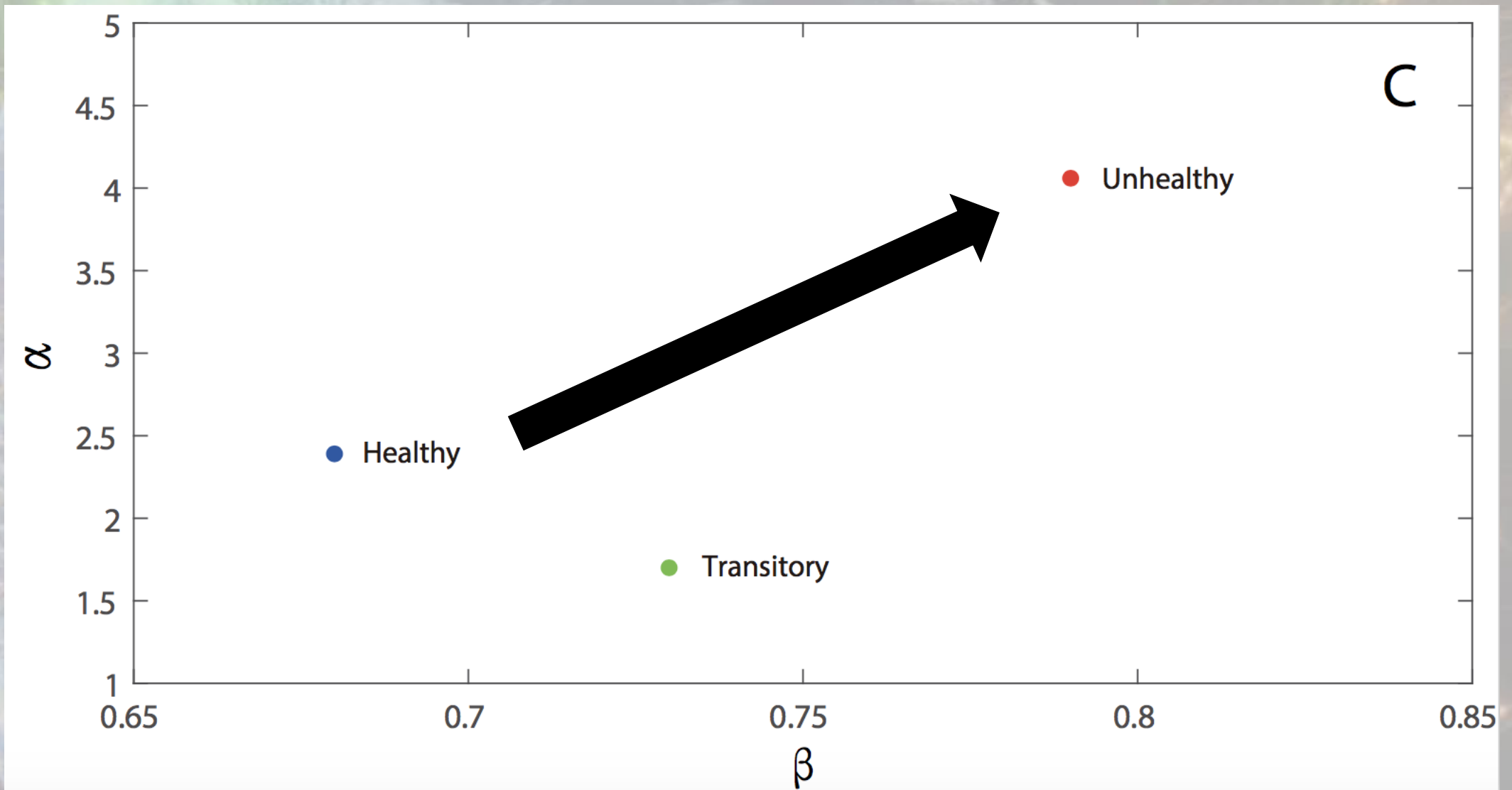
Population Patterns as Fingerprint of Species Network Topology





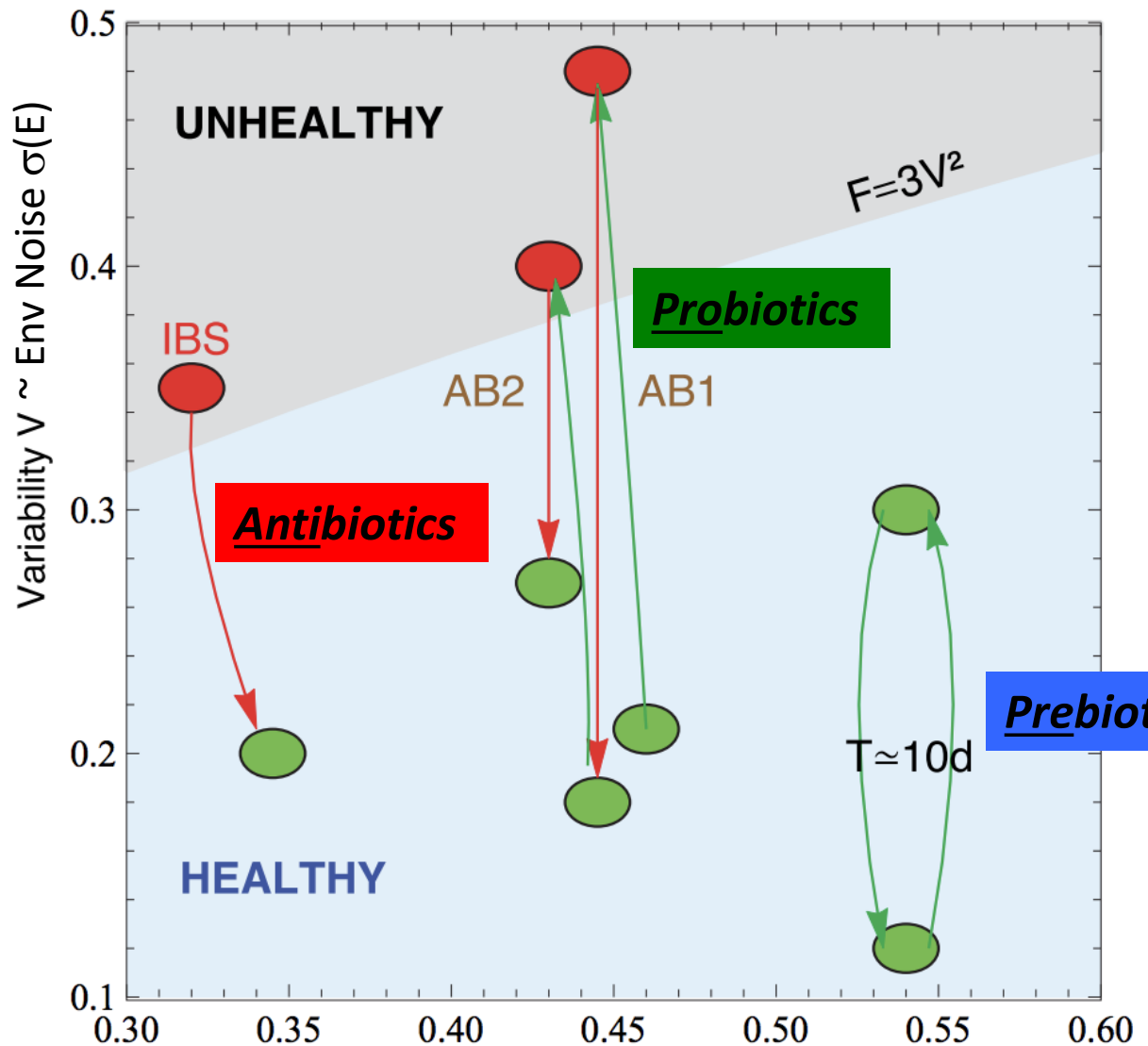
Warning! Abnormal Scaling of the Unhealthy due to "Invasive" Species





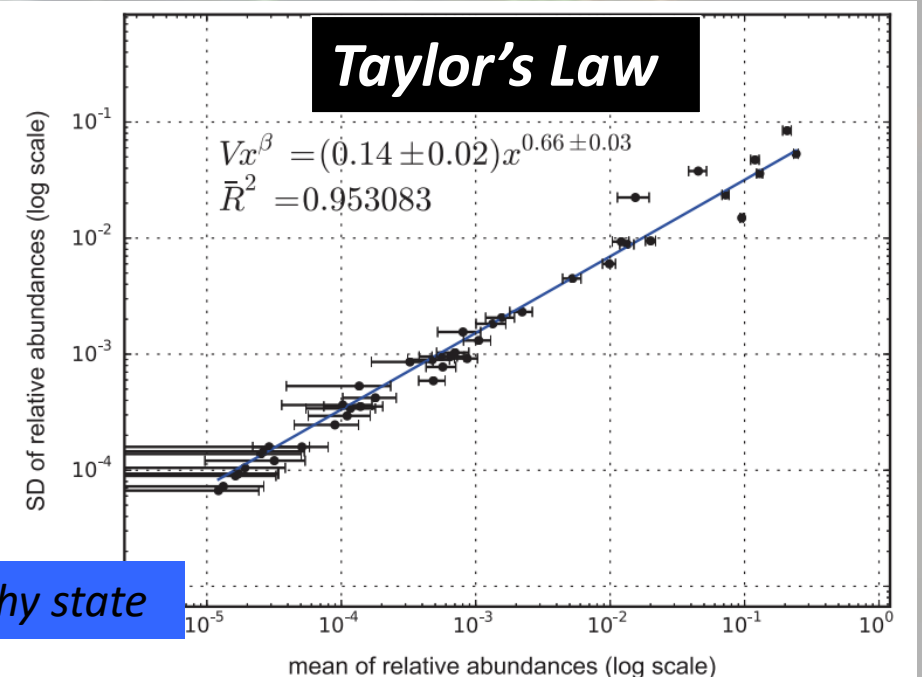
Taylor's – Zipf's Macroecological State Indicators



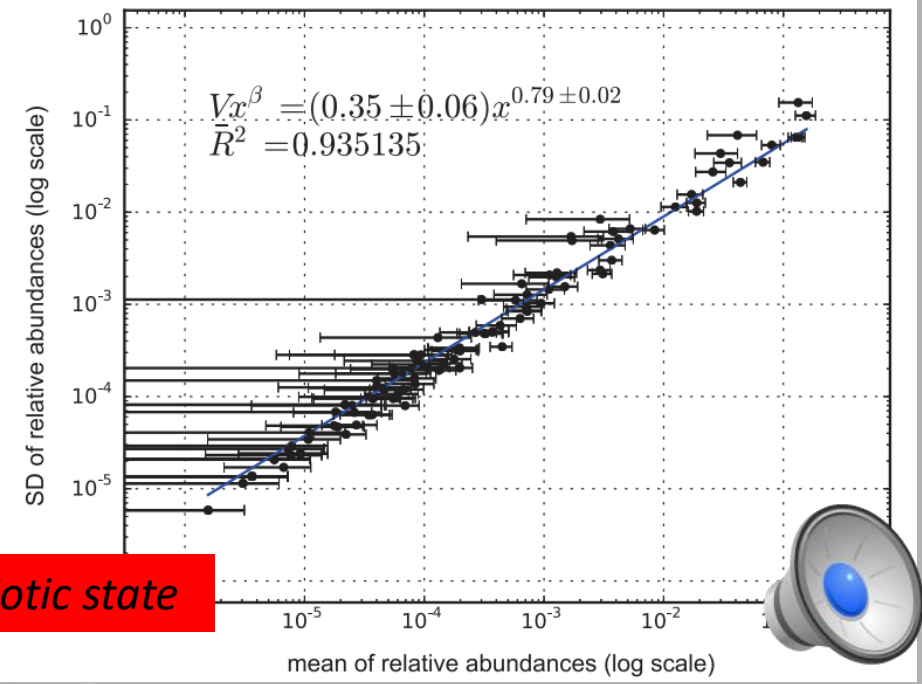


Fitness $F \sim$ Ability to Absorb
Environmental Signal = $E * \mu$

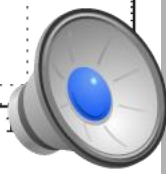
Health Imprinted in the Temporal Dynamics



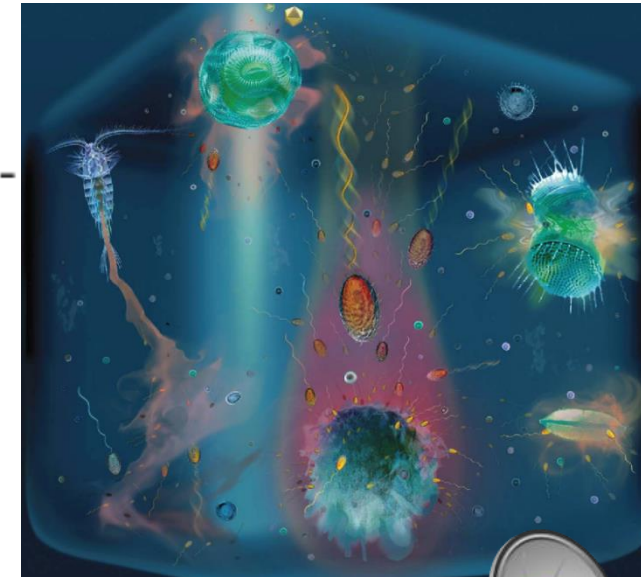
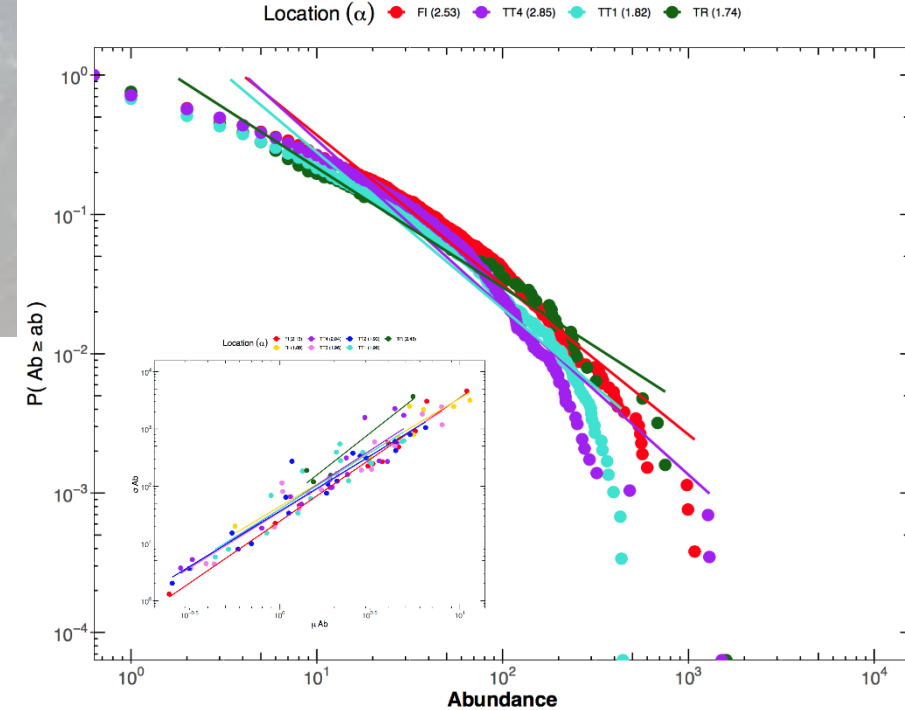
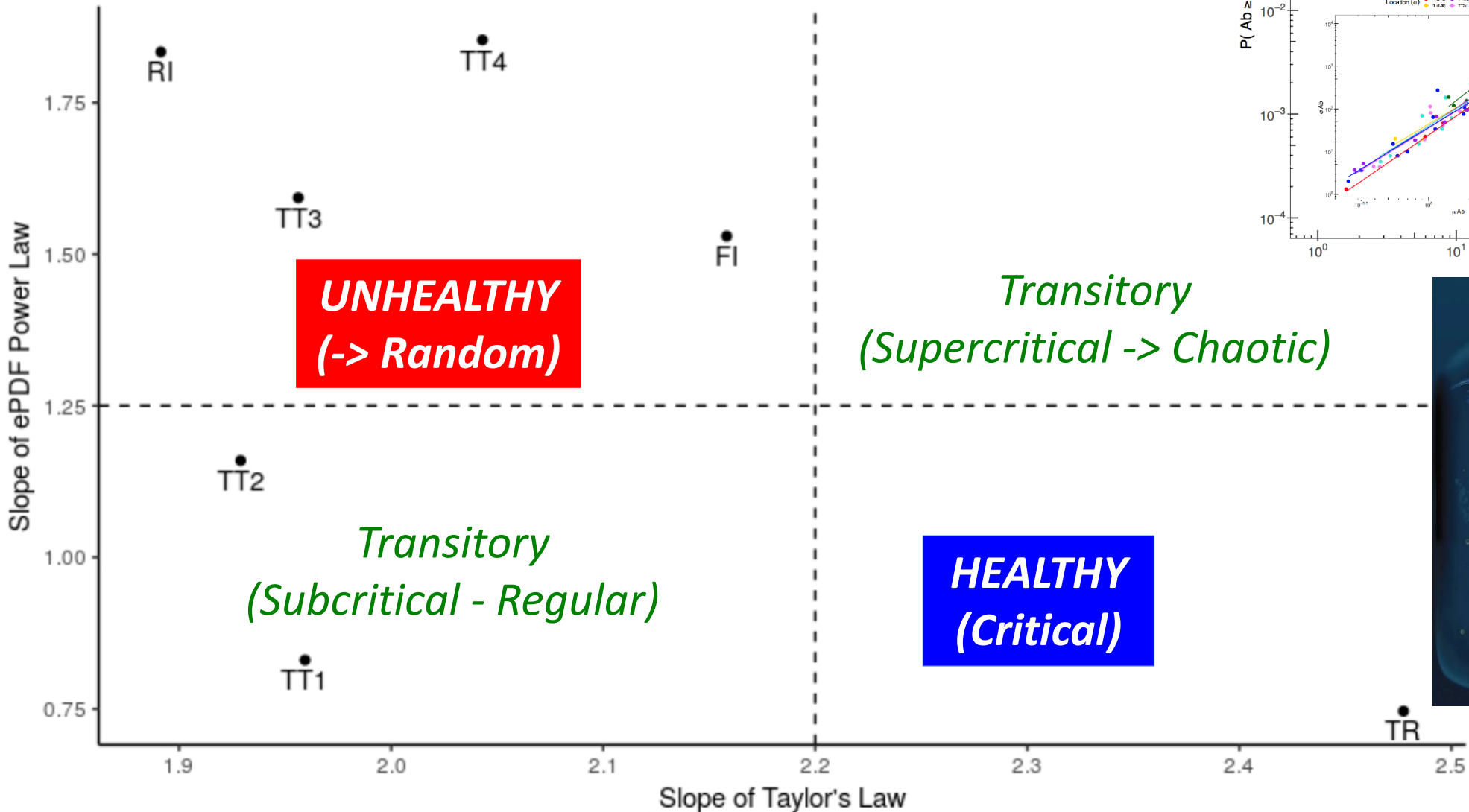
Healthy state



Dysbiotic state

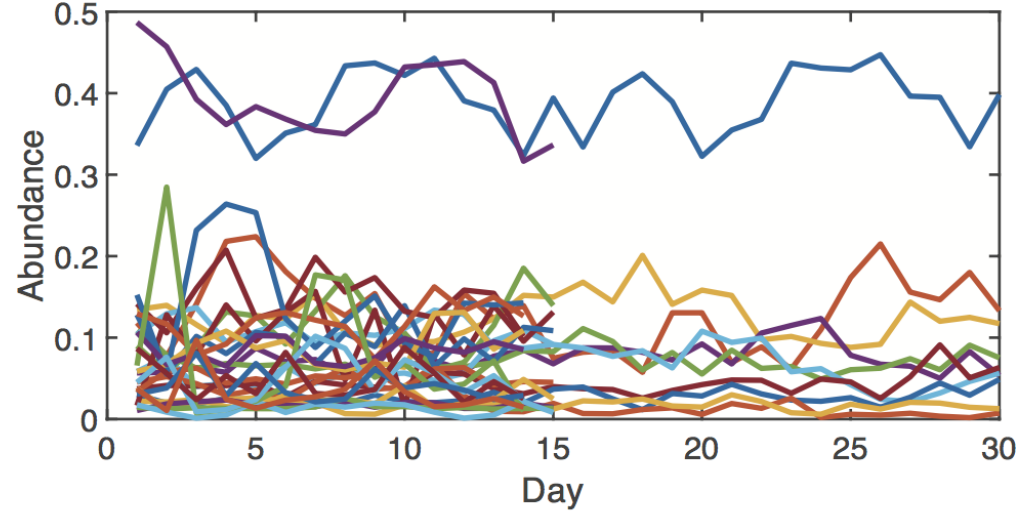


Macroecological Classification: Optimal Metabolic Function for Open Systems and Endemic Species

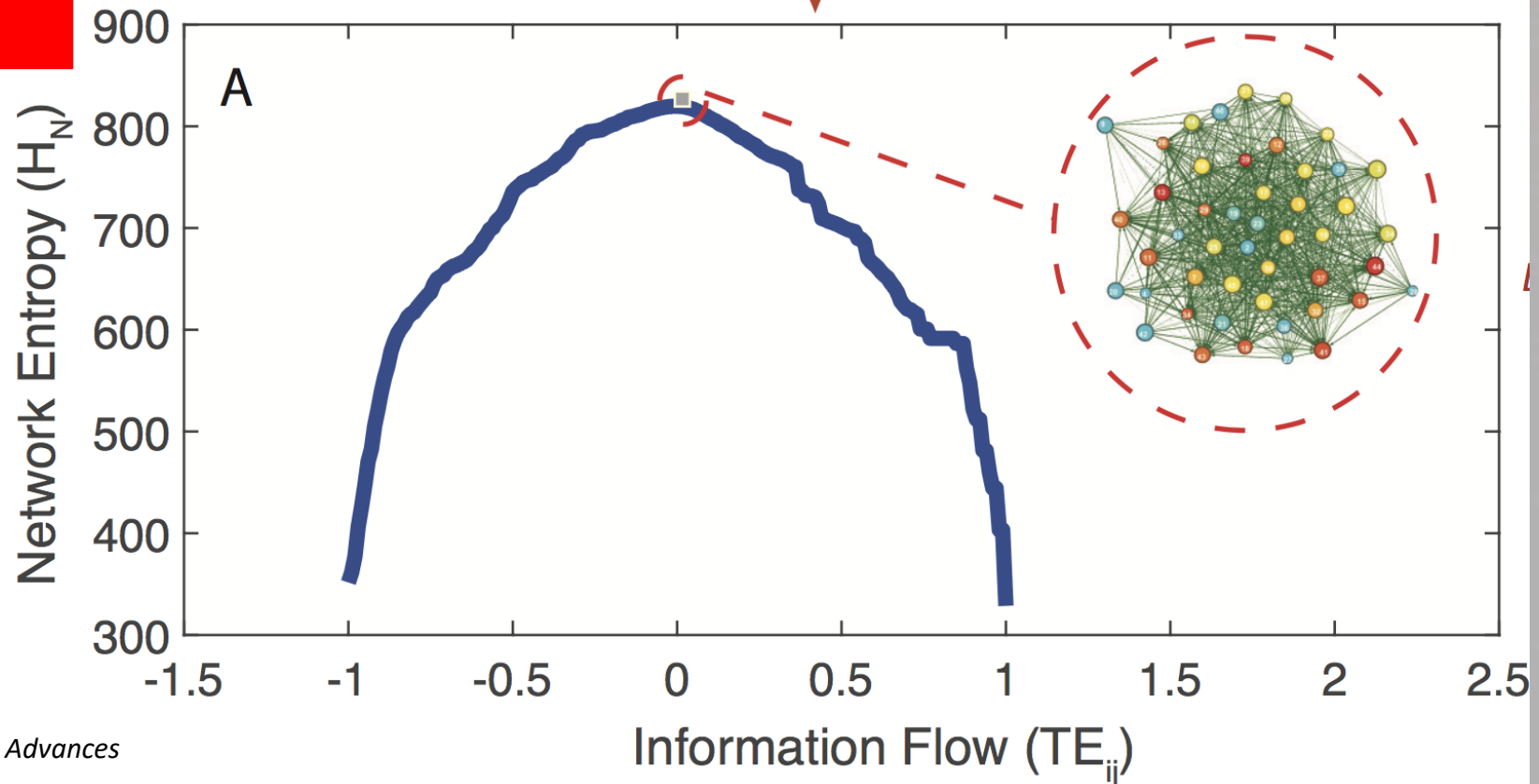


Species Functional Interaction Network Inference

OINs: the minimum directed functional and/or structural networks useful for predicting a systemic indicator



MICROBIOME NETWORK INFERENCE



Inferring Interdependency

$$H_{c,d} \sim \sum_i \Gamma(1 + d, 1 - c \ln(p_i)) \quad H = \sum_i p_i \log(p_i)$$

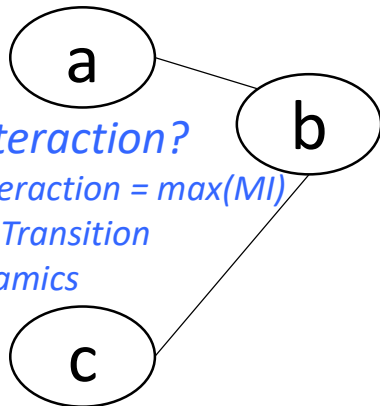
Hanel and Thurner, (2013), Entropy

Mutual Information

$$I(X, Y) = \sum_x \sum_y p(x, y) \log \frac{p(x, y)}{p(x)p(y)}$$

The amount of information that one variable contains about another variable. High I, d small.

$$d(X, Y) = e^{-I(X, Y)}$$

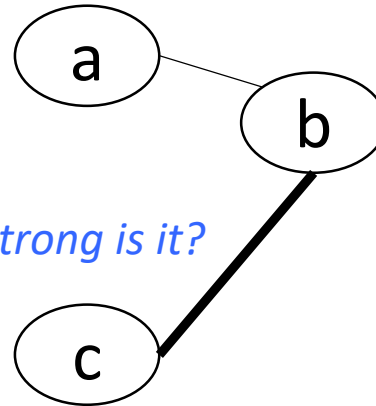


Is there an interaction?
Focus on Max Interaction = max(MI)
→ Prediction of Transition
vs Collective Dynamics

Conditional Entropy

$$H(Y|X^*) = - \sum_x \sum_y p(x^*, y) \log p(y|x^*)$$

The amount of information that one variable contains *conditional* on the knowledge of other variables. Entropy "Reduction".

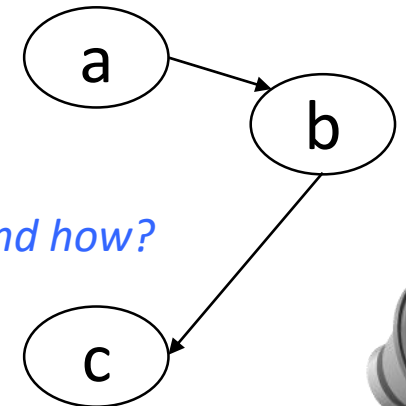


How strong is it?

Transfer Entropy

$$T_{X \rightarrow Y} = H(Y^\tau | Y^{t-\tau}) - H(Y^\tau | Y^{t-\tau}, X^{t-\tau})$$

The amount of information that one variable contains based on the knowledge of the *history* of another variable. After Entropy Reduction. TE ~ Causal Info Flow.



When does it occur and how?

Information Network Landscape

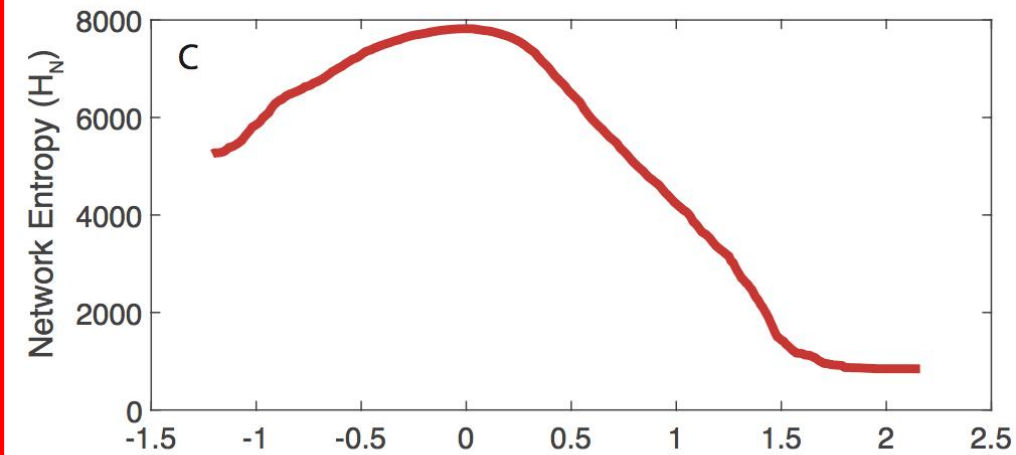
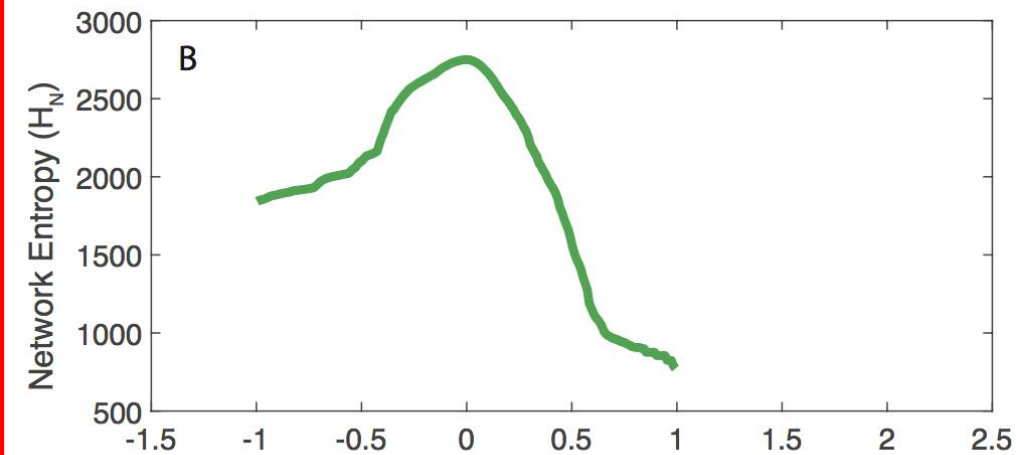
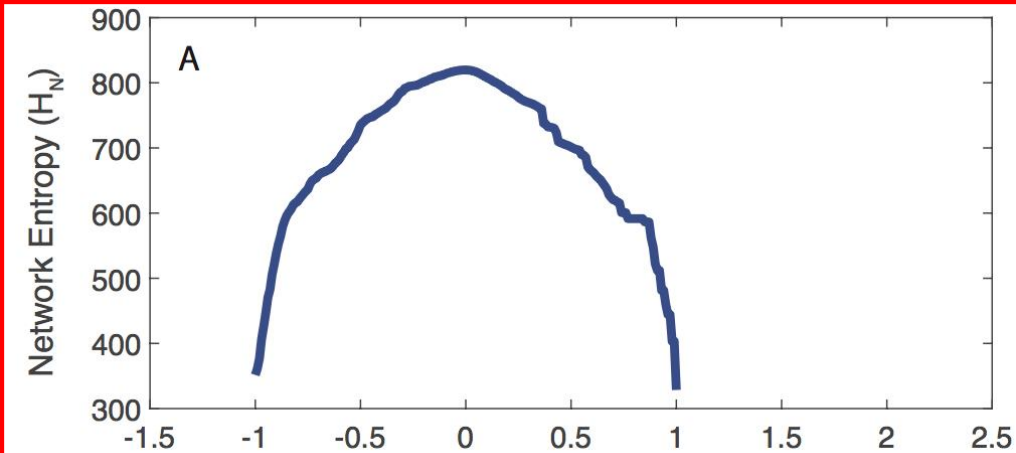
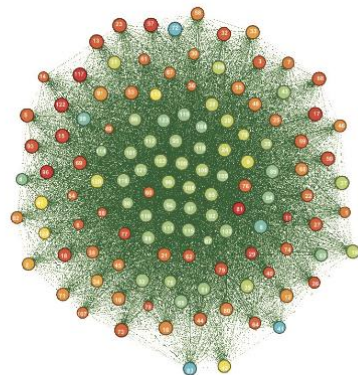
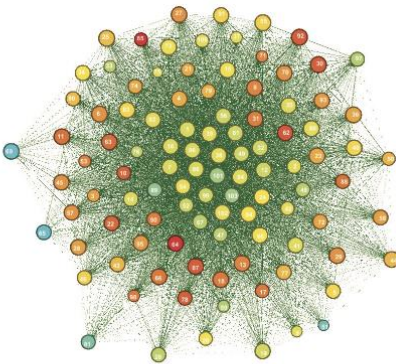
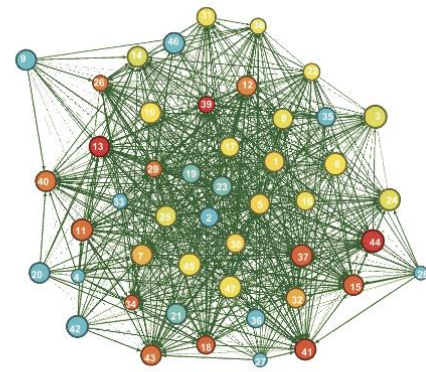
Neutral & critical

- Negative TE as Misinformation
- Extreme TE for increased Divergence & Asynchronicity

Non-ne

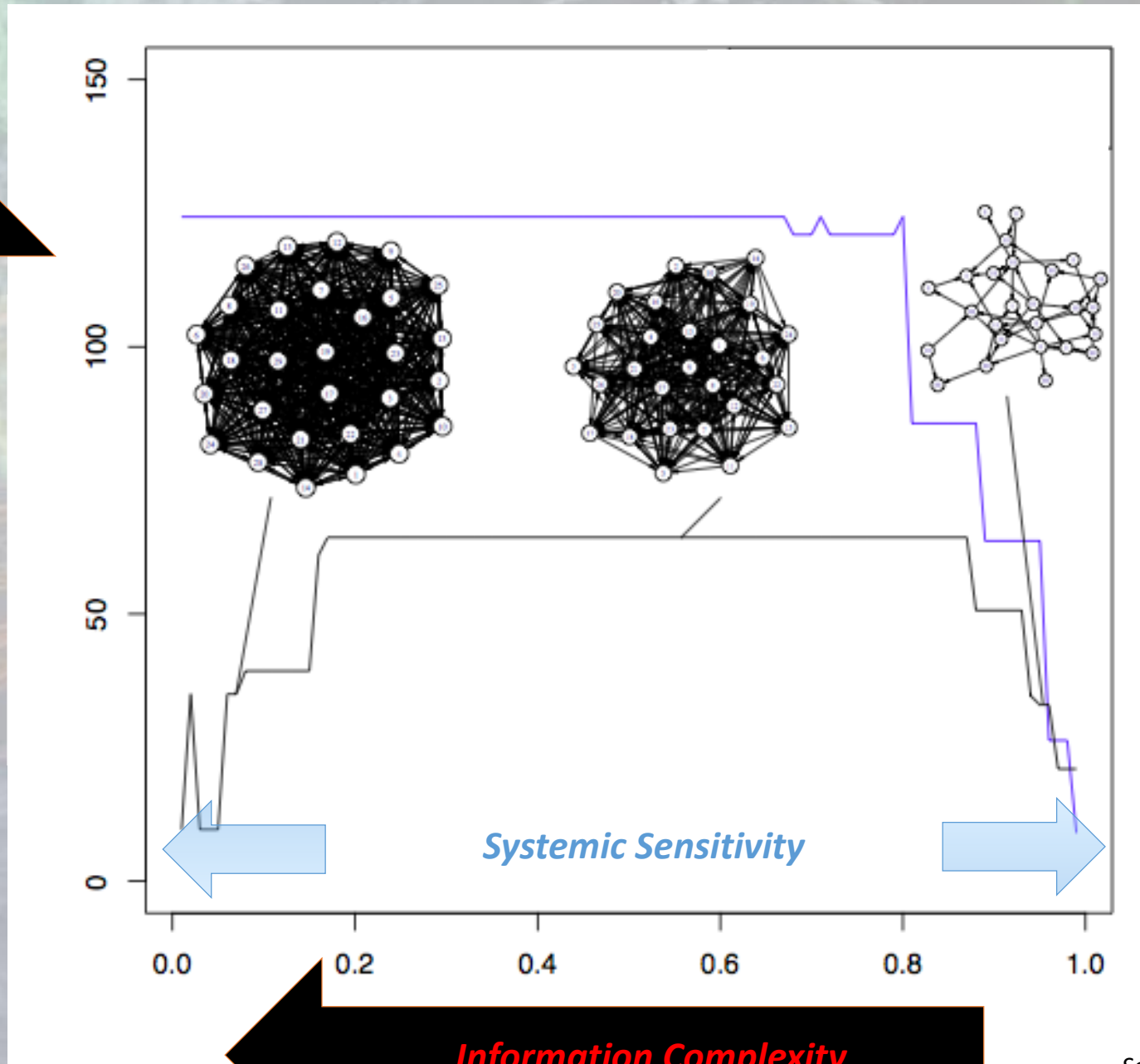
Env Variations (e.g. Infections, Stormwater, extreme Climate Change) are the cause of the environmental shift

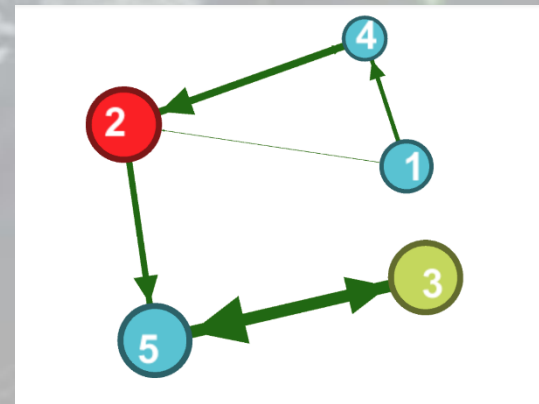
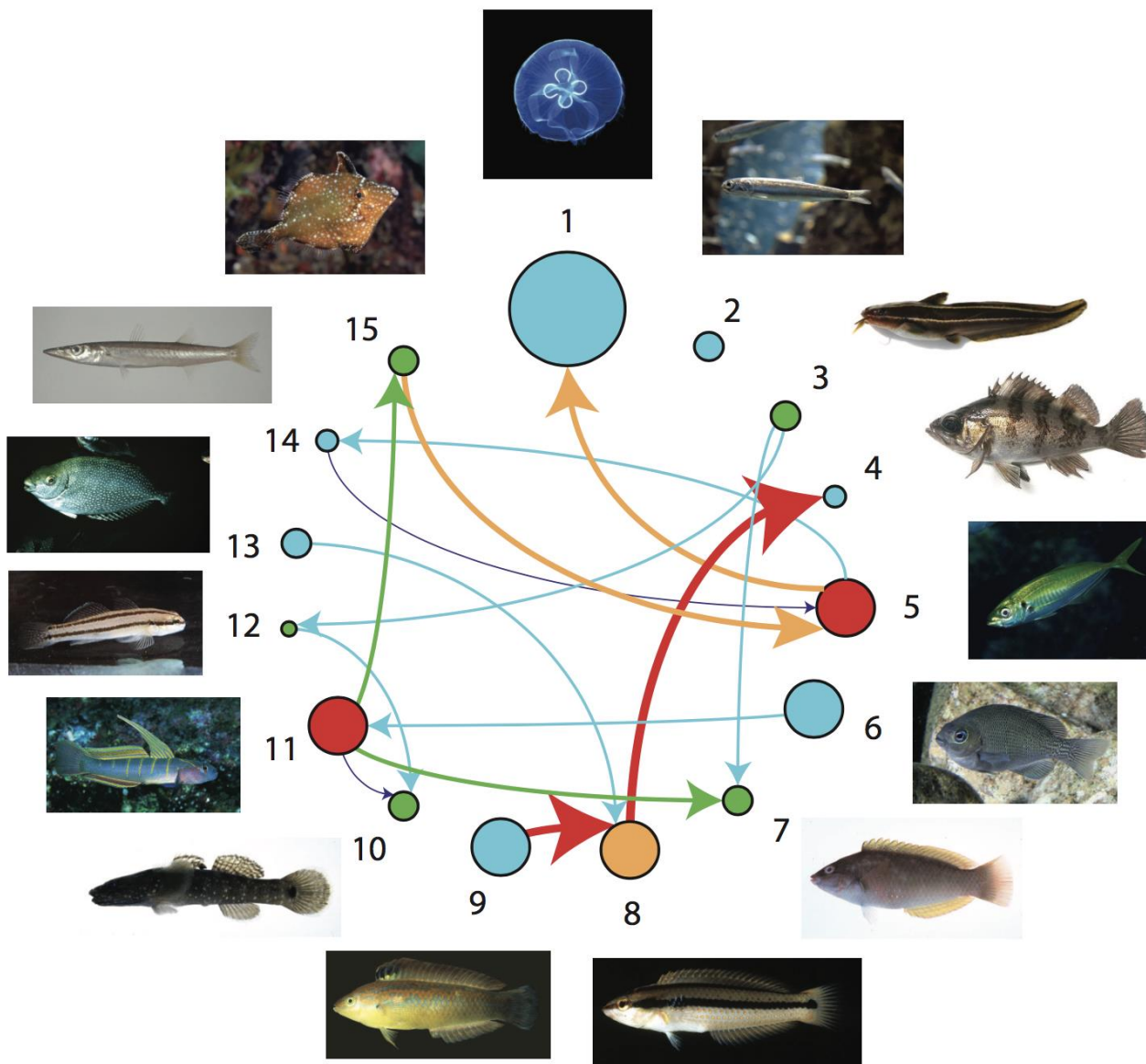
Non-neutral (niche) & chaotic



Complexity & OINs

The ambiguity of simplicity ... between order and chaos...





Network Viz for MaxEnt Interactions

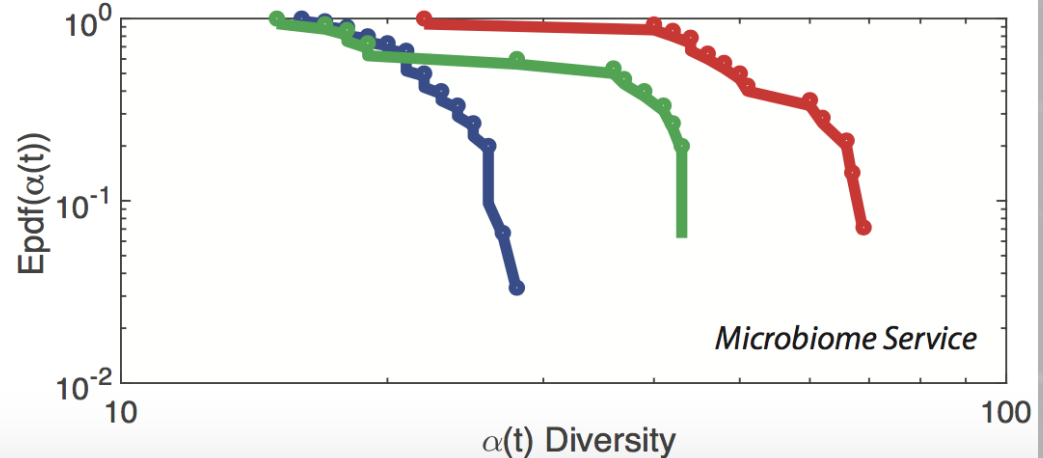
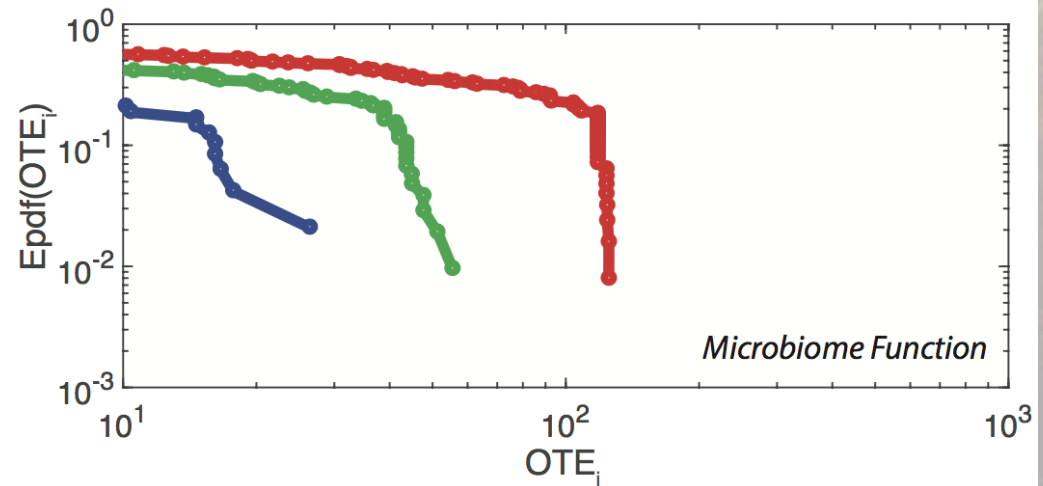
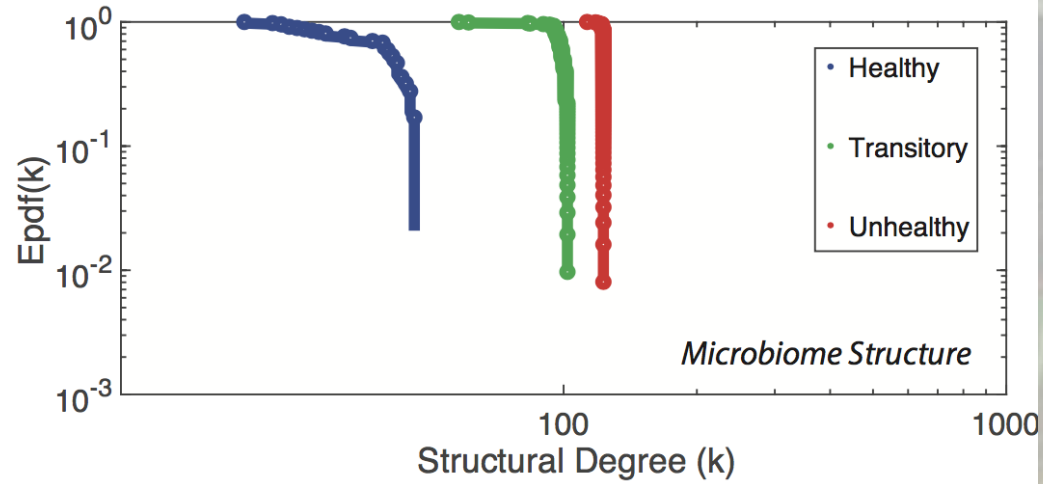
- (1) the **size** of each node is proportional to the **Shannon Entropy of the species (AIS)**
- (2) the **color** of each node is prop to the sum of **total Outgoing TE** of the node (OTE). The higher OTE, the warmer the color
- (3) **distance** = $\min(\exp(-I(X,Y)))$ where $I(X,Y)$ is the **mutual information** between variables x and y.
- (4) the **width** of each edge is proportional to the pairwise **Transfer Entropy/Info Flow**
- (5) the **direction** is related to $TE(i \rightarrow j)$; the direction of this edge is from i to j.



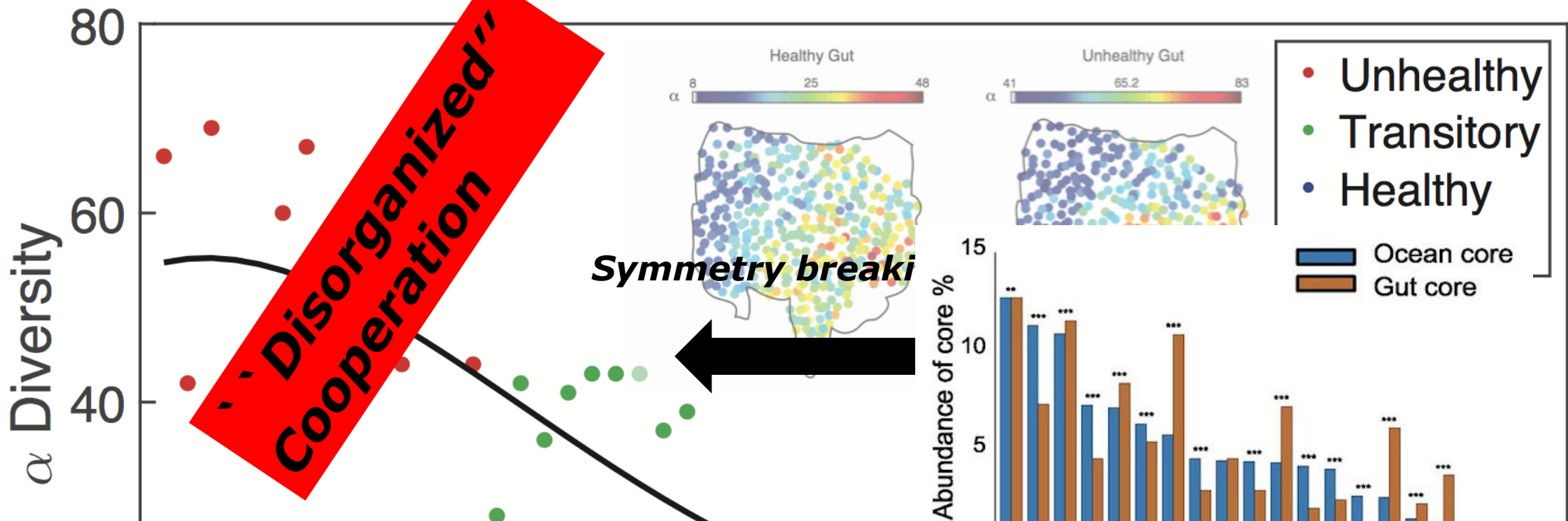
Structure is not precisely reflecting Function; therefore assessing the Information Exchange is crucial to guarantee Eco Services! Function-Service Nexus much stronger

It seems however possible to alter structure (if spatially defined, e.g. a dispersal net) and have an effect on function. Relationships between structure and function can be mapped!

Syntax, Communication, and Semantic



Second Order Phase Transition in the Human Gut



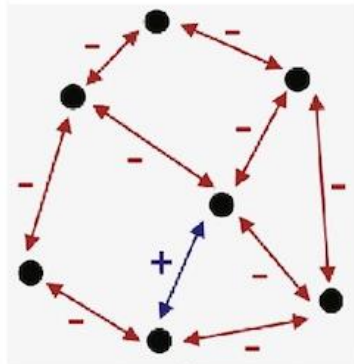
~70% of similarity between human and ocean microbiome (77% for unhealthy), topology & transition!

Transition Time

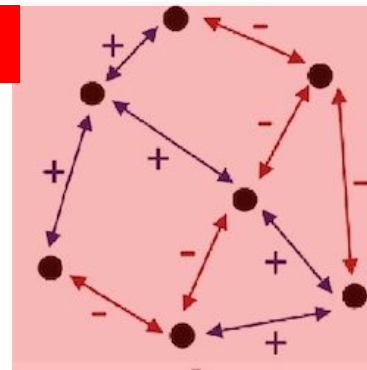


Network Function (as Predictable Dynamics vs Bio-causality) and Ecosystem Stability. Positive Interaction Bio-sensu -> Low predictability / Max Cooperation

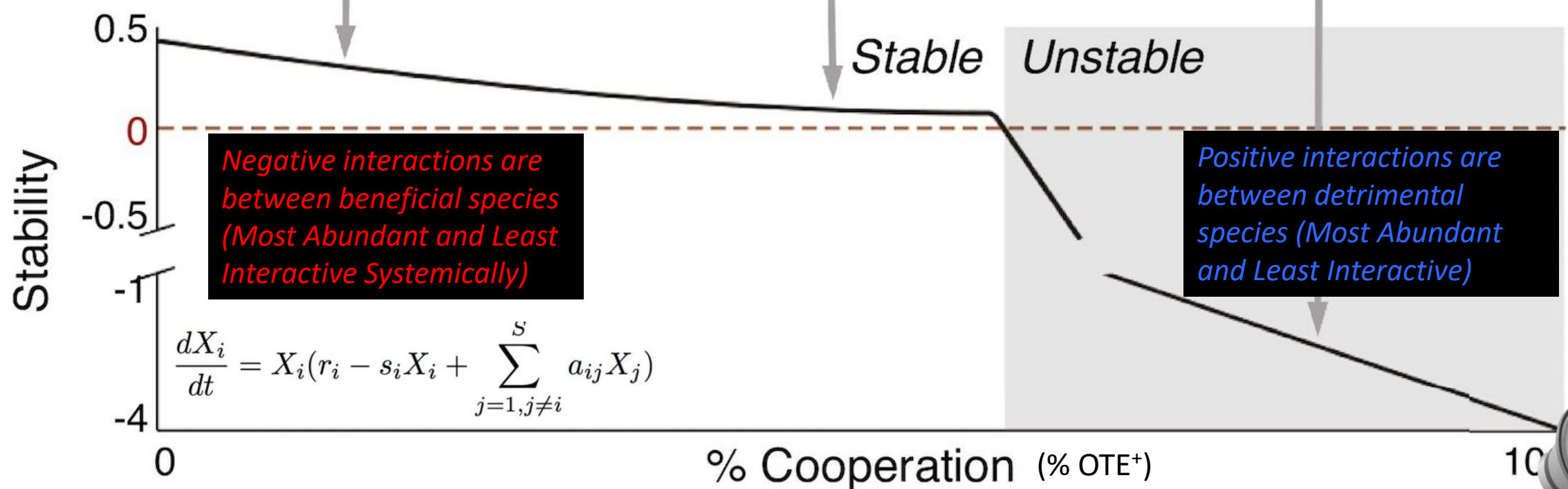
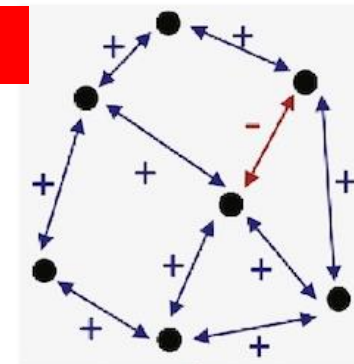
(c)



Neutral



Niche



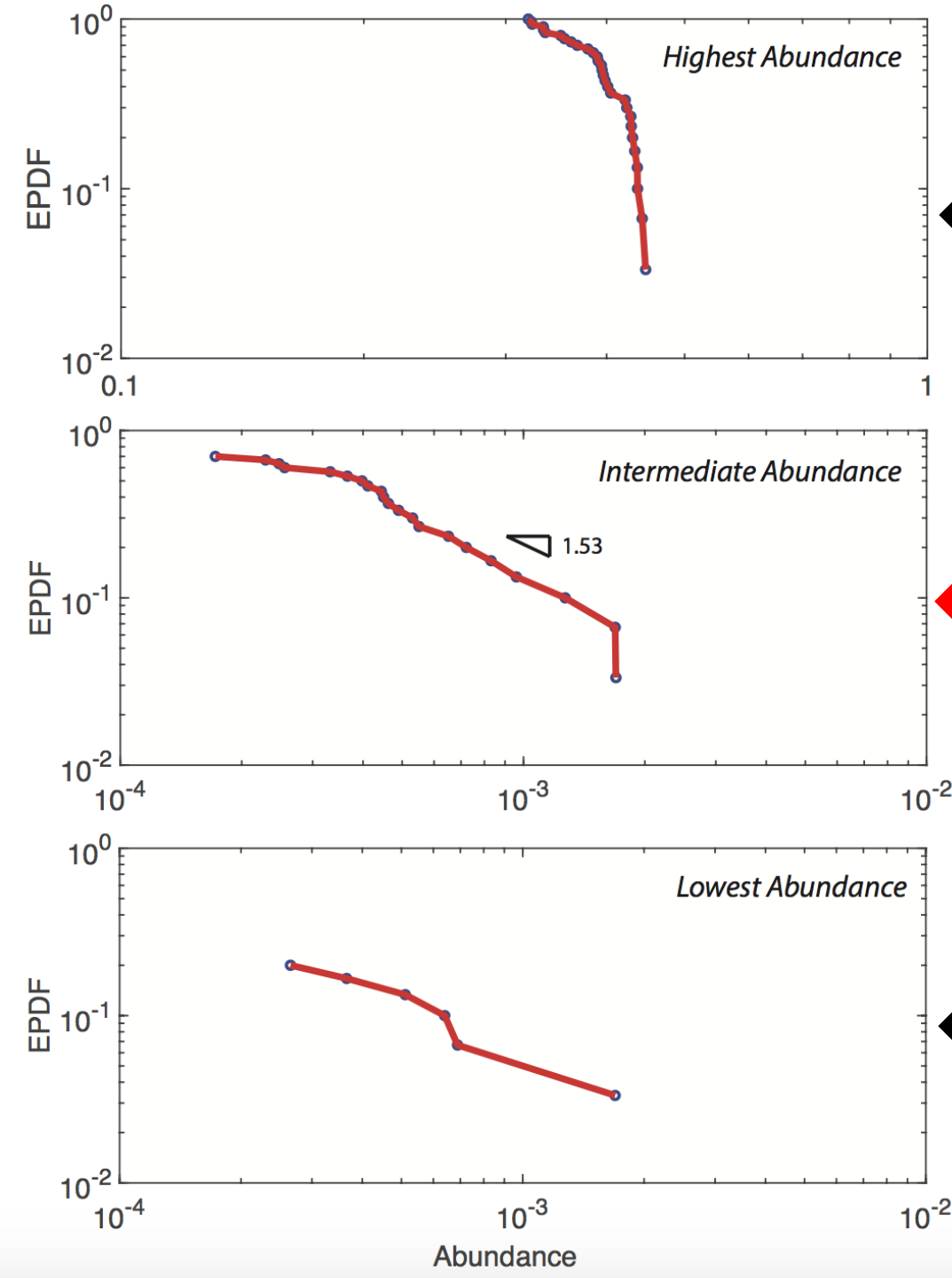
Species Abundance Distribution

The Common, "Dominant" (Low Fitness)

The dominant make the norm, but the uncommon produce the spiky evolution (those are the ones that "talk" the most) ... the Tragedy of the Commons, & on the diminishing role of network hubs

Most stable (High Fitness, Globally Stable)

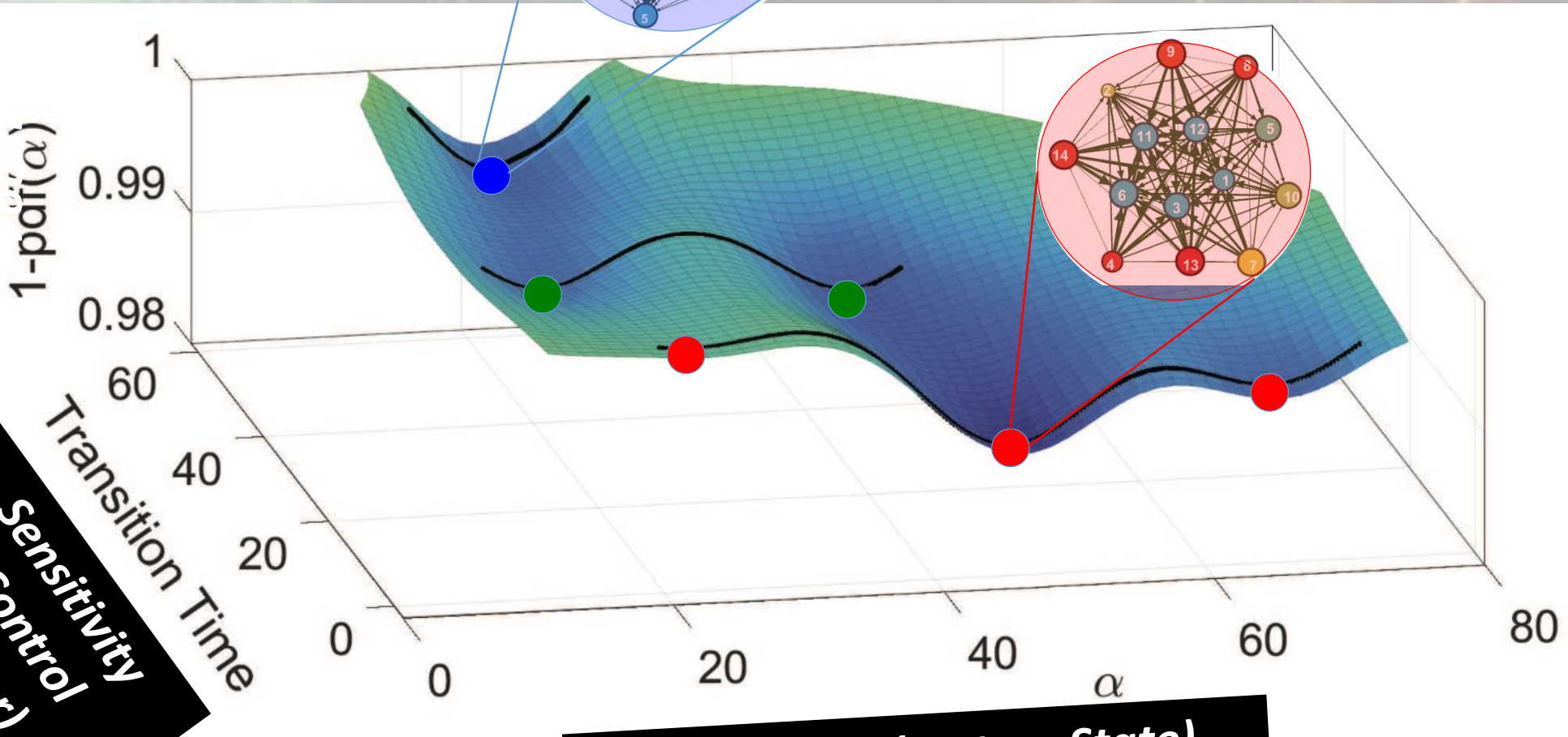
The Uncommon, Causing the "Butterfly Effect", the Tipping



Ecosystem Potential Landscape

$$E_F = E_T \text{ (dissipation)} - H$$

Free Energy/Information



Sensitivity (Control Factor)

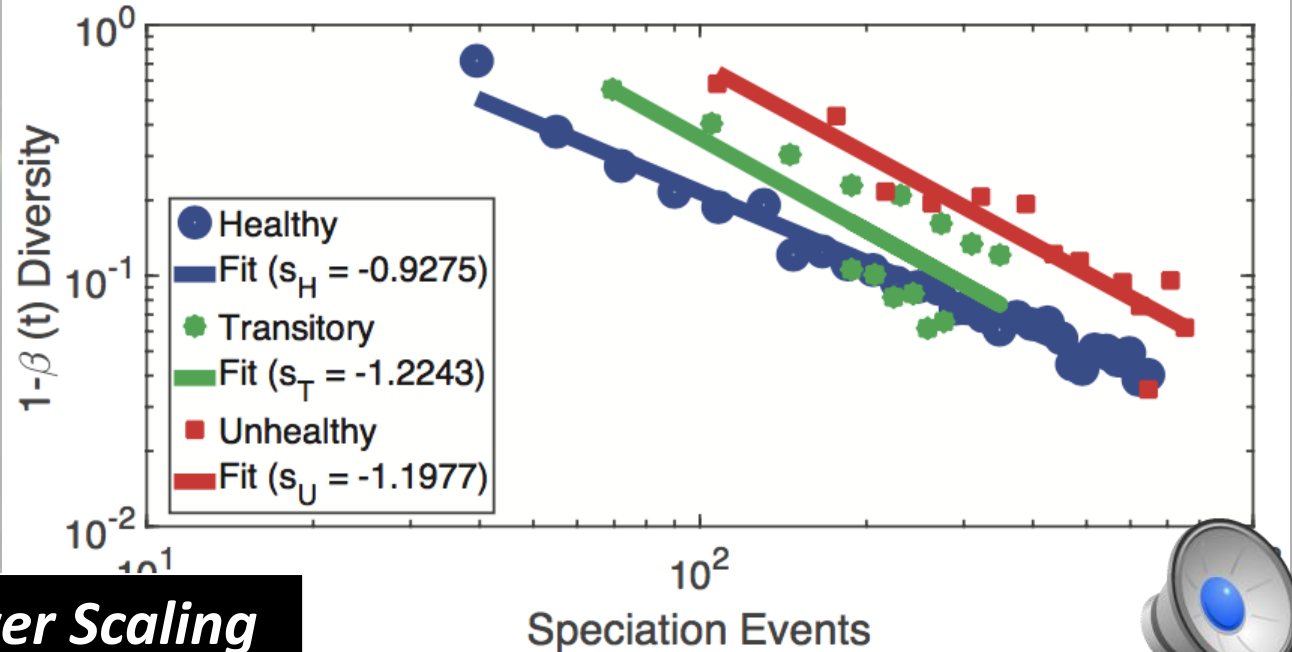
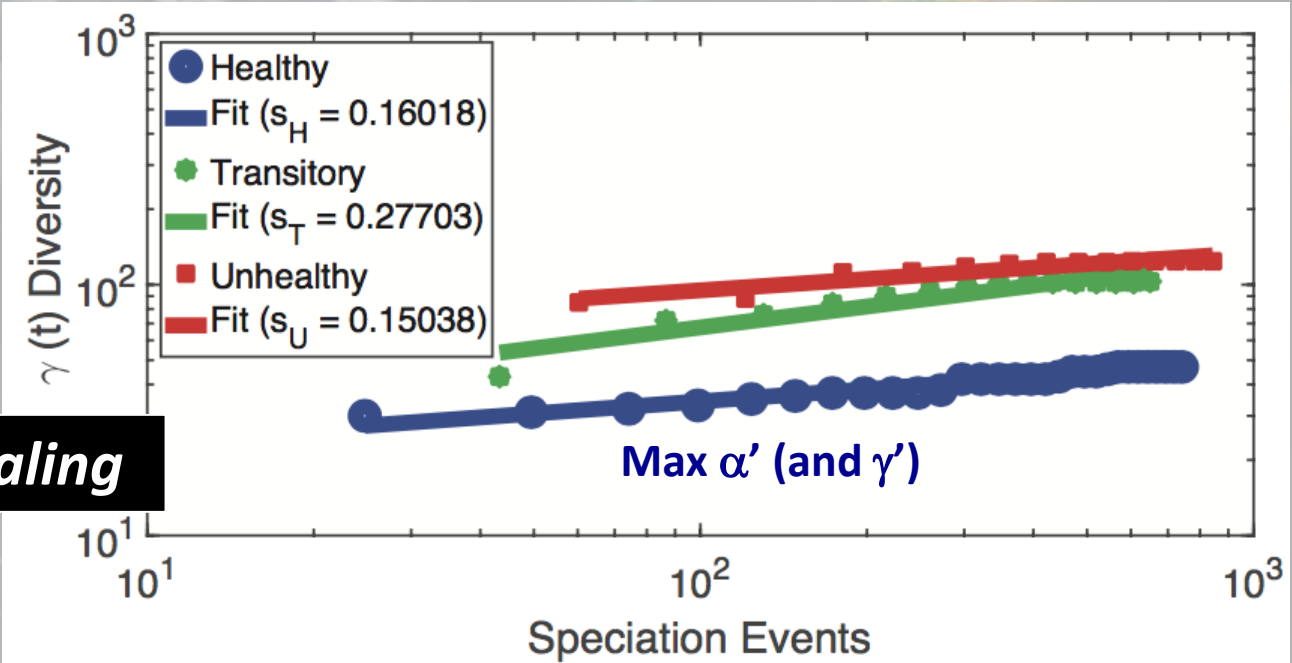
Complexity (System State)



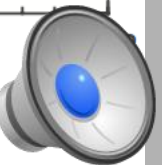
Macroecological Patterns

Principle of Optimal Evolution and Diversity Decay

Species-Area Scaling



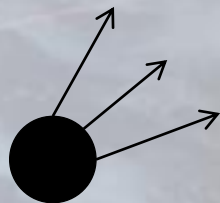
Species Turnover Scaling



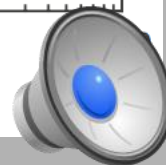
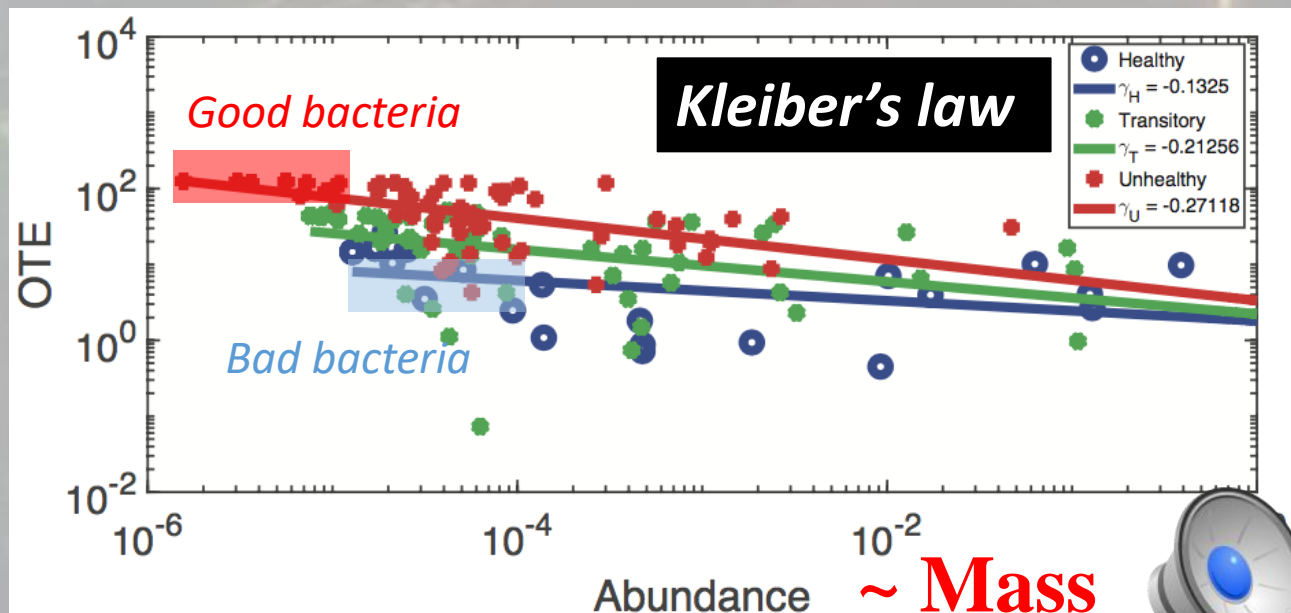
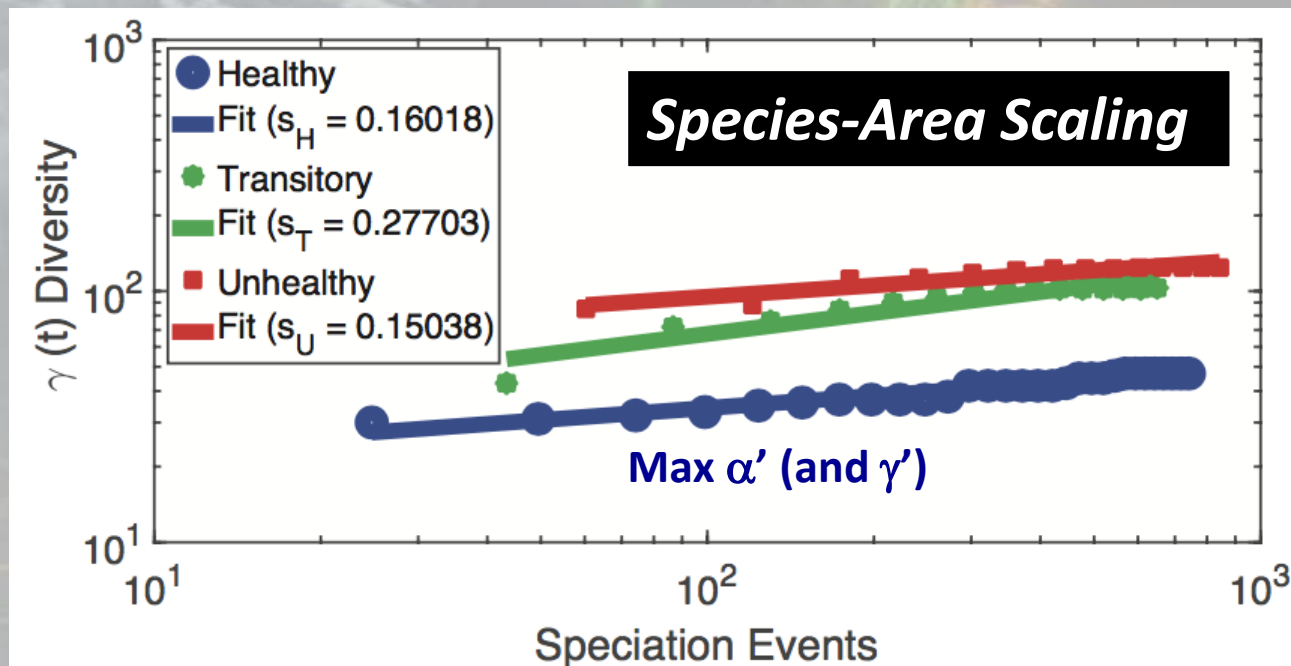
Macroecological Patterns & Network Function

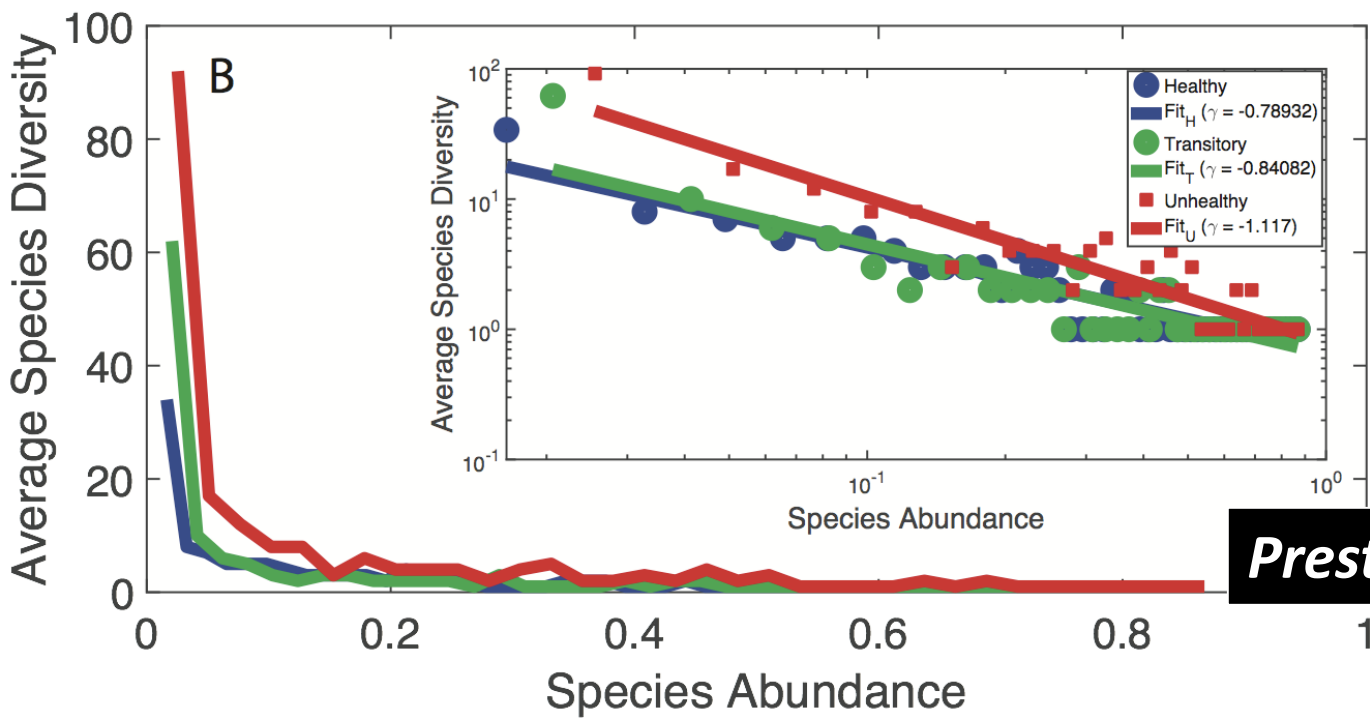
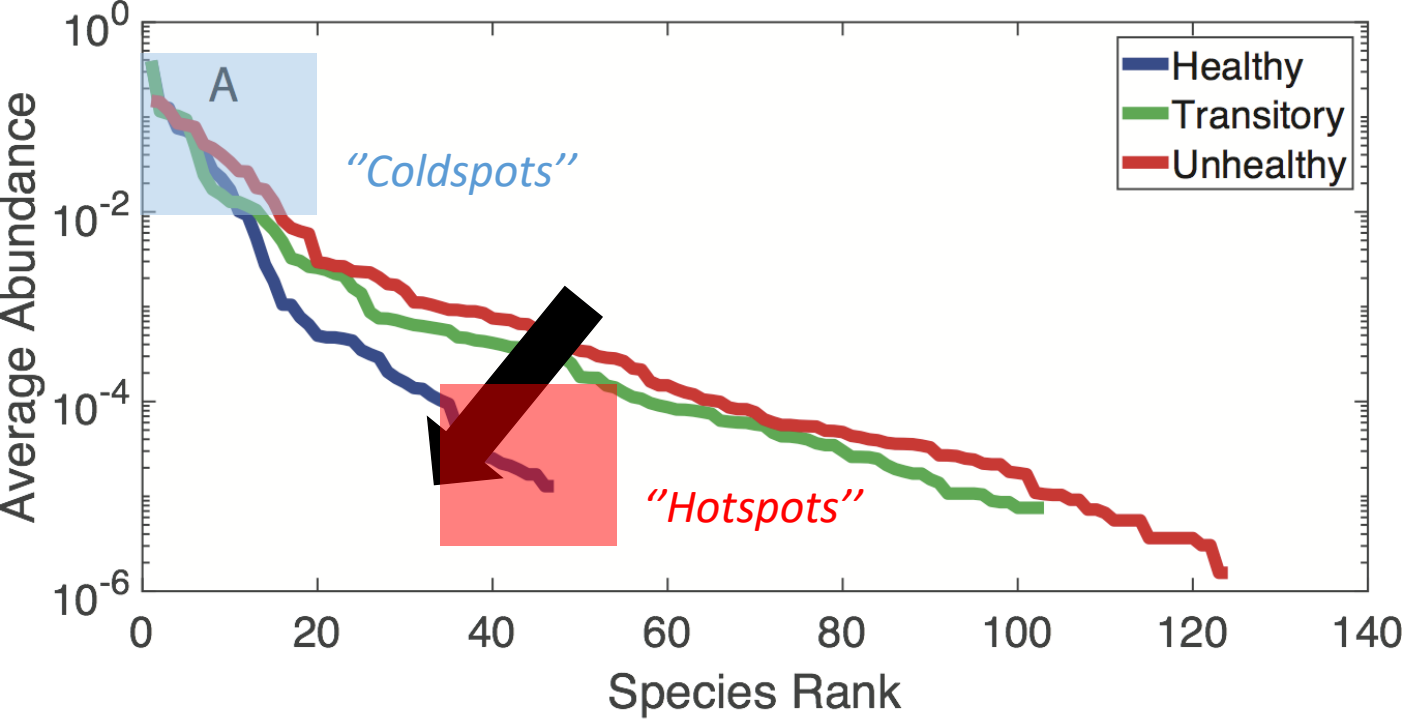
Principle of Pareto Optimal Evolution
("Heaps' law")

Each Abundance class defines a
Function (OTE) \sim Hydrolisis Rate



\sim Metabolic
Rate_{mass spec}

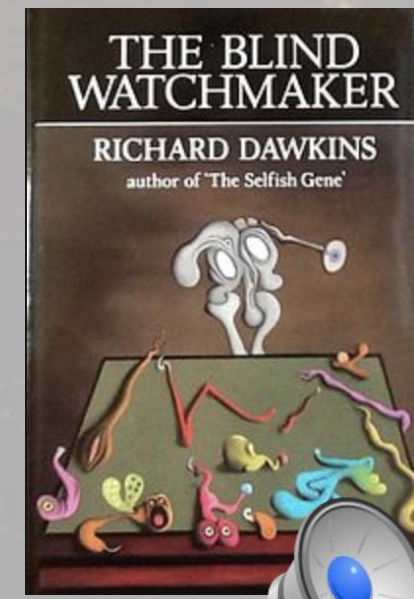
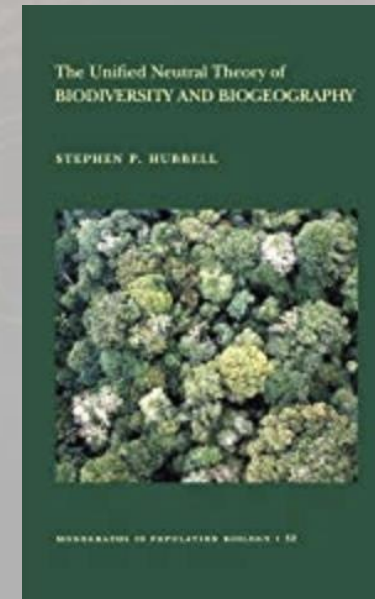




Preston Plot

Universal Pattern and Singular Variations: Transitions from Simple Patterns

A **power-law decay** of the Relative Species Abundance (RSA) for the **unhealthy microbiome** is what we desire (!) vs. the expected neutral and **Poissonian pattern** of the **healthy RSA**



Convertino and Li (2015), Ecol. Lett.

Information Dissipation for Info-based Species Rank

How long is the information about a node's state retained in the network? (Active Information Storage)

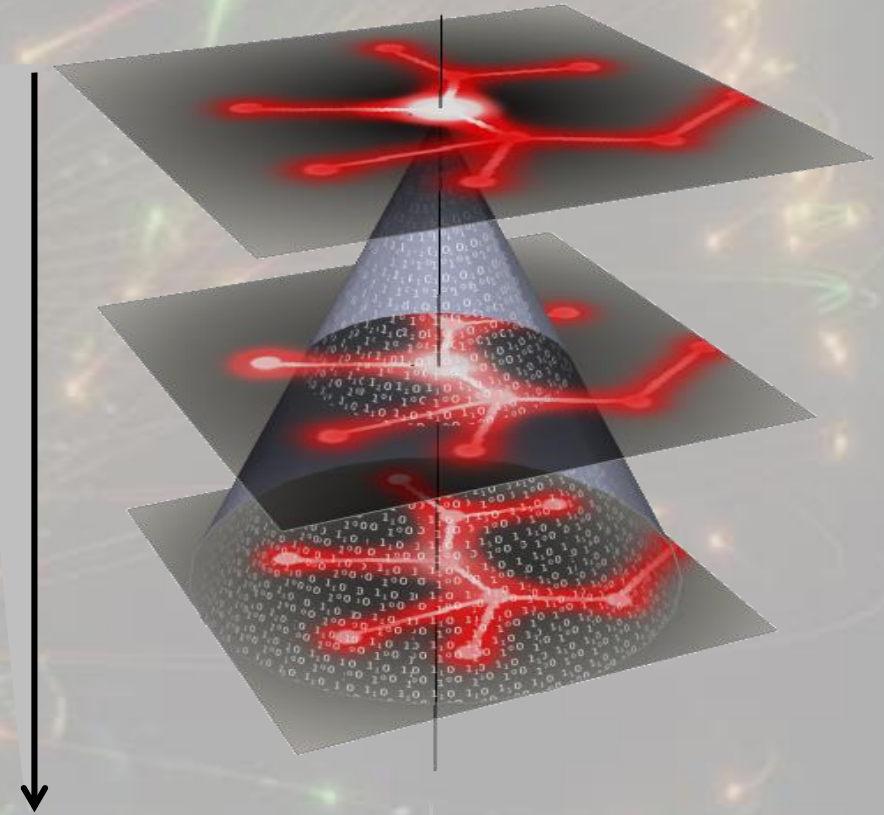


measures of influence of a single node (or of a stressor) to the dynamics of the entire network!



How far can the information about a node's state reach before it is lost? (Transfer Entropy)

Information dissipation time



Information dissipation length (space)



Info Balance -> Info-theoretic Global Sensitivity Analysis

Ludtke et al., 2008, JRSI
Saltelli et al., 2008, JWS
Convertino et al., 2013, EM&S

Information Balance Eq.

Local Variability

Functional and/or Structural
Systemic Variability

$$H(IH) \approx \sum_i H(x_i) + \sum_i \sum_{j \neq i} TE_i(x_i, x_j) + \sigma(IH)$$

Noise

General Collective sensitivity indices

$$\mu_i = \frac{H(x_i) \cdot g(x_{i,t})}{H(OIN)}$$

$$\sigma_i = \frac{OTE(j) = \sum_i TE_{j \rightarrow i}}{H(OIN)}$$

Collective sensitivity indices (constrained to predictability of ecoservices Y, e.g. α)

S_i - first-order sensitivity index

$$I(X_i; Y) / H(Y)$$

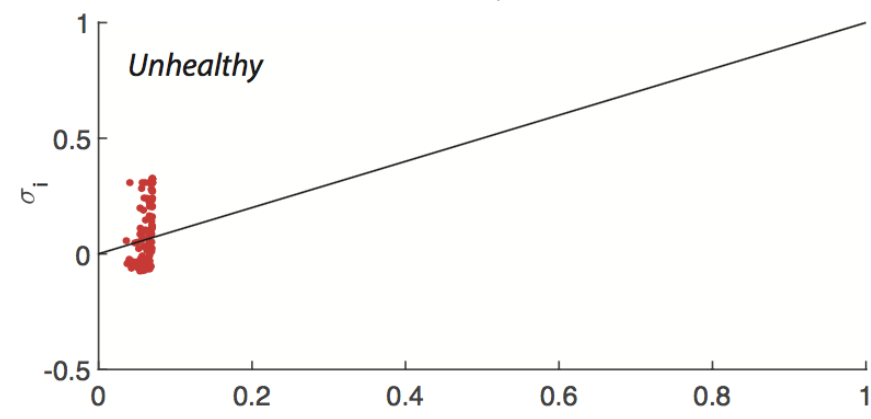
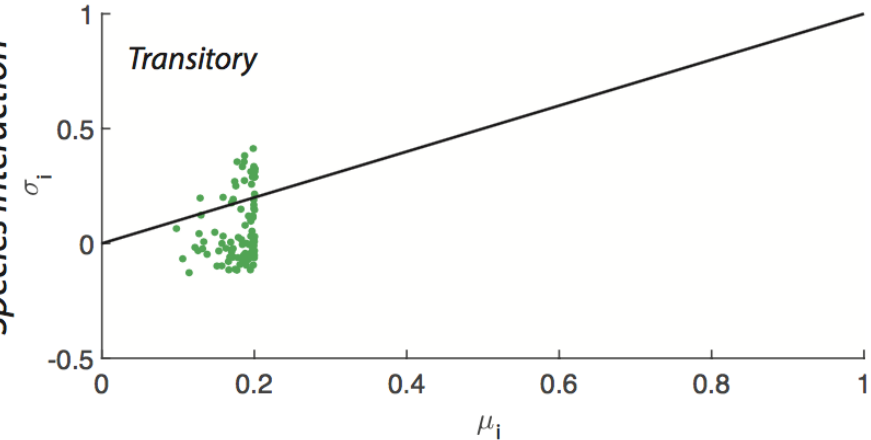
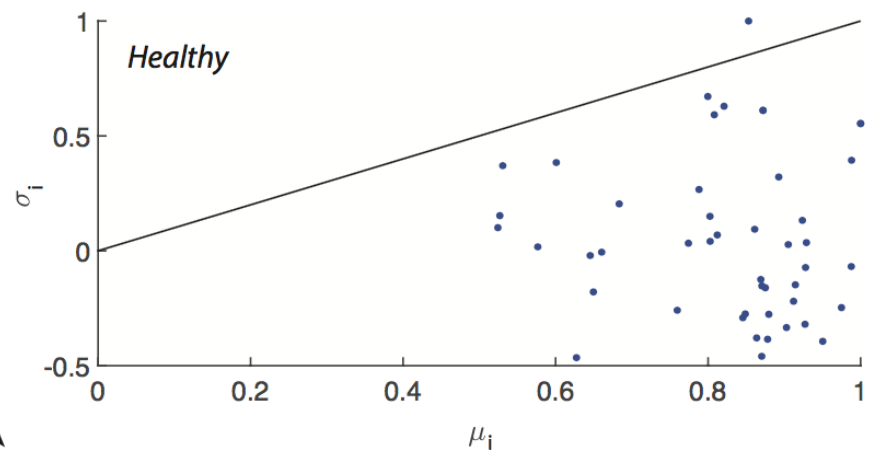
S_{ij} - 2nd ord. sensitivity index

$$I(X_i, X_j; Y) / H(Y)$$

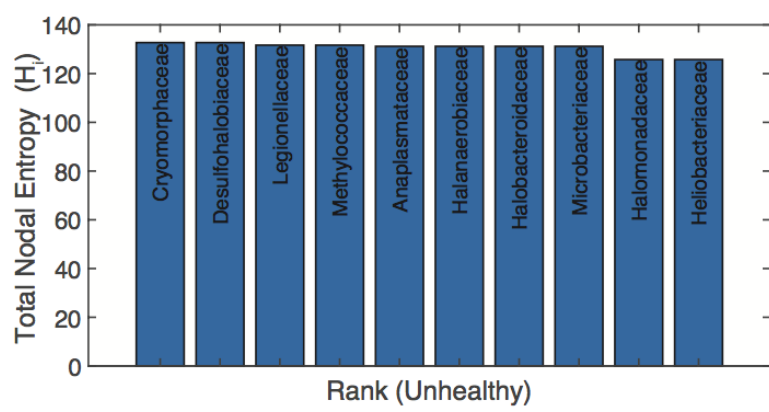
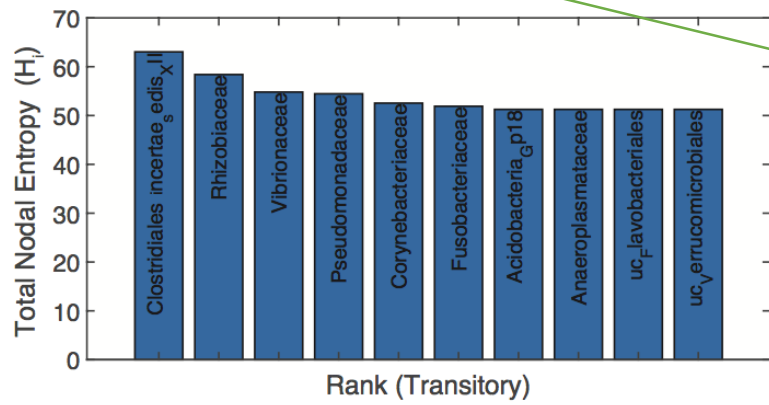
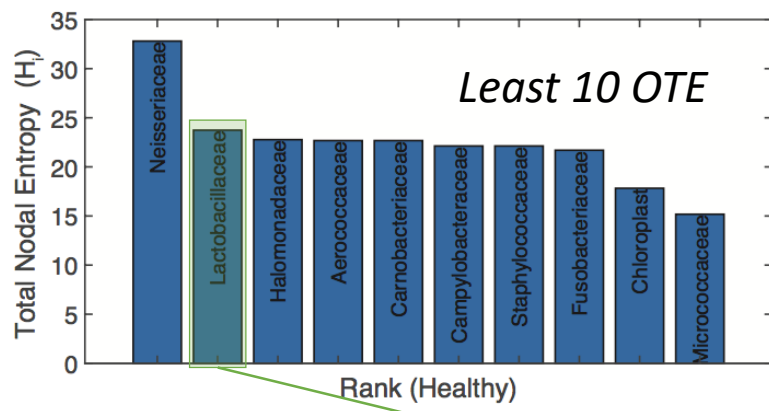


$$\sigma_i = \frac{OTE(j) = \sum_i TE_{j \rightarrow i}}{H(OIN)}$$

Species Interaction \rightarrow



Species Singular Importance \rightarrow $\mu_i = \frac{H(x_i) \cdot g(x_{i,t})}{H(OIN)}$

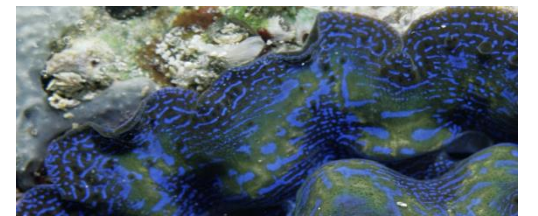


Pinpointing Causes for Microbiome Engineering: TEI

Probiotics (Bacteria Inoculation)



Eco-engineering (e.g. symbiotic algae) with potential for nutrient filtering



Geomorphic Engineering (Temp & hydro protection)

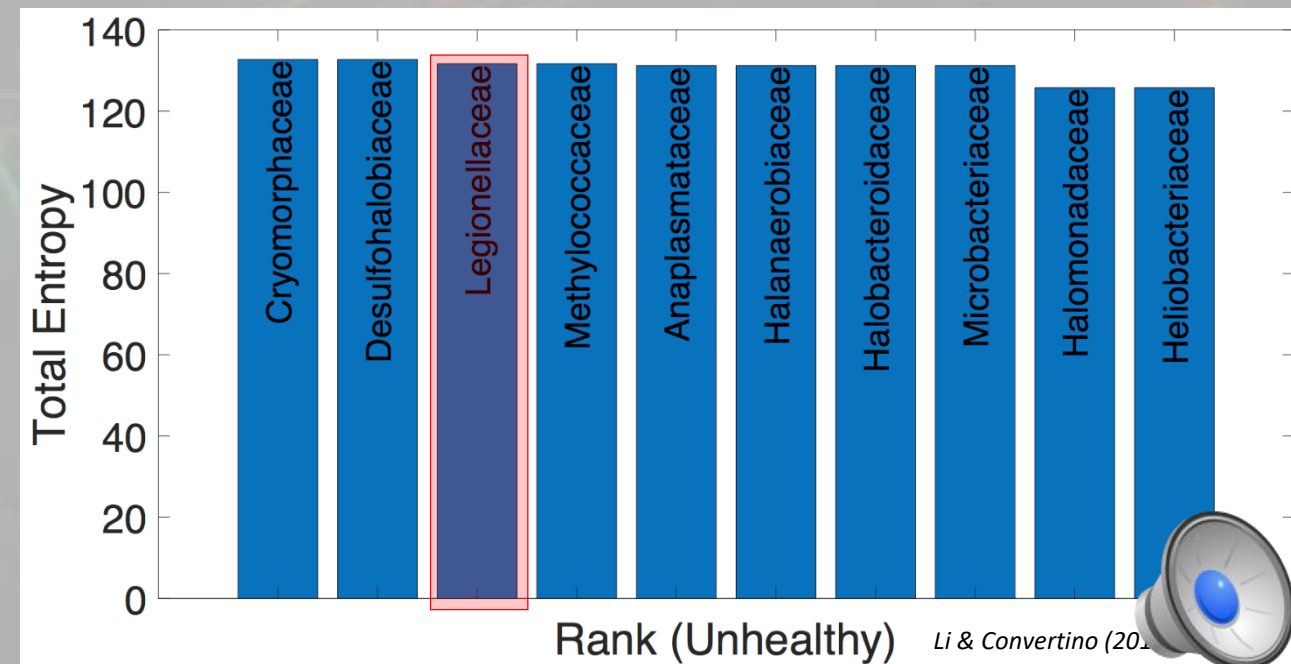
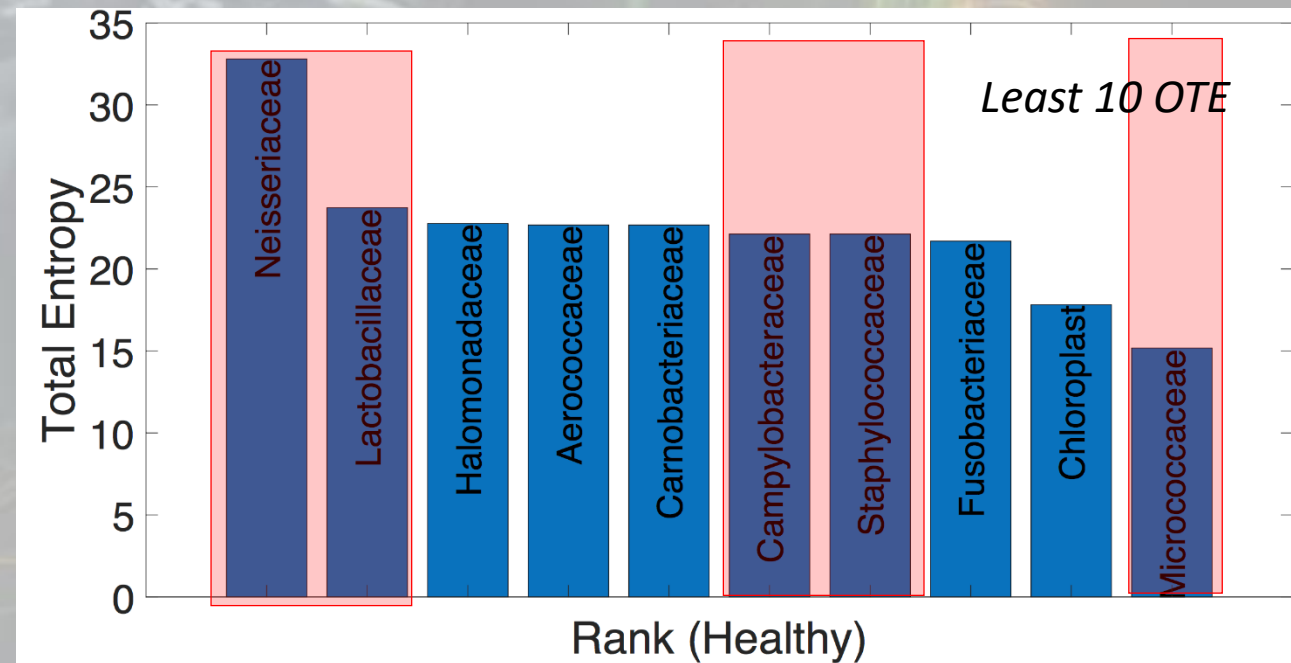


Detection of Top Species contributing to Health States for Population / Personalized Control

The top ten **active nodes** (competitive, predictability sensu) in the healthy state are **the least abundant** and **the most dangerous** species; however they are kept under control by the “good” nodes!

The top ten **active nodes** (competitive, predictability sensu) in the unhealthy state are **the least abundant** and **the least harmful** species; unfortunately they are controlled by the “bad” nodes!

“Hubs” (or better **CRITICAL NODES!**) have fewer active interactions and they are **competitive** (positive feedbacks biological sensu, TE is high). On the diminishing role of network hubs (based on k) ... vs “weak” ties (Granovetter) for predictability & health



OTE Importance

OTE = total Outgoing Transfer Entropy

TE = pairwise Transfer Entropy

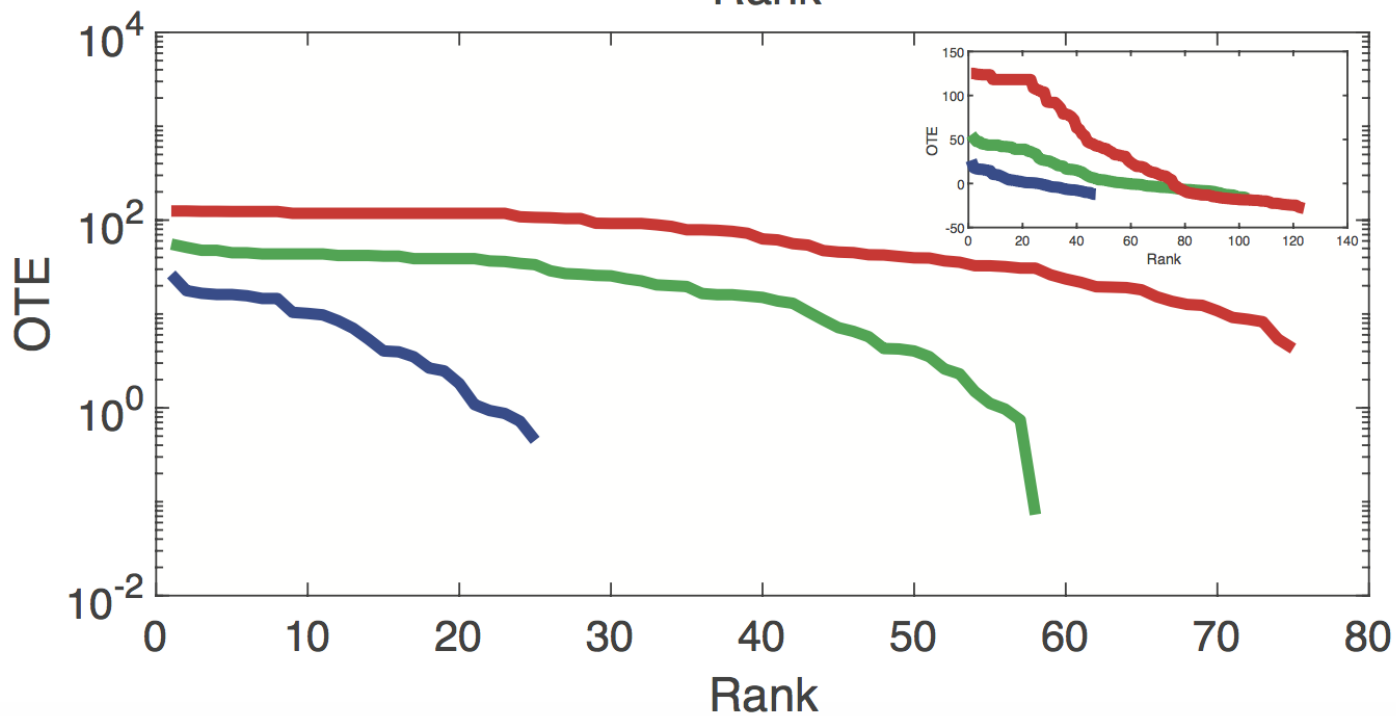
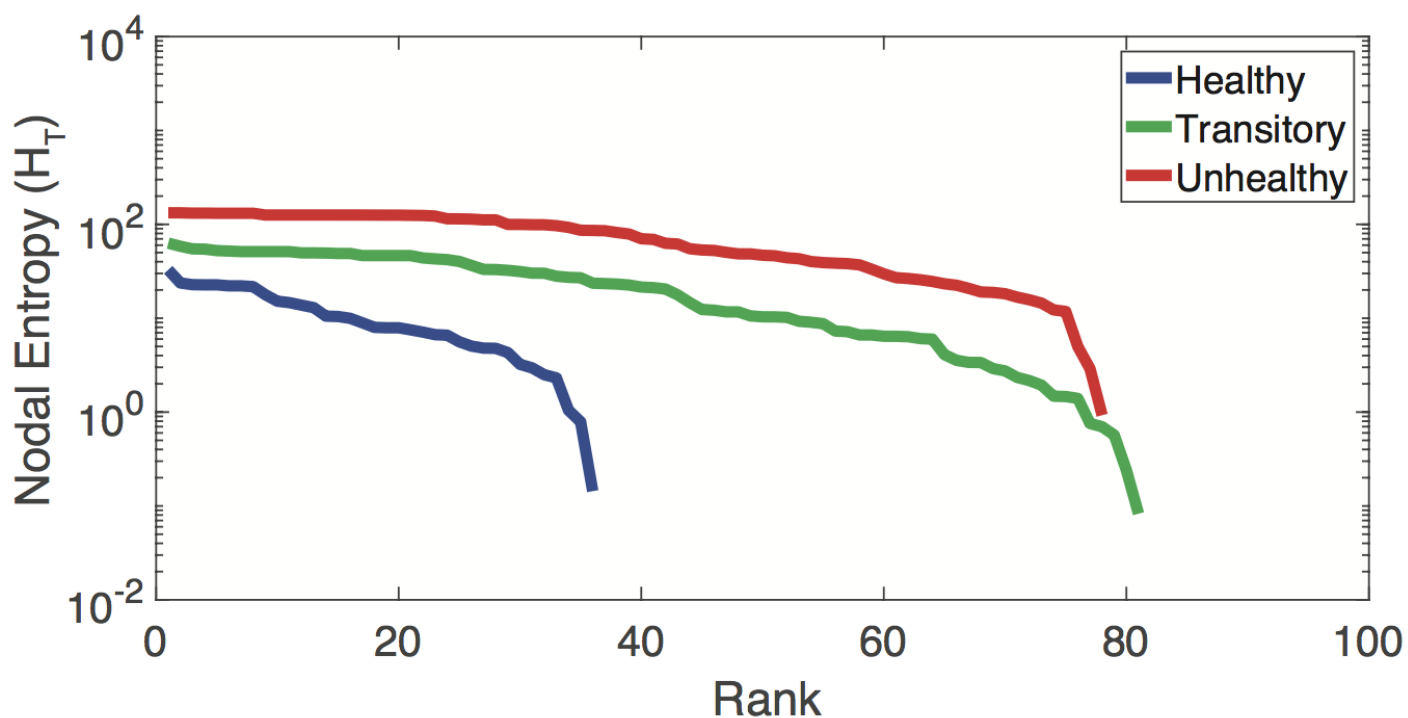
NIS: Net Information Storage = Sum of Incoming TE – Outgoing TE

OTE is controlling the dynamics of the network (in terms of network topology)!

Unhealthy: Random Nets

Healthy: SW Nets with tendency

SF



Specific Findings

Neutral symmetrical patterns correspond to *healthy states*; this corresponds to *small-world states* that has a tendency toward a *scale-free (fractal) optimal state*; *SW is optimal against random and targeted attacks*

The critical state correspond to *the neutral state* where + and – interactions are balanced; *criticality is not at the phase transition (of second order in this case) and is not caused by instantaneous external trigger (Criticality conferring Resilience)*

The Highest Diversity Growth Rate is The Healthiest, yet suboptimal State; Max Feasible Entropy across the Info Landscape. Unhealthy State with Non-native Diversity

The most abundant are the most beneficial and the least interacting species in the healthy state (Endemic State). Most Competitive systemically -> Highest Predictability.

New Definition of Network Hubs (CRITICAL NODES!) based on OTE v

OTE Ranking Focused on Species Causing Transitions

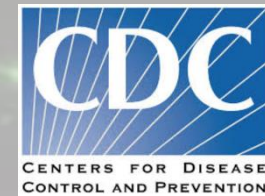
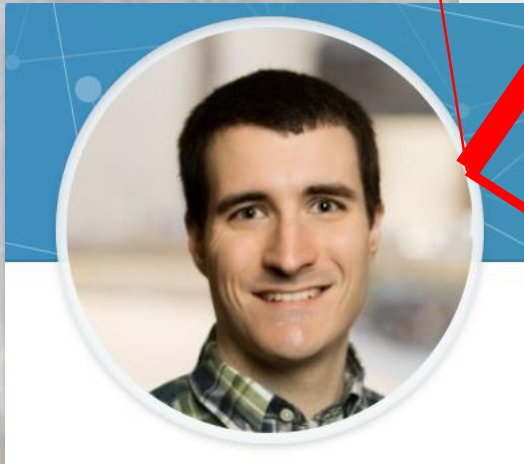
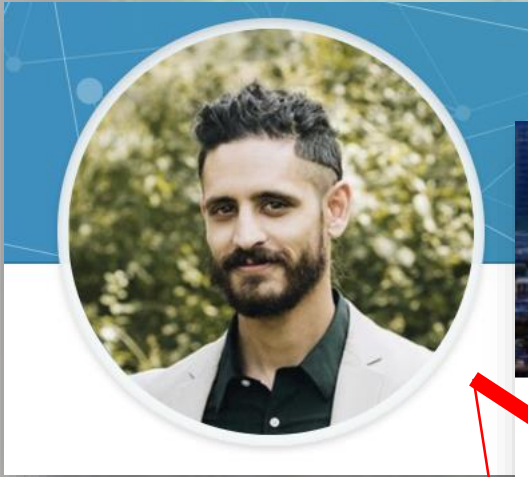


*Pareto Decisions
are Critical for
Health!*





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THANKS!

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