



1 Extended Abstract

² Equilibration of polyelectrolyte-surfactant layers at fluid/fluid ³ interfaces: Different Scenarios ⁺

Eduardo Guzmán ^{1,2,*}, Laura Fernández-Peña ³, Irene Abelenda-Núñez ¹, Armando Maestro ⁴, Andrew Akanno ¹,
 Sara Llamas ¹, Francisco Ortega ^{1,2}, Ramón G. Rubio ^{1,2}

| 6 | ¹ Departamento de Química Física, Facultad de Ciencias Químicas, Universidad Complutense de Madrid. |
|----|---|
| 7 | Ciudad Universitaria s/n, 28040-Madrid (Spain) |
| 8 | ² Instituto Pluridisciplinar, Universidad Complutense de Madrid. Paseo Juan XXIII, 28040-Madrid (Spain) |
| 9 | ³ Centro de Espectroscopía y Raman, Universidad Complutense de Madrid. Ciudad Universitaria s/n, 28040- |
| 10 | Madrid (Spain) |
| 11 | ⁴ Donostia International Physics Center. Paseo Manuel de Lardizabal, 4. 20018-San Sebastián (Spain) |
| 12 | * Correspondence: eduardogs@quim.ucm.es |
| 13 | + Presented at the 2 nd International Online Conference on Polymer Science-"Polymer and Nanotechnology for |
| 14 | Industry 4.0", 1-15 November 2021. |
| 15 | Abstract: This work addresses the main physico-chemical aspects related to the formation of |
| 16 | polyelectrolyte-surfactant layers at fluid interfaces, combining a careful examination of the |
| 17 | interfacial properties of the adsorbed films by using a pool of surface-sensitive technique. |
| 18 | Furthermore, the assembly of the mixtures will be correlated to the bulk association processes trying |
| 19 | to provide a comprehensive picture describing the interfacial behavior of polyelectrolyte-surfactant |
| 20 | mixtures at fluid interface. This requires the study of combinations of different polycations |
| 21 | (poly(diallyldimethylammonium chloride) and chitosan) with surfactants bearing different charge |
| 22 | (neutral, anionic and zwitterionic). Thus, it will be possible to obtain a whole perspective of the role |
| 23 | of the association processes on the structure and properties of the interfacial layers. |

Keywords: polyelectrolytes; surfactants; fluid Interfaces; rheology.

| n |
|---|
| ſ |

The interaction of polyelectrolyte-surfactant mixtures with interfaces plays a very important role in many technological fields, including cosmetics, food science or drug delivery [1-3]. This has stimulated the research trying to shed light on the most fundamental aspects governing the adsorption processes of the complexes formed in the bulk, and the equilibration of the interfacial layers. The current knowledge related to the physico-chemistry of polyelectrolyte-surfactant systems has evidenced that, in most of the cases, the association process of polyelectrolyte and surfactant molecules in the bulk is guided by non-equilibrium effects, even though the control of the protocol used for mixing the component allows obtaining reproducible aggregates (kinetically trappedaggregates), with these non-equilibrium effects impacting decisively on their interfacial properties of polyelelectrolyte-surfactant systems [4,5]. Therefore, the understanding of the interfacial processes involving polyelectrolyte-surfactant mixtures makes necessary deepening on the mechanisms underlying the complexation process occurring in the bulk [6-8], i.e. the structural complexity of polyelectrolyte-surfactant mixtures and the richness of their phase behavior, which result from the formation of supramolecular aggregates [9-12].

Despite the large number of studies dealing with the polyelectrolyte – surfactant mixtures, it has not been possible yet to establish a framework enabling for the description of the association of polymers and surfactants in the bulk and at interfaces mainly due to the intricate balance of interactions involved in these systems, which emergence from

| Citation: Guzmán, E.; Fernández- | | | |
|--------------------------------------|----|--|--|
| Peña, L.; Abelenda-Núñez, I.; | | | |
| Maestro, A.; Akanno, A.; Llamas, S.; | | | |
| Ortega, F.; Rubio, R.G | | | |
| Equilibration of polyelectrolyte- | 26 | | |
| surfactant layers at fluid/fluid | 27 | | |
| interfaces: Different Scenarios. | | | |
| Mater. Proc. 2021, 3, x. | | | |
| https://doi.org/10.3390/xxxxx | | | |
| 1 0. | 30 | | |
| Published: date | 31 | | |
| | | | |

 Publisher's
 Note:
 MDPI
 stay³³

 neutral with regard to jurisdictional diams in published maps and sinstitutional affiliations.
 36

32

37

38 39

46



Copyright: © 2021 by the authors 40 Submitted for possible open access upublication under the terms and conditions of the Creative Commons Attribution (CC BY) license (https://creativecommons.org/license s/by/4.0/).

their multicomponent character [7-10,13]. The understanding of the complex physicochemical behavior of polymer-surfactant systems can be probably considered one of the most important challenges of colloidal and interfacial sciences due to its recognized interest in different fields of science and technology.

The main aim of this work is to unravel the different interfacial behavior appearing in polycation-surfactant mixtures. The adsorption at the water/vapor interface is studied by surface tension measurements. In addition to the steady state measurements of the surface tension, we will follow the adsorption kinetics of the complexes at the water/vapor interface by the time evolution of the surface tension (dynamic surface tension) and the mechanical performance of the interfaces against dilation using oscillatory barrier experiments in a Langmuir trough. The obtained results will be combined with the information obtained from the study of the self-assembly phenomena taking place in solution to provide a comprehensive description of the equilibration processes occurring during the formation of interfacial layers in this type of systems.

2. Experimental Section

2.1. Chemicals

PDADMAC with an average molecular weight in the 100-200 kDa range and chitosan (CHI) with an average molecular weight in the 50–190 kDa range and average deacetylation degree in the 75-85 % range were purchased from Sigma-Aldrich (Saint Louis, MO, USA) and used as received. The anionic surfactant SLES (sodium laureth sulfate), with an average number of 2 oxyethylene, was supplied by Kao Chemical Europe S.L. (Barcelona, Spain) as an aqueous solution of 70 wt% of surfactant concentration. SLMT (sodium N-lauroyl-N-methyltaurate) was synthetized and purified following the procedure described in our previous publication [14]. The zwitterionic surfactants CB (coco-betaine) and CAPB (cocoamidopropyl-betaine) were supplied by Clariant International Ltd. (Muttenz, Switzerland) and Solvay S.A. (Brussels, Belgium), respectively. Both carboxybetaines were obtained as aqueous solutions with a surfactant concentration of 31 wt% for CB and 38 wt% for CAPB.

Glacial acetic acid, hydrochloride acid (HCl, aqueous solution at 35 wt%) and sodium hydroxide (NaOH, purity 99%) for fixing the pH, and sodium chloride (NaCl, purity >99.9%) were supplied for Sigma-Aldrich (Saint Louis, MO, USA).

Ultrapure deionized water used for cleaning and solution preparation was obtained by a multicartridge purification system aquaMAXTM-Ultra 370 Series (Young Lin Instrument, Co., Anyang, Korea). The water used had a resistivity higher than 18 M Ω ·cm, and a total organic content lower than 6 ppm.

2.3. Characterization techniques

The binding of the anionic surfactants to the polycation chains was evaluated by potentiometric titration using a surfactant selective electrode model 6.0507.120 from Metrohm AG (Herisau, Switzerland) connected to a pH-meter (model CG842-Schott Instruments Gmbh, Mainz, Germany). The binding degree of surfactant β is estimated from the potentiometric measurements as [15]

$$\beta = \frac{c_s^{bound}}{c_{monomer}},\tag{1}$$

where c_s^{bound} is the concentration of surfactant bound to the polymer chains and $c_{monomer}$ the concentration of charged monomers on the polyelectrolyte chain. The determination of the binding isotherm using surfactant selective electrodes requires firstly to obtain a calibration curve using surfactant solutions in the same concentration range used for the preparation of the polyelectrolyte-surfactant mixtures. For this purpose, the

2

3

4

5

6

7

8

9

10

11

12

13

14

15 16

17

18

19

20

21

22

23

24

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46 47 electromotive force (EMF) of surfactant solutions is recorded, which allows constructing a calibration curve by plotting the recorded EMF against the surfactant concentration. The comparison of the calibration curve with the EMF dependence on the surfactant concentration obtained for polyelectrolyte-surfactant mixtures provides an evaluation of the number of free surfactant molecules remaining in solution when the mixture is analyzing.

The turbidity of the solutions was evaluated from their transmittance at 400 nm obtained using a UV-Visible spectrophotometer (HP-UV 8452). The turbidity of the samples was determined by the optical density at 400 nm ($OD_{400}=[100 - T(\%)]/100$, where T is the transmittance). It is worth mentioning that neither the polyelectrolyte nor the surfactant present any absorption band above 350 nm.

The changes on the surface pressure Π occurring during the adsorption of polyelectrolyte–surfactant aqueous solutions with different surfactant concentrations to the water/vapor interface was followed using a home-made profile analysis tensiometer in pendant drop configuration (for further details see reference [14]). The adsorption at the water/vapor interface was measured until steady state was reached, i.e., changes of surface pressure smaller than 0.1 mN·m⁻¹ during 30 min.

3. Results and discussion

3.1. Polymer-surfactant association in solution

The binding isotherms for the surfactants to the polymer chains deduced from electromotive force (EMF) measurements for the association of SLES and SLMT to PDADMAC chains shown in Figure 1a evidences a high efficiency of PDADMAC for binding anionic surfactant as has been previously reported in the literature [16], with an amount of free surfactant in solution remaining below 10% even for the highest surfactant concentrations. The low concentration of free surfactant in solution allows us to make the assumption that for the interaction of PDADMAC and anionic surfactant, the bulk has approximately zero free-surfactant concentration. On the contrary, when the interaction of chitosan chains with anionic surfactant is concerned (see inset in Figure 1a), the situation changes and even though it occurs from the lowest surfactant concentrations, a very high fraction of the charged monomers remain uncompensated. This appears clear considering that for concentrations close to 2.6×10^{-2} mM, where big aggregates are already detected in the solution, only the 0.2 % of the charged monomers are compensated by SLES binding. Furthermore, the amount of free surfactant at the highest surfactant concentrations remains around the 25 % of the initial surfactant concentration. Therefore, the results suggest that the chitosan-SLES solutions contain both chitosan-SLES complexes and a non-negligible concentration of free SLES molecules [17]. The low binding of the anionic surfactant to the chitosan can be understood considering a strong screening of the electrostatic interactions due to the relatively high ionic strength (100 mM). Furthermore, the strong contribution of the charge screening justify the formation of insoluble complexes for surfactant concentrations far from the corresponding to the saturation of all the charges [18]. Therefore, the interaction of polycation and oppositely charged systems can lead to two different systems: strongly interacting systems (PDADMACanionic surfactant) and weakly interacting systems (chitosan-anionic surfactant). This is clear from the dependence of ratio between the number of free surfactant molecules and the total number of surfactant molecules on the ration between the number of charges monomers and the number of surfactant molecules for mixtures of PDADMAC and chitosan with SLES (see Figure 1b).



Figure 1. (a) Binding isotherms for PDADMAC-SLMT (0) and (0) PDADMAC-SLES complexes (polymer concentration 5 g/L, pH=5.6 and NaCl concentration 40 mM) as function of the initial concentration of surfactant in bulk, c_s . The inset shows the binding isotherm for chitosan-SLES complexes (polymer concentration 2 g/L, pH=4.6 and NaCl concentration 100 mM) as function of the initial concentration of surfactant in bulk, c_s . The lines are guides for the eyes. **(b)** Z ratio dependences of the ratio between the concentration of free SLES molecules remaining in the solution ($c_{s(free)}$) and the total SLES concentration (c_s) for mixtures of SELS with chitosan (0) and PDADMAC (0). Notice that the concentration of NaCl was fixed in 100 mM.

The association of zwitterionic surfactant with polycations cannot be followed by measuring the changes of the EMF. However, turbidity and electrophoretic mobility measurements can provide important insights in the association process when zwitterionic surfactant are involved, where the the presence of anionic and cationic groups in the hydrophilic head of the zwitterionic molecule may modify the aggregation pattern in relation to that what is found in mixtures of polyelectrolytes and surfactant bearing opposite charges. Figure 2 shows the dependences of the electrophoretic mobility and turbidity on the surfactant concentration for the association of PDADMAC with CB and CAPB.

The results from turbidity and electrophoretic mobility measurements did not evidence any signature of complexation between PDADMAC and the zwitterionic surfactants for low surfactant concentrations, with the values of both electrophoretic mobility and turbidity being very close to that what found for PDADMAC solutions. This bulk behavior might be a result of the weak interaction between the species in the solution for the diluted surfactant concentration range. However, the increase of surfactant concentrations leads to a decrease of the electrophoretic mobility from the value corresponding to PDADMAC solutions down to values close to the isoelectric point at the highest surfactant concentrations, which is accompanied by an increase of the turbidity. These results are compatible with the existence of polyelectrolyte–zwitterionic surfactant complexation. Therefore, it may be expected that the surfactant binding occurs through surfactant micelles. This makes possible an effective compensation of the PDADMAC charges, which was hindered at the lowest surfactant concentrations as result of the presence of a positive charge on the polar head of the zwitterionic surfactant.



Figure 2. Surfactant concentration dependences of the electrophoretic mobility for mixtures of PDADMAC with CB (0) and CAPB (0). The line shows the electrophoretic mobility of pure PDADMAC solution. The inset represents the surfactant concentration dependence of the solution turbidity for mixtures of PDADMAC with CB (0) and CAPB (0). The composition of the mixtures is polymer concentration 5 g/L, pH=5.6 and NaCl concentration 40 mM.

3.2. Surface pressure isotherms for polymer-surfactant mixtures

The study of the surfactant concentration dependences of the surface pressure Π of solutions of surface active compounds provides important information on the mechanisms involved in the equilibration of the fluid interface. Figures 3a and 3b shows the surfactant concentration dependences of the surface pressure for mixtures of PDADMAC and the two anionic surfactants. For the sake of comparison, the data corresponding to the pure surfactant are also shown. It should be stressed that PDADMAC alone does not undergo any adsorption at the fluid interface.



Figure 3. Surface pressure dependences on the surfactant concentration: (a) SLMT (\bullet) and PDADMAC – SLMT (0). (b) SLES (\bullet) and PDADMAC – SLES (0) solutions. (c) CB (\bullet) and PDADMAC-CB (0). The inset presents the data for CAPB (0) and PDADMAC-CAPB (\bullet). The composition of the mixtures is polymer concentration 5 g/L, pH=5.6 and NaCl concentration 40 mM.

The adsorption behavior of the anionic surfactant is the typical for surfactant solutions, where Π increases with the bulk concentration up to the surfactant concentration overcomes the threshold defined by the critical micellar concentration (cmc). Afterwards, Π remains constant with further increases of surfactant. On the other

side, the adsorption of PDADMAC-surfactant solutions show that the surface pressure values for pure surfactant and polyelectrolyte-surfactant solutions are similar at the lowest surfactant concentrations due to the low coverage of the interface. The increase of the surfactant concentration leads to the increase of Π for both surfactant and polyelectrolyte-surfactant solutions. This increase starts for surfactant concentrations are onsidered, which is signature of the existence of a synergetic effect for the increase of the surfactant. This type of synergetic effects do not influence the adsorption behavior of solutions formed by PDADMAC and zwitterionic surfactants derived of the betaines, which may be explained by the aforementioned differences in the aggregation process occurring in the bulk (see Figure 3c) [19].

The surface pressure isotherms of both pure surfactant solutions and PDADMACzwitterionic surfactant mixtures present a monotonous increase from the quasi-null value corresponding the bare water/vapor interface up to to values close to 40 mN/m in the vicinity of the cmc of the pure surfactant. The differences of surface tension of the pure surfactant solutions and PDADMAC-surfactant solutions are smaller than the combined error bars both mixtures. This together with the results previously discussed for the bulk properties seems to confirm the absence of real complexation below the cmc of the surfactant. This can be explained considering that the presence of the positive charge within the hydrophilic head of the surfactant introduces an electrostatic barrier which may prevent the complexation process between the carboxylic acid group of the surfactants (pK ~ 2- 4), which is expected to be deprotonated under the pH conditions in the present study (slightly acid, pH ~ 5.5) [20], and the quaternarium ammonium of the PDADMAC.

The scenario is even more complex when the adsorption of mixtures of chitosan and SLES is considered, which may be ascribed to the weak association of chitosan and the anionic surfactant. Furthermore, on the contrary that PDADMAC, chitosan is a surface active polymer under the here considered conditions. Figure 4 shows the surface pressure-surfactant concentration isotherms for the adsorption of pure SLES and chitosan-SLES mixtures at the water/vapor interface.



Figure 2. Surfactant concentration dependences of the surface pressure for SLES (\bullet), chitosan-SLES mixture (polymer concentration 2 g/L, pH=4.6 and NaCl concentration 100 mM) (0) and chitosan-SLES mixtures with the surfactant concentration re-scaled to the free surfactant concentration remaining in solution (polymer concentration 2 g/L, pH=4.6 and NaCl concentration 100 mM) (\triangle). The solid line represents the surface pressure value of a chitosan solution.

The surface pressure of both pure SLES solutions and chitosan-SLES mixtures increases with the surfactant concentration. However, for chitosan-SLES mixtures, the surface pressure appears different to that corresponding to the pure surfactant from the lowest value of the surface tension (chitosan-SLES mixtures present higher values of the surface pressure for the lowest SLES concentrations). This indicates, similarly than in mixtures of PDADMAC and anionic surfactant, the existence of a synergetic effect of chitosan and SLES. However, for a SLES concentration around 5×10^{-3} mM, it was found a crossover between the surface pressure curves corresponding to the mixture and to the pure, which leads to a situation in which the surface pressure of the mixture becomes lower to that of the SLES solution with the same concentration. This unexpected behavior can be explained in terms of that discussed for mixtures of proteins and ionic surfactants [21]. A first regime of adsorption, appearing at the lowest SLES concentration, where higher values of surface pressure are found for chitosan-SLES mixtures with respects to those corresponding to pure SLES solutions. This may be due to the surface activity of bare chitosan at the water/vapor interface, and the synergism of the interaction of the chitosan and SLES on the increase of the surface pressure. Thus, the increase of the surface pressure with the surfactant concentration before the crossover of the surface pressure curves may be due to a co-adsorption of chitosan-complexes and free surfactant molecules, with the concentration of complexes at the interface being reduced at the highest surfactant concentrations. The latter may be explained considering the role of the hydrophobic interactions between the SLES hydrophobic tails, and probably between the SLES hydrophobic tails and the hydrophobic domains of chitosan (deacetylated monomers). This leads to the formation of hydrophilic chitosan-SLES aggregates with a lower surface activity, in agreement with the picture proposed by Petrovic et al. [22] for mixtures similar to that studied in the current work.

The above scenario may be confirmed by the re-scaling the surface pressure isotherm of chitosan-SLES mixtures considering only the concentration of free surfactant remaining in solution as was obtained from the binding isotherm (see Figure 1). The re-scaled surface tension curve for chitosan-SLES mixtures tends to overlap with the surface tension isotherm obtained for SLES solutions at the highest surfactant concentrations. Thus, according to the above description three different regions can be differentiated in the adsorption isotherm: (i) in absence SLES, chitosan is adsorbed at the interface leading to a surface pressure higher than that expected for the bare fluid interface (ii) at the lowest SLES concentrations ($<5x10^{-3}$ mM), chitosan and SLES are co-adsorbed at the interface and the surface pressure is higher than that corresponding to SLES solutions, and (iii) at the highest SLES concentration ($> 5x10^{-3}$ mM), the amount of chitosan at the interface is relatively low, and the behavior of the monolayer is reminiscent from that corresponding to pure SLES layer. This leads to a situation in which the interfacial behavior is governed by the concentration of SLES free in solution, and the surface pressure is slightly lower than the corresponding to SLES solutions with the same concentration.

4. Conclusions

The adsorption of mixtures formed by polycations and surfactants at the water vapor/interface results in a complex picture which depends on both the chemical nature of the polymer and the surfactant. This results from the differences on the association mechanism in the bulk that leads to the existence of different species in the solution. These species present different affinity for the interface, with their preferential segregation at the fluid interface determining their equilibration.

Author Contributions: Conceptualization, R.G.R. and E.G.; methodology, E.G., L.F.P., I.A.N. and L.F.P.; software, E.G.; validation, F.O., R.G.R. and E.G.; formal analysis, L.F.P. and I.A.N.; investigation, E.G., L.F.P., I.A.N., A.M. F.O. and R.G.R.; resources, E.G., F.O. and R.G.R.; data curation, E.G.; writing—original draft preparation, E.G.; writing—review and editing, E.G., L.F.P., I.A.N., A.M. F.O. and R.G.R.; visualization, E.G.; supervision, R.G.R. and E.G.; project

- administration, E.G., F.O and R.G.R.; funding acquisition, F.O., R.G.R. and E.G. All authors have read and agreed to the published version of the manuscript. **Funding:** This work was funded in part by MICINN (Spain) under grant PID2019-106557GB-C21,
 - by Banco Santander-Universidad Complutense grant PR87/19-22513 (Spain) and by E.U. on the framework of the European Innovative Training Network-Marie Sklodowska-Curie Action NanoPaint (grant agreement 955612).
 - Institutional Review Board Statement: Not applicable
 - Informed Consent Statement: Not applicable.
 - Data Availability Statement: Data are available upon request.
 - **Acknowledgments:** Authors acknowledge to the Centro de Espectroscopía y Correlación (UCM) for the use of their facilities.
- 12Conflicts of Interest: The authors declare no conflict of interest. The funders had no role in the13design of the study; in the collection, analyses, or interpretation of data; in the writing of the14manuscript, or in the decision to publish the results.

15 **References**

1

2

3

4

5

8

9

10 11

- Llamas, S.; Guzmán, E.; Ortega, F.; Baghdadli, N.; Cazeneuve, C.; Rubio, R.G.; Luengo, G.S. Adsorption of polyelectrolytes and polyelectrolytes-surfactant mixtures at surfaces: a physico-chemical approach to a cosmetic challenge. *Adv. Colloid Interface Sci.* 2015, 222, 461-487, doi:10.1016/j.cis.2014.05.007.
- Fernández-Peña, L.; Guzmán, E. Physicochemical Aspects of the Performance of Hair-Conditioning Formulations. *Cosmetics* 2020, 7, 26, doi:10.3390/cosmetics7020026.
- Lindman, B.; Antunes, F.; Aidarova, S.; Miguel, M.; Nylander, T. Polyelectrolyte-surfactant association from fundamentals to applications. *Colloid J.* 2014, *76*, 585-594, doi:10.1134/S1061933X14050111.
- Guzmán, E.; Fernández-Peña, L.; Ortega, F.; Rubio, R.G. Equilibrium and kinetically trapped aggregates in polyelectrolyte–
 oppositely charged surfactant mixtures. *Curr. Opin. Colloid Interface Sci.* 2020, 48, 91-108, doi:10.1016/j.cocis.2020.04.002.
- Varga, I.; Campbell, R.A. General Physical Description of the Behavior of Oppositely Charged Polyelectrolyte/Surfactant
 Mixtures at the Air/Water Interface. *Langmuir* 2017, 33, 5915-5924, doi:10.1021/acs.langmuir.7b01288.
- Varga, I.; Campbell, R.A. General Physical Description of the Behavior of Oppositely Charged Polyelectrolyte/Surfactant Mixtures at the Air/Water Interface. *Langmuir* 2017, 33, 5915-5924, doi: 5910.1021/acs.langmuir.5917b01288.
- Guzmán, E.; Llamas, S.; Maestro, A.; Fernández-Peña, L.; Akanno, A.; Miller, R.; Ortega, F.; Rubio, R.G. Polymer-surfactant
 systems in bulk and at fluid interfaces. *Adv. Colloid Interface Sci.* 2016, 233, 38-64, doi:10.1016/j.cis.2015.11.001.
- Gradzielski, M.; Hoffmann, I. Polyelectrolyte-surfactant complexes (PESCs) composed of oppositely charged components. *Curr. Opin. Colloid Interface Sci.* 2018, 35, 124-141, doi:10.1016/j.cocis.2018.01.017.
- Bain, C.D.; Claesson, P.M.; Langevin, D.; Meszaros, R.; Nylander, T.; Stubenrauch, C.; Titmuss, S.; Klitzing, R.v. Complexes of surfactants with oppositely charged polymers at surfaces and in bulk. *Adv. Colloid Interface Sci.* 2010, 155, 32–49, doi:10.1016/j.cis.2010.01.007.
- Nylander, T.; Samoshina, Y.; Lindman, B. Formation of polyelectrolyte–surfactant complexes on surfaces. *Adv. Colloid Interface Sci.* 2006, 123–126, 105-123, doi::10.1016/j.cis.2010.01.004.
- Thalberg, K.; Lindman, B. Polymer-surfactant interactions recent developments. In *Interactions of Surfactants with Polymers and Proteins*, Goddard, E.D., Ananthapadmanabhan, K.P., Eds. CRC Press: Boca Raton, FL, USA, 1993.
- Miyake, M. Recent progress of the charaterization of oppositely charged polymer/surfactant complex in dilution deposition
 system. *Adv. Colloid Interface Sci.* 2017, 239, 146-157, doi:10.1016/j.cis.2016.04.007.
- 42 13. Goddard, E.D. Polymer/Surfactant Interaction: Interfacial Aspects. J. Colloid Interface Sci. 2002, 256, 228-235,
 43 doi:10.1006/jcis.2001.8066.
- Llamas, S.; Fernández-Peña, L.; Akanno, A.; Guzmán, E.; Ortega, V.; Ortega, F.; Csaky, A.G.; Campbell, R.A.; Rubio, R.G.
 Towards understanding the behavior of polyelectrolyte–surfactant mixtures at the water/vapor interface closer to
 technologically-relevant conditions. *Phys. Chem. Chem. Phys.* 2018, 20, 1395-1407, doi:10.1039/c7cp05528e.
- Mezei, A.; Mezaros, R. Novel Method for the Estimation of the Binding Isotherms of Ionic Surfactants on Oppositely Charged
 Polyelectrolytes. *Langmuir* 2006, 22, 7148-7151, doi:10.1021/la0612670.
- Campbell, R.A.; Angus-Smyth, A.; Yanez-Arteta, M.; Tonigold, K.; Nylander, T.; Varga, I. New Perspective on the Cliff Edge
 Peak in the Surface Tension of Oppositely Charged Polyelectrolyte/Surfactant Mixtures *J. Phys. Chem. Lett.* 2010, *1*, 3021-3026,
 doi:10.1021/jz101179f.
- Hernández-Rivas, M.; Guzmán, E.; Fernández-Peña, L.; Akanno, A.; Greaves, A.; Léonforte, F.; Ortega, F.; G. Rubio, R.; Luengo,
 G.S. Deposition of Synthetic and Bio-Based Polycations onto Negatively Charged Solid Surfaces: Effect of the Polymer
 Cationicity, Ionic Strength, and the Addition of an Anionic Surfactant. *Colloids and Interfaces* 2020, *4*, 33,
 doi:10.3390/colloids4030033.

- Chiappisi, L.; Hoffmann, I.; Gradzielski, M. Complexes of oppositely charged polyelectrolytes and surfactants recent developments in the field of biologically derived polyelectrolytes. *Soft Matter* 2013, *9*, 3896–3909, doi:10.1039/c3sm27698h.
- Akanno, A. Bulk and Surface Properties of Polyelectrolyte Surfactant Mixtures. Universidad Complutense de Madrid, Madrid,
 2018.
- 5 20. Laschewsky, A. Structures and Synthesis of Zwitterionic Polymers. Polymers 2014, 6, 1544-1601, doi:10.3390/polym6051544.
- Kotsmar, C.; Pradines, V.; Alahverdjieva, V.S.; Aksenenko, E.V.; Fainerman, V.B.; Kovalchuk, V.I.; Krägel, J.; Leser, M.E.;
 Noskov, B.A.; Miller, R. Thermodynamics, adsorption kinetics and rheology of mixed protein–surfactant interfacial layers. *Adv. Colloid Interface Sci.* 2009, 150, 41-54, doi:10.1016/j.cis.2009.05.002.
- 9 22. Petrović, L.; Milinković, J.; Fraj, J.; Bučko, S.; Katona, J.; Spasojević, L. Study of interaction between chitosan and sodium lauryl
- 10 ether sulfate. *Colloid Polym. Sci.* **2017**, 295, 2279-2285, doi:10.1007/s00396-017-4205-7.
- 11