

# Exergy Analysis of a Wood Fireplace Coupled with Thermo-Electric Modules <sup>†</sup>

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**Abstract:** In recent years the climate change issue, coupled with the concern of resource depletion, are favouring the blossoming of renewable energy conversion systems. Particularly, the development of new technologies for the combustion of biomass, have drawn a special attention to the possibility of coupling thermoelectric modules with stove-fireplaces. The current thermoelectric generators have many attractive points, such as a solid structure, absence of noise, and no maintenance required, however, due to their very low efficiency (4–8%), they are still economically non-attractive. However, if the modules are applied to a heat source, which otherwise would be wasted, the interest of the solution certainly grows. In this study an exergy analysis of a stove-fireplace coupled with thermo-electric modules is performed, with the aim of identifying the critical issues of the overall system. The obtained exergy efficiency of the whole system resulted to be of 36.2%. A sensitivity analysis on the main parameters affecting the second law efficiency of the system (such as number of cells, dimension of the stove fireplace, heat input ...) is also carried out.

**Keywords:** thermo-electric modules; stove-fireplace; exergy analysis; thermodynamic

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## 1. Introduction

In the last years, several solutions for the energy management of small micro grids have been developed. Particularly, smart distributed energy systems [1,2] had a widespread diffusion. The necessity of a smart energy system is due to the need of managing not only one energy demand, but numerous, such as electricity, heat and cold. Connected to the diffusion of smart energy system is the concern of environmental pollution and resource depletion, which have favored the blooming of renewable energy.

Among other renewable, biomass fireplaces are extensively used, especially in isolated households, which are not connected to the national natural gas distribution network. In this context, a wood fireplace is used in order to generate the heating, as well as hot sanitary water with the aid of a water storage system.

A further advancement of wood fireplaces could be to use them for the production of not only heat and sanitary water, but also electricity. The conditions to implement thermo-electric (TE) power generation systems to the fireplace seem very appealing. Indeed, the size of the combustions chamber is larger when compared to pellet or wood chip stoves; furthermore, there is a very wide area of the fireplace which operates through radiation heat transfer, allowing a relevant heat flux to the walls of the stove. Furthermore, from the cooling of the TE, sanitary hot water can be generated, increasing therefore the efficiency of the system.

The utilization of TE modules is favored compared to other waste heat energy systems by its low environmental impact, as it avoids all gas emissions [3], thanks to its solid configuration.

Moreover, TE modules can be positioned in parallel, allowing a great flexibility for the configuration of the system. They also require very limited maintenance and do not have any moving parts or involve chemical reactions to convert heat in electricity.

An interesting study which aimed to prove the technical feasibility of coupling TE modules to small cooking ovens was developed by Champier et al. [4]. In this study, the authors developed and experimental campaign, achieving the power production of 6 W, with 4 TE modules. The modules were air-cooled on the cold side, using a large finned heat dissipater.

A successive work by Champier et al. [5] utilized a hot water storage unit to remove the heat from the TE modules, in order to increase the convective heat flux. In this work, the authors developed a full model of heat transmission across the module, including equations describing the electrical characteristic of the TE module, which showed a good agreement with the experiments that they carried out, obtaining a maximum power output of 10 W.

An experimental investigation on an electric oven test bench was carried out by Zheng et al. [6], in order to validate the developed model of TE. In their study, an economic assessment was also carried out, highlighting the possibility of attacking the market with a 5.6 yrs PBP.

Other numerical and experimental studies on domestic woodstoves fitted with TE modules were carried out by Nuwayhid et al. [7,8]. In these studies, they obtained from the first developed prototype a power production of 1W. The power production was connected to the utilization of low-cost Peltier modules, as well as the low temperature difference which they achieved.

A higher power output was obtained by Lertsatitthanakorn [9], applying the TE modules on a biomass cooking stove. The reached power output was of 2.4 W with a temperature difference of 150 °C, which ensured a short PBP (lower than 1 year), especially when compared to batteries supplying the required power instead of the TE modules.

An experimental campaign on the utilization of TE modules to a domestic natural gas water heater was developed by Ding et al. [10]. In their study, the TE modules generated a maximum power of 42.4 W with the maximum flow rate conditions (33 lpm) with a temperature difference of 80 °C.

The possible application of TE modules to stove-fireplaces was assessed by Sornek et al. [11]. They developed an experimental test rig, in which they compared to types of TE modules with 2 different operating  $\Delta T$ . They concluded that the maximum possible power generation would be of 30 W, while achieving an experimental value of 6 W, stating that the solution would not be therefore economically profitable. In a successive work [12] they compared 2 types of TE modules with different cooling systems. The maximum experimental obtained power for the first assessed TE modules was of 18.8 W, corresponding to 41.7% of the nominal power output. The maximum power output obtained by the second type was higher (31.2 W), but with a 31.2% value respect to the nominal power output.

From the literature review, it seems that the majority of the developed works were aimed to demonstrate the practical operation of a thermo electric system integrated with a stove, adding commercial TE modules to existing stoves with minor adjustments. This leads to very low power levels, mainly because of limits determined by the air cooling of the back side of the modules, or of the limited temperature difference and heat flux.

The authors, in a previous study [13], proposed to apply TE modules to a wood fireplace, taking advantage of the high heat flux available in the radiation chamber. It was demonstrated that 7 modules of 20 W could be applied to a 26 kWt fireplace generating therefore a total power output of 140 W. The aim of the current study is to develop an exergy analysis in order to assess the sources of inefficiency of the system. Indeed, it seems that there is still a gap in literature regarding the exergy analysis of wood fireplaces. The main sources of exergy destruction and loss are therefore highlighted in this study.

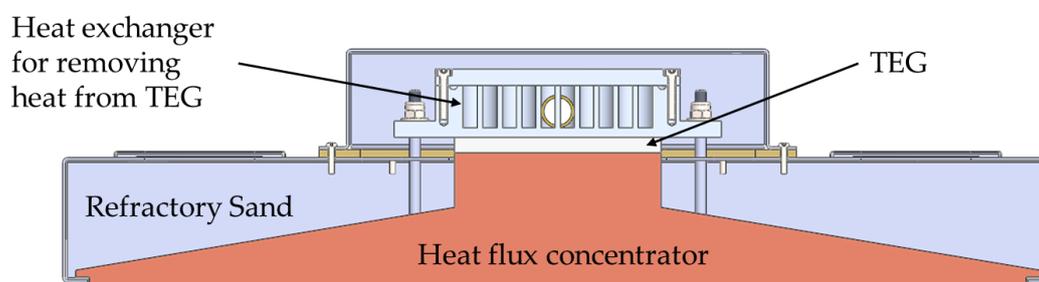
## 2. Materials and Methods

### 2.1. Layout of the Fireplace Unit

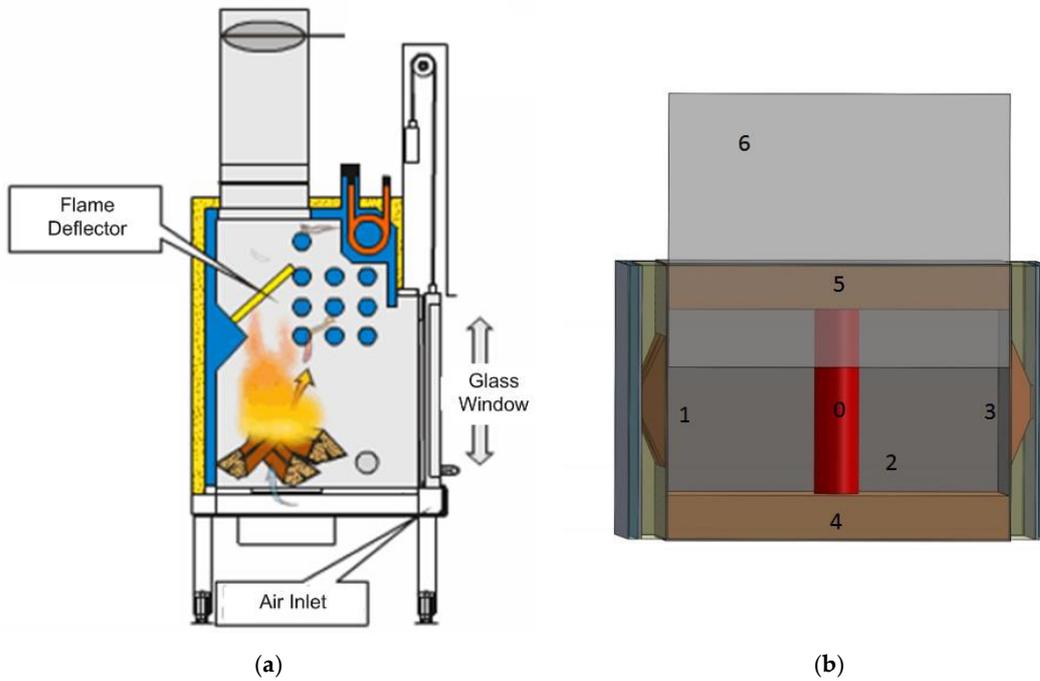
In order to comply with the heating demand of a typical household, a wood fireplace with a maximum power rating of 26 kWt is required. To cover the production of sanitary water, a hot water storage of about 0.4 m<sup>3</sup> is required, which impacts on the dimensions of the fireplace. The water storage is heated through multi-pass fire-tube configurations, which allow to reach typical temperature for sanitary water and heating system in the range of 60–80 °C. Table 1 presents the overall dimensions of the analyzed wood fireplace (Figure 1 for a general schematic), with focus on the combustion chamber. The side and back walls of this last (1, 2, 3) are made by CORTEN steel; the upper and lower sides (4, 5) have a silica-based refractory liner having low emissivity, while front windows to the ambient is made of quartz glass (6). The side and back faces are equipped with TE modules. In order to properly convey the high-flux radiative heat transfer to the TE section, it is necessary to use a Heat Flux Concentrator (HFC). The HFC is made by copper and packaged inside an insulated box, hosting inside also the TE module and the water cooler (for removing heat from the TE), as displayed in Figure 1. The void space between the HFC and the box is filled with fine refractory sand, so that heat is preferably transmitted through the high-conductivity copper thermal bridge. Externally to the HFC box, still air is considered to fill the gap between the CORTEN and the outside ambient. Figure 2 shows the schematic of the wood fireplace with hot water storage and of the combustion chamber with HFC.

**Table 1.** Wood fireplace dimensions.

Dimensions	[m]
Overall Width	1
Overall Depth	0.7
Overall Height	1.6
Combustion Chamber Width	0.78
Combustion Chamber Depth	0.5
Combustion Chamber Height	0.43



**Figure 1.** Schematic of heat flux concentrator box.



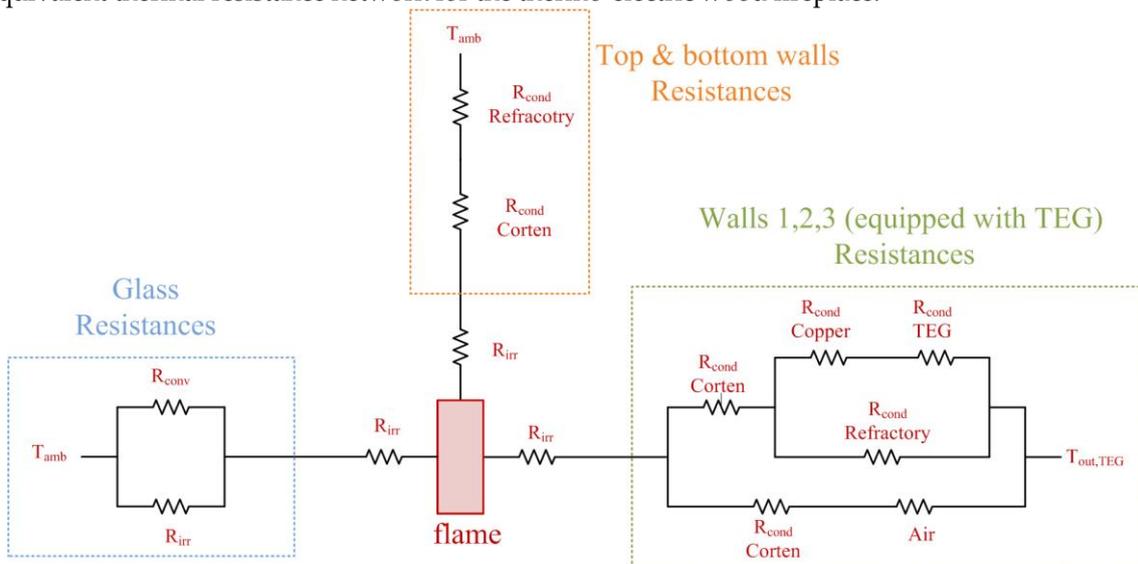
**Figure 2.** Schematic (a) of household fireplace with integrated hot water storage and (b) schematic of combustion chamber with heat flux concentrators.

2.2. Thermodynamic and Exergy Model of the Thermo-Electric Fireplace

The model of the thermo-Electric fireplace [13] was developed through several coupled sections:

1. Radiation model of the combustion chamber
2. Wavelength selectivity of the glass window
3. Heat transfer to thermo-electric modules (in/out)
4. Heat flux concentrator

The fundamental equations are detailed in Appendices A and B. Furthermore, Figure 3 displays the equivalent thermal resistance network for the thermo-electric wood fireplace.



**Figure 3.** Equivalent thermal resistance network for the thermo-electric wood fireplace.

The exergy analysis combines the First and Second Laws of Thermodynamics, allowing the evaluation of the efficiency of the energy system and the irreversibilities (exergy destructions) of the system components [14,15].

Exergy is generally defined as the maximum work obtainable from a system or a process through the interaction with the surrounding environment. Having to deal with heat fluxes, it is convenient to apply a heat - exergy approach. Therefore, the heat-exergy can be determined [16] defining a Carnot factor, which determines the quality of the heat depending on its temperature, as in Equation (1):

$$\dot{E}x_j = \theta_k \cdot \dot{Q}_k = \left(1 - \frac{T_a}{T_k}\right) \cdot \dot{Q}_k \quad (1)$$

Every layer of the system can be described by an exergy balance distinguishing between exergy rates connected with its fuel and product [16], according to the component exergy balance:

$$\dot{E}x_{F,k} = \dot{E}x_{P,k} + \Sigma \dot{E}x_{D,k} + \Sigma \dot{E}x_{L,k} \quad (2)$$

Equation (2) takes into account the exergy destructions and losses, which influence the irreversibility of the system operation. An exergy destruction derives from friction or irreversibility of heat transfer within a defined control volume, while an exergy loss is associated with exergy transfer (waste) to the surroundings. The directly calculated exergy efficiency of a component is defined as the ratio between the product exergy and the fuel exergy. The indirect definition of exergy efficiency requires the evaluation of exergy destructions and losses. The exergy efficiency can be determined by the following Equation (3):

$$\eta_k = \frac{\dot{E}x_{P,k}}{\dot{E}x_{F,k}} = 1 - \frac{\Sigma \dot{E}x_{D,k} + \Sigma \dot{E}x_{L,k}}{\dot{E}x_{F,k}} \quad (3)$$

which can be applied both at each layer and at system level.

In the present case, all the grouped systems (Glass, bottom-and top walls and walls enclosing the TEGs) are producing exergy loss to the environment.

### 3. Results

#### 3.1. Exergy Destruction and Losses of Design Configuration

The exergy performance of the analyzed wood fireplace is of 36.2 % for a heat input of 26.7 kWt. The highest exergy loss is the one connected to the flue gas stream, which lower the temperature from the flame to the ambient, as displayed in Equation (4).

$$ExL_{fg} = Q_{fg} \cdot (1 - \theta_{fg}) = Q_{fg} \cdot \frac{T_{amb}}{T_{fg}} \quad (4)$$

where

$T_{fg}$  is calculated as the logarithmic mean temperature difference between the flame temperature and the ambient temperature.

Indeed, the flue gas exergy loss is the only real one from the system, as the exergy destructions and losses through the walls contribute to heating the housing, which is the real scope of the wood fireplace. However, in this study, the considered products of the system are the flue gases exergy output (which is directly connected to heating the housing) and the power produced by the TE modules, as displayed in Equation (5); while the fuel exergy is considered as the heat input times the Carnot coefficient of the flame, as displayed in Equation (6).

$$Ex_p = Q_{fg} \cdot \theta_{fg} + \dot{W}_{TOT,TE} \quad (5)$$

$$Ex_f = Q_{in} \cdot \theta_0 \quad (6)$$

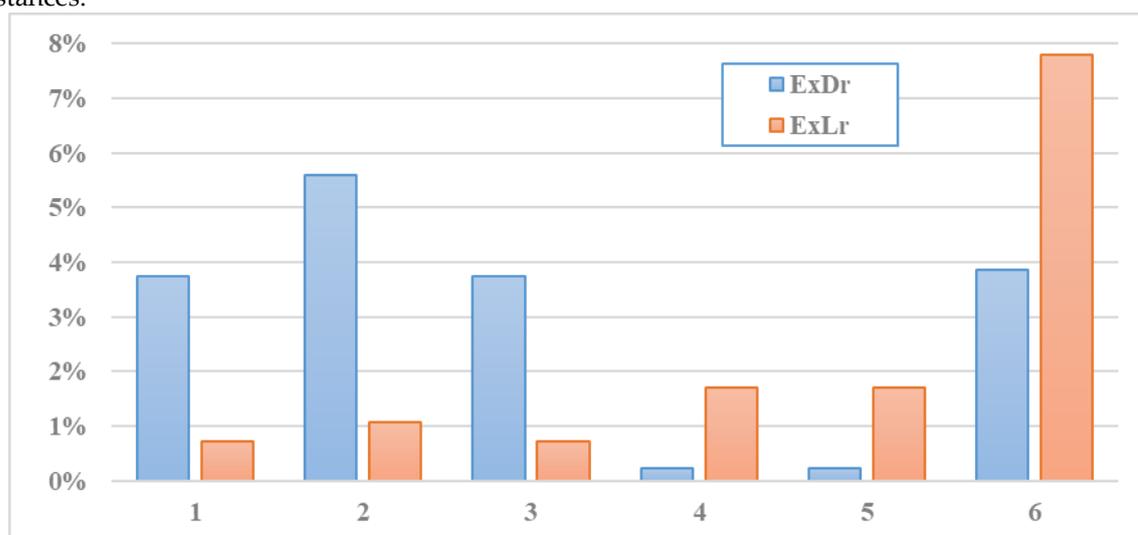
where

$\theta_0$  is calculated as  $1 - \frac{T_{amb}}{T_0}$  and  $T_0$  is the flame temperature.

Therefore, the total exergy input ( $Ex_i$ ) is of 19.6 kWt, while the exergy loss of the flue gases is of 6.4 kWt, which corresponds to 51.2% of the total exergy destruction and losses of the system. The

other main contributor of the losses of the system is the glass window, with a value of 1.53 kWt, which corresponds to 12% of the total exergy destruction and losses of the system.

Figure 4 displays the exergy destruction and losses of the walls of the wood fireplace, adimensionalized respect to the exergy input. Walls 1 and 3 have the same configuration, as they have the same numbers of TE modules (2), on the other hand wall 2 has 3 TE modules, therefore the heat flux is more concentrated in this wall. The walls which comprise TE modules are the ones which contributes more on the exergy destruction and losses. This is due to the higher flux which is channeled through these walls compared to the bottom and top surfaces. Furthermore, the share of the exergy destruction is higher respect to the exergy loss, because of the high number of thermal resistances.



**Figure 4.** Relative Exergy Destruction and Losses of the walls within the combustion chamber.

Figures 5 and 6 display the detailed share of the exergy destruction and losses on walls 1 and 3 and on wall 2. Particularly, it can be noted from a comparison of the figures, that the number of cells slightly influence the exergy destruction and losses share, impacting only marginally on exergy destruction rate of the flame and of the Corten.

Corten has been divided in external and internal. With external it is referred to the one in contact with the still air, while the internal it is the one in contact with the copper. The thickness of the Corten is slightly different for the external and internal configuration (0.037 and 0.033 [m] respectively).

The highest exergy destruction is located in the TE modules, due to the very low conversion efficiency of the modules (electric efficiency is only 3.8%). The second highest contribution is given by the exergy destruction from the flame to the wall, the other contributions are far lower, implying a correct design of the thermal resistances system.

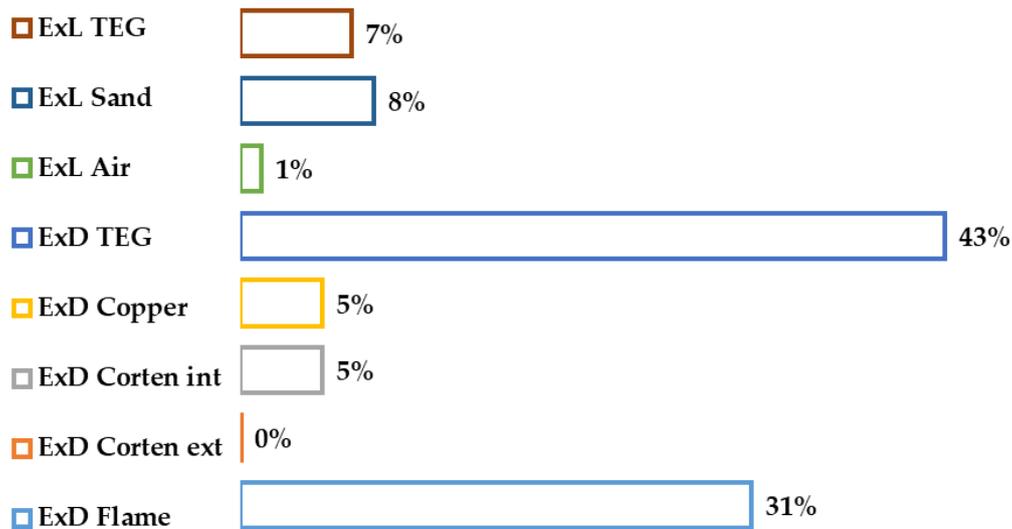


Figure 5. Detailed share of exergy destruction and loss of walls 1 and 3.

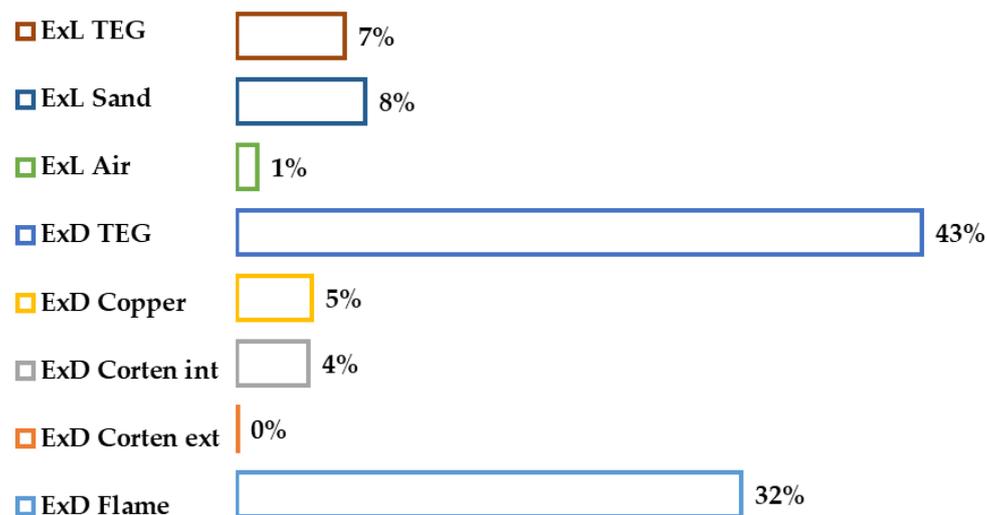


Figure 6. Detailed share of exergy destruction and loss of wall 2.

### 3.2. Sensitivity Analysis of the Main Parameters Affecting the Exergy Efficiency

After the exergy performance of the design case study was assessed, a sensitivity analysis on the main parameters affecting the efficiency of the system has been carried out.

Figure 7 displays the variation of exergy efficiency as function of the heat input. Particularly, the exergy efficiency increases due to the higher flue gases exergy output, which increases linearly with the heat input.

Figure 8 on the other hand shows the variation of exergy efficiency as function of the height of the wood fireplace. This dimensional parameter is the only one affecting the exergy efficiency of the system, as the other length and width of the combustion chamber do not influence the performance of combustion chamber. The increase in height of the wood fireplace allows to increase the area of the walls, therefore more TE modules could be placed, however, this implies that a higher heat flux is located to the walls. As a consequence of the increase heat exchange, the temperature of the flame is colder, decreasing therefore the exergy content of the flue gases. Therefore, the height of the fireplace, allows to increase the numbers of modules, but, on the other hand, it decreases the temperature of the flame and therefore the exergy efficiency of the system.

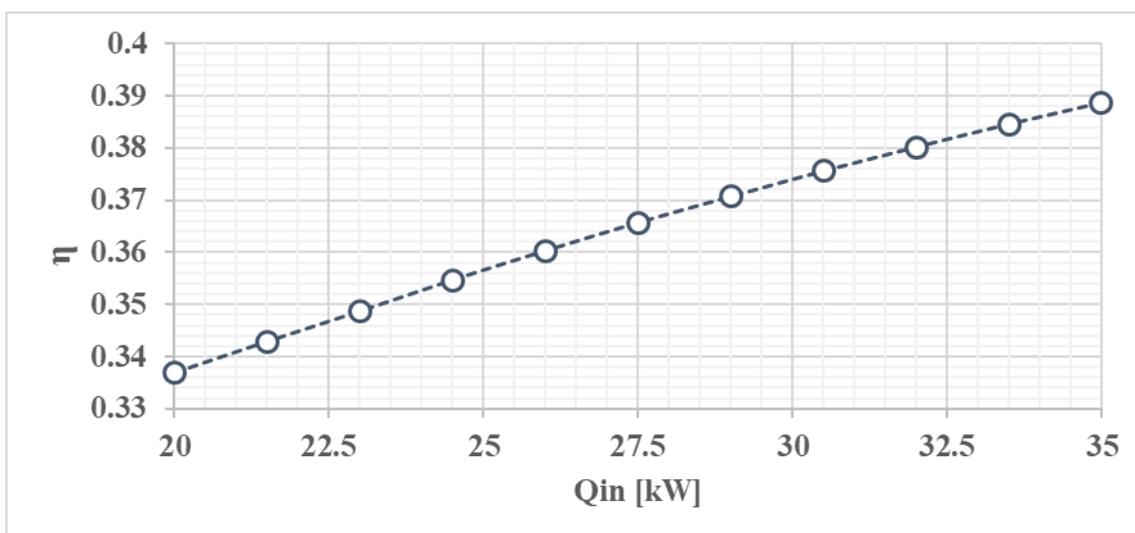


Figure 7. Exergy efficiency of the wood fireplace as function of heat input.

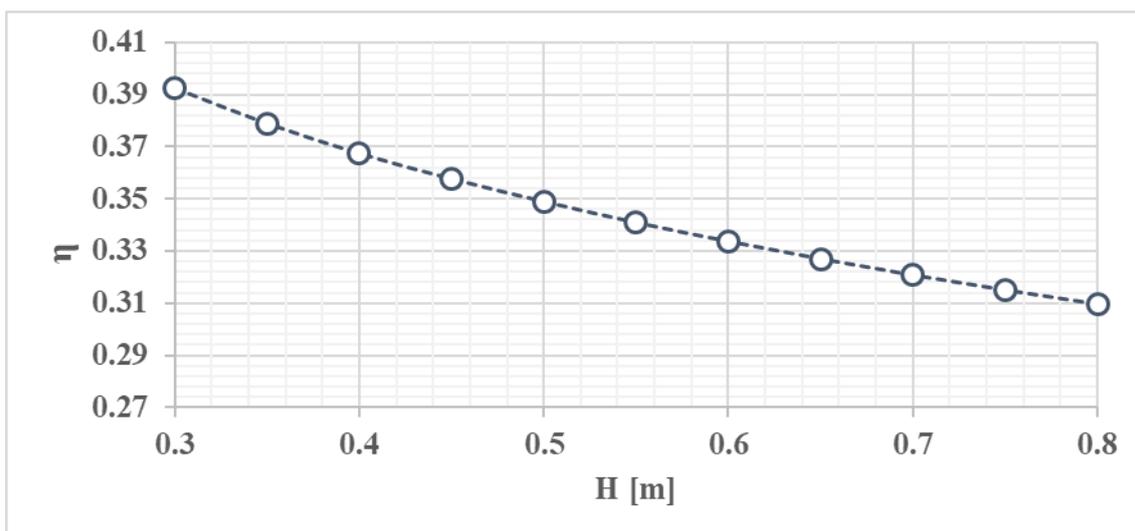


Figure 8. Exergy efficiency of the wood fireplace as function of combustion chamber height.

Table 1 displays the exergy efficiency as function of total number of TE modules. As can be noted from the table, the total number of modules slightly affect the efficiency of the system, as the power output of the cells provides only a 2% of the total exergy output of the system.

Table 1. Exergy efficiency of the wood fireplace as function of total number of TE modules.

# of TE modules	η [%]
6	36.03
7	35.97
8	35.96

#### 4. Discussion and Conclusions

An exergy analysis highlighting the inefficiency sources of an innovative design of a thermo-electric wood fireplace has been carried out. Several components were considered in the analysis, which included in the system boundaries all the elements, from the flame to the ambient. An original

thermal resistance configuration was also assessed, considering a heat flux concentrator which is able to enhance the performance of the TE modules.

The exergy efficiency of the design case study was found to be of 36.2%, with a high contribution of the exergy values of the flue gases. The main sources of inefficiencies were the exergy loss of the flue gases, the exergy destruction and loss of the glass window and the radiative destruction component from the flame to each wall. The TE modules also generated a considerable exergy destruction and loss. A possible solution to this issue could be utilizing more efficient modules (even if the conversion efficiency range of such modules can be only slightly higher), or to utilize the wasted heat from the TE with a water heat exchanger for the production of sanitary water. In this way the exergy efficiency of the system would definitely be higher.

After the exergy performance evaluation of the case study, a sensitivity analysis on the main parameters affecting the second law efficiency of the system was carried out. Particularly, it was found that the exergetic efficiency rises with the increase of heat input, as it allows a rise in the exergy content of the flue gases. Conversely, increasing the height of the fireplace, a reduction of exergy efficiency is produced. This is due to the higher area of the walls, which get a higher heat flux from the flame, which however lower its temperature. A colder flame implies a lower exergy content of the flue gases, reducing thus the exergy efficiency of the system.

Finally, the total number of modules slightly influences the exergy efficiency of the system, as the share of the produced electric power on the total exergy output is only of 2%.

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**Conflicts of Interest:** “The authors declare no conflict of interest.”

## Nomenclature

A	Surface, m <sup>2</sup>
HFC	Heat flux concentrator
TEG	Thermo electric generators
Ex	Exergy, kW
ExD	Exergy destruction, kW
ExL	Exergy loss, kW
h	Heat transfer coefficient, W/(m <sup>2</sup> K)
H	Height of fireplace, m
Lpm	Liters per minute
PBP	Payback period
Q	Heat, kW
$\dot{m}$	Mass flow rate, kg/s
T	Temperature, K
R	Conduction resistance

## Greek symbols

$\alpha$	Absorption coefficient
$\varepsilon$	Emissivity
$\eta$	Exergy Efficiency
$\sigma$	Stefan-Boltzmann constant

## Subscripts and superscripts

Amb	Ambient
Cond	Conduction
Conv	Convection
Ext	External

f	Fuel
fg	Flue gases
In	Inlet
Int	Internal
Irr	Radiation
Out	Outlet
p	Product
r	Relative
0...6	Reference sections of fireplace

### Appendix A. Model of Combustion Chamber

Mullikin’s approach was utilized for the radiation modeling from the flame to the walls and the glass window.

The overall heat radiated from the flame (0) to the walls is:

$$Q_{irr} = \sum_1^6 Q_{irr,0,i} \quad i=1...6 \quad (A1)$$

The heat entering the system is determined by the wood consumption rate of the fireplace:

$$Q_{in} = \dot{m}_w (H_i + \alpha c_{p,a} T_a) \quad (A2)$$

The sensible heat flow exiting the combustion chamber (modelled as a 0-D black box) with the hot combustion gases is given by:

$$Q_u = \dot{m}_w (1 + \alpha) c_{p,g} T_g \quad (A3)$$

The combustion chamber balance can be written as:

$$Q_{in} - Q_{irr} - Q_u = 0 \quad (A4)$$

The flame is conceptually replaced by a cylindrical radiating body (0) ( $D_f = 0.1$  m) with emissivity  $\varepsilon = 0.85$  (corresponding to a typical wood fire). Each radiation heat rate is evaluated separately, considering both radiation from flame to the walls, and radiation among walls at different temperatures considering the geometrical view factors.

$$Q_{irr,i,j} = \sigma S_i V F_{j,i} (\varepsilon_i T_i^4 - \varepsilon_j T_j^4) \quad i, j = 1...6 \quad (A5)$$

$$Q_{irr,0} = \sum_{j=1}^6 Q_{irr,0,j} \quad j = 1...6 \quad (A6)$$

### Appendix B. Heat Transfer to Thermo-Electric Modules

The radiation model allows to calculate the (equivalent average) temperature of each wall, and consequently the heat rate radiated from the flame to the wall. the glass window is treated as a thin isothermal layer, with heat flux conditions set by the external radiation and natural convection (hot vertical plate) heat losses:

$$Q_{irr,0,6} = Q_{gw,a} = \frac{\sigma S_{gw} (T_{gw}^4 - T_j^4)}{1 + \frac{(1-\varepsilon_{gw})}{\varepsilon_{gw}}} + h_{VP} S_{gw} (T_{gw} - T_a) \quad (A7)$$

TE modules can be installed on walls 1,2 and 3, the heat rate balance can be set in the following terms:

$$Q_{irr,0,1} + Q_{irr,0,2} + Q_{irr,0,3} = (n_1 + n_2 + n_3) Q_{in,TE} \quad (A8)$$

On the whole, the TE heat transfer balance is described by the following equations, considering a heat flux concentrator:

$$Q_{in,TE} = \frac{(T_H - T_{CH})}{R_{ov}} \quad (A9)$$

$$R_{ov} = R_{ci} + R_{Cu} + R_c \quad (\text{A10})$$

Each TE module provides a power according to the thermoelectric characteristic of the module:

$$P = 0.0005 \cdot (T_{TE,H} - T_{TE,C}) \cdot 2 = 20 \text{ W} \quad (\text{A11})$$

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