Application of Rényi entropy-based 3D electromagnetic centroids to segmentation of fluorescing objects in tissue sections

Renata Štysová-Rychtáriková et al.

Laboratory of Experimental Complex Systems Institute of Complex Systems Faculty of Fisheries and Protection of Waters University of South Bohemia in České Budějovice



Entropy 2021, 05/05-07/2021

# I. Theoretical assumptions

- Extended Nijboer-Zernike Theory
- Multifractality

## 2. Technical solutions

- Small camera pixel
- Primary vice-bit camera signal
- Short z-step
- Strong light illumination

### **Extended Nijboer-Zernike Theory**





### + Theory of Electromagnetic Centroid Volume electromagnetic centroid:

- intensity extreme
- the same intensity in two consecutive images

Rychtáriková et al., Ultramicroscopy, 2017.







Two consecutive z-stack images

Rychtáriková et al., Entropy, 2018.

#### Multifractality approach: Point Divergence Gain $\Omega_{\alpha}^{(L \to M)}$



Difference of two Rényi entropies:

$$\Omega_{\alpha}^{(L \to M)} = \left[\frac{1}{1-\alpha}\log_2\sum_{i=1}^{j} \left(p_i^{(L \to M)}\right)^{\alpha} - \frac{1}{1-\alpha}\log_2\sum_{i=1}^{j} (p_i)^{\alpha}\right]$$

$$\Omega_{\alpha}^{(L \to M)} = \frac{1}{1-\alpha} \log_2 \left[ \frac{(n_L - 1)^{\alpha} - n_L^{\alpha} + (n_M + 1)^{\alpha} - n_M^{\alpha}}{C_{\alpha}} + 1 \right]$$

Specific case 
$$\alpha = 2$$
 (the Rényi collision entropy)  

$$\begin{aligned}
&\text{Taylor s.} \\
\Omega_2^{(L \to M)} &= \frac{1}{1-\alpha} \log_2 \left[ \frac{2}{c_2} (n_M - n_L + 1) + 1 \right] \stackrel{\downarrow}{\approx} A(n_M - n_L) + B
\end{aligned}$$

i – value of intensity

M- pixel intensity in the first image (I)

L – pixel intensity in the following image (I+1)

j- number of intensities occupied in the image

 $p_i$  – probability of the occurrence of intensity *i* in the image

 $n_i$ - number of the occurrence of intensity *i* in the image  $\alpha$ - the Rényi dimensionless coefficient ( $\alpha \ge 0, \alpha \ne 1$ )  $C_{\alpha} = \sum_{i=1}^{j} n_i^{\alpha}$  - constant for intensity distribution of image (I)

Rychtáriková et al., Entropy, 2018.

#### **Multifractality approach**

Point Divergence Gain Entropy  $I_{\alpha}$ :

$$I_{\alpha}(\mathbf{I}_{a};\mathbf{I}_{b}) = \sum_{i=1}^{n} \left| \Omega_{\alpha}^{a_{i} \to b_{i}} \right| = \sum_{L=1}^{j} \sum_{M=1}^{j} n_{lm} \left| \Omega_{\alpha}^{L \to M} \right|$$

#### **Point Divergence Gain Entropy Density** $P_{\alpha}$ **:**

$$P_{\alpha}(\mathbf{I}_{a};\mathbf{I}_{b}) = \sum_{L=1}^{J} \sum_{M=1}^{J} X_{lm} |\Omega_{\alpha}^{L \to M}| \qquad \begin{array}{c} X_{lm} = \mathbf{1}, \ n_{lm} \ge \mathbf{1} \\ X_{lm} = \mathbf{0}, \ n_{lm} = \mathbf{0} \end{array}$$

 $I_a = \{a_1, ..., a_n\}$  and  $I_b = \{b, ..., b_n\}$  – two consecutive one-dimensional data frames with pixel indices  $a_i$  and  $b_i$ , respectively.  $n_{lm}$  – number of substitutions  $l \rightarrow m$  at transformation  $I_a \rightarrow I_b$ 



### $\Omega_{\alpha}^{(L \to M)}$ in microscopy image processing

#### I.3D segmentation

- Finding "volume electromagnetic centroid"
- Movements detection

#### 2. Image classification

- Finding in-focus region/image

### **Application in fluorescence microscopy**



#### Prostate cancer tissue section

- DAPI, red, and green autofluorescence
  - Pixel size 328×328 nm<sup>2</sup>
    - Wide-field mode



TissueFaxs-PLUS-Confocal fluorescence microscope (TissueGnostics, Vienna, AT)

Rychtáriková et al., Arxiv 1709.03894, 2017.

#### **Outline of calculation**









**PSF**s



RAf









Dalibor Štys, University of South Bohemia, CZ Michael Fischer, Donau University, Krems, AT Gero Kramer, Medical University, Vienna, AT Georg Steiner, TissueGnostics, Vienna, AT

#### ACKNOWLEDGEMENT



fa ImageCode fa Optax

THANK YOU FOR YOUR ATTENTION