

# Cold Dark Matter and Leptogenesis in the $SE_6SSM$

Roman Nevzorov  
(Lebedev Physical Inst.)

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# Outline

1.  $U(1)_N$  extension of the MSSM
2.  $SE_6SSM$
3. Leptogenesis
4. Dark matter-nucleon scattering cross-section
5. Conclusions

Based on:

R. Nevzorov, On the Suppression of the Dark Matter-Nucleon Scattering Cross Section in the  $SE_6SSM$ , Symmetry **14** (2022) no.10, 2090 [arXiv:2209.00505 [hep-ph]].

R. Nevzorov, Leptogenesis as an origin of hot dark matter and baryon asymmetry in the  $E_6$  inspired SUSY models, Phys. Lett. B **779** (2018) 223.

# $U(1)_N$ extension of the MSSM

- At very high energies  $E_6$  group can be broken to  $SO(10) \times U(1)_\psi$  with sequential breakdown of  $SO(10)$  to  $SU(5) \times U(1)_\chi$  and  $SU(5)$  to the SM gauge group  $SU(3)_C \times SU(2)_W \times U(1)_Y$ .
- Near the GUT scale  $U(1)_\psi \times U(1)_\chi$  symmetry can be broken to  $U(1)_N \times Z_2^M$ , where  $Z_2^M = (-1)^{3(B-L)}$  is a matter parity while  $B$  and  $L$  are baryon and lepton numbers.
- Only in this  $E_6$  inspired  $U(1)_N$  extension of the MSSM ( $E_6$ SSM) right-handed neutrinos  $N_i$  can be superheavy [S.F.King, S.Moretti, RN, Phys. Rev. D 73 (2006) 035009; Phys. Lett. B 634 (2006) 278].
- To ensure anomaly cancellation the particle content of the  $E_6$ SSM is extended to include three complete  $27_i$  representations of  $E_6$ .
- Thus the  $E_6$ SSM contains **extra exotic matter** beyond the MSSM:
  - SM singlet superfields  $S_i$  that carry non-zero  $U(1)_N$  charge;
  - $H_i^d$  and  $H_i^u$  that have quantum numbers of the MSSM Higgs doublets;
  - the exotic quarks ( $\bar{D}_i$  and  $D_i$ ) which are either diquarks or leptoquarks.

- Extra exotic matter may give rise to non-diagonal flavor transitions and rapid proton decay.
- In the modification of the E<sub>6</sub>SSM (SE<sub>6</sub>SSM) a single discrete  $\tilde{Z}_2^H$  symmetry forbids flavor-changing transitions as well as the most dangerous baryon and lepton number violating operators.
  - The SE<sub>6</sub>SSM implies that below the GUT scale  $M_X$  three complete 27-plets are accompanied by lepton doublets  $L_4$  and  $\bar{L}_4$ , a pair of superfields  $S$  and  $\bar{S}$  as well as four  $E_6$  singlet superfields ( $\phi$  and  $\phi_i$ ).
  - The supermultiplets  $\phi$ ,  $S$ ,  $\bar{S}$ ,  $L_4$ ,  $\bar{L}_4$  as well as  $SU(2)_W$  doublets  $H_d \equiv H_3^d$  and  $H_u \equiv H_3^u$  are required to be even under the  $\tilde{Z}_2^H$  symmetry whereas all other supermultiplets are odd [R. Nevzorov, Phys. Rev. D 87 (2013) 015029; P. Athron, M. Mühlleitner, R. Nevzorov, A.G. Williams, JHEP 1501 (2015) 153.].
- The presence of  $L_4$  and  $\bar{L}_4$  at low energies allows the lightest exotic colored state to decay before BBN and facilitates the unification of gauge couplings.

- In the  $SE_6SSM$  the sector responsible for the breakdown of the gauge symmetry is formed by the scalar components of  $\phi$ ,  $S$ ,  $\bar{S}$ ,  $H_d$  and  $H_u$ .
  - $S$  and  $\bar{S}$  can develop large vacuum expectation values (VEVs) along the D-flat direction breaking the  $U(1)_N$  symmetry and generating masses of all exotic fermions and  $Z'$  boson.
- The conservation of  $Z_2^M$  and  $\tilde{Z}_2^H$  symmetries implies that  $R$ -parity and  $Z_2^E$  symmetry are also conserved where  $\tilde{Z}_2^H = Z_2^M \times Z_2^E$ .
- Here we focus on the scenarios in which **gravitino** is the lightest  $R$ -parity odd state so that it is stable and contributes to the density of dark matter.
- In this case the lightest exotic state, which is odd under the  $Z_2^E$  symmetry, has to be stable as well.
- We assume that the lightest stable exotic state is predominantly formed by the fermion components of  $H_1^d$  and  $H_1^u$ .
- In order to find a viable scenarios with stable gravitino one needs to ensure that the lightest unstable  $R$ -parity odd (or exotic) state  $Y$  decays before BBN, i.e. its lifetime  $\tau_Y \lesssim 1 \text{ sec}$ .

- For  $m_\gamma \simeq 1 \text{ TeV}$  one can get  $\tau_\gamma \lesssim 1 \text{ sec}$  if gravitino mass  $m_{3/2} \lesssim 1 \text{ GeV}$ .
- When gravitinos originate from scattering of particles in the thermal bath their contribution to the dark matter density is proportional to the reheating temperature  $T_R$

$$\Omega_{3/2} h^2 \sim 0.27 \left( \frac{T_R}{10^8 \text{ GeV}} \right) \left( \frac{1 \text{ GeV}}{m_{3/2}} \right) \left( \frac{M_{\tilde{g}}}{1 \text{ TeV}} \right)^2 .$$

- Since  $\Omega_{3/2} h^2 \leq 0.12$  for  $m_{3/2} \simeq 1 \text{ GeV}$  and gluino mass  $M_{\tilde{g}} \gtrsim 3 \text{ TeV}$  one finds an upper bound  $T_R \lesssim 10^{6-7} \text{ GeV}$ .
- Even for so low reheating temperatures the appropriate amount of the lepton asymmetry can be induced within the SE<sub>6</sub>SSM via the decays of the lightest right-handed neutrino/sneutrino ( $N_1 / \tilde{N}_1$ ).
- Due to **sphaleron interactions** the generated lepton asymmetry is converted into the baryon asymmetry.

# Leptogenesis

- The interactions of the superfields  $N_i$  are described by

$$W_N = \frac{1}{2} M_i N_i N_i + \tilde{h}_{ij} N_i (H_u L_j) + h_{i\alpha} N_i (H_\alpha^\mu L_4).$$

- After inflation the lightest right-handed neutrino/sneutrino ( $N_1 / \tilde{N}_1$ ) with mass  $M_1$  may be produced by thermal scattering if  $T_R > M_1$ .
- To guarantee that leptogenesis takes place we set  $M_1 \simeq 10^5 \text{ GeV}$ .
- We also assume that  $M_{2,3} \lesssim 10^6 \text{ GeV}$ .
- In order to reproduce the left-handed neutrino mass scale  $m_\nu \lesssim 0.1 \text{ eV}$  the couplings of ordinary leptons  $L_j$  to  $N_i$  should be rather small, i.e.  $|\tilde{h}_{ij}|^2 \ll 10^{-8}$ , and can be ignored.
- Then the lepton asymmetry can be generated via the decays  
 $N_1 \rightarrow L_4 + H_\alpha^\mu$ ,  $N_1 \rightarrow \tilde{L}_4 + \tilde{H}_\alpha^\mu$ ,  $\tilde{N}_1^* \rightarrow L_4 + \tilde{H}_\alpha^\mu$ ,  $\tilde{N}_1 \rightarrow \tilde{L}_4 + H_\alpha^\mu$ .
- This process is controlled by the set of CP asymmetries

$$\varepsilon_{1, l_4}^\alpha = \varepsilon_{1, \tilde{l}_4}^\alpha = \varepsilon_{\tilde{1}, l_4}^\alpha = \varepsilon_{\tilde{1}, \tilde{l}_4}^\alpha = \frac{\Gamma_{N_1 l_4}^\alpha - \Gamma_{N_1 \tilde{l}_4}^\alpha}{\sum_\beta \left( \Gamma_{N_1 l_4}^\beta + \Gamma_{N_1 \tilde{l}_4}^\beta \right)}.$$

- $H_\alpha^\mu$  can be redefined so that only  $H_1^\mu$  interacts with  $L_4$  and  $N_1$  so that  $h_{12}$  may be set to zero and  $\varepsilon_{1, l_4}^2 = \varepsilon_{1, \tilde{l}_4}^2 = \varepsilon_{\tilde{1}, l_4}^2 = \varepsilon_{\tilde{1}, \tilde{l}_4}^2 = 0$ .

- Assuming that the sparticle mass scale  $M_5$  is negligibly small as compared with  $M_1$ ,  $h_{j1} = |h_{j1}|e^{i\varphi_{j1}}$  and  $M_j$  are real one finds

$$\varepsilon_{1, l_4}^1 = \varepsilon_{1, \tilde{l}_4}^1 = \varepsilon_{\tilde{1}, l_4}^1 = \varepsilon_{\tilde{1}, \tilde{l}_4}^1 = \varepsilon = \frac{1}{8\pi} \left[ \sum_{j=2,3} |h_{j1}|^2 f \left( \frac{M_j^2}{M_1^2} \right) \sin 2\Delta\varphi_{j1} \right]$$

$$\Delta\varphi_{j1} = \varphi_{j1} - \varphi_{11}, \quad f(z) = \frac{2\sqrt{z}}{1-z} - \sqrt{z} \ln \left( \frac{1+z}{z} \right).$$

- For  $h_{31} = 0$  and  $h_{21} = 0.1$  one can obtain  $\varepsilon \simeq 0.01$  if  $M_2 \approx M_1$ .
- The induced baryon asymmetry can be estimated as follows

$$Y_{\Delta B} \sim 10^{-3} (\varepsilon \cdot \eta), \quad Y_{\Delta B} = \left. \frac{n_B - n_{\bar{B}}}{s} \right|_0 = (8.75 \pm 0.23) \times 10^{-11}.$$

- In the strong washout scenario the efficiency factor  $\eta$  is given by

$$\eta \simeq \frac{H(T = M_1)}{\Gamma_1}, \quad H = 1.66 g_*^{1/2} \frac{T^2}{M_P}, \quad \Gamma_1 = \frac{|h_{11}|^2}{8\pi} M_1.$$

- For  $\varepsilon \simeq 0.01$  the observed  $Y_{\Delta B}$  can be reproduced if  $|h_{11}| \sim 0.001$ .

# Dark matter-nucleon scattering cross section

- The scalar components of  $\phi_i$ ,  $S_i$ ,  $H_\alpha^u$  and  $H_\alpha^d$  do not acquire VEVs.
- Their fermion components form the exotic (inert) neutralino and chargino states.
- When the components of  $\phi_i$  are very heavy the interactions of  $S_i$ ,  $H_\alpha^u$  and  $H_\alpha^d$  are described by

$$W_{IH} \simeq -\tilde{\mu}_i S_i S_i + \lambda_{\alpha\alpha} S(H_\alpha^d H_\alpha^u) + \tilde{f}_{i\alpha} S_i(H_\alpha^d H_u) + f_{i\alpha} S_i(H_d H_\alpha^u).$$

- Here we assume that  $H_1^d$  and  $H_1^u$  mostly interact with  $S_1$ ,  $H_u$  and  $H_d$ , whereas all other couplings of  $H_1^u$  and  $H_1^d$  are very small.
- The mass of the lightest exotic chargino is determined by  $\mu_{11} = \lambda_{11} \langle S \rangle$ , i.e.  $m_{\chi_1^\pm} = |\mu_{11}|$ .
- If  $|\tilde{\mu}_1|$  is considerably larger than  $|\mu_{11}|$ ,  $\langle H_d \rangle = v_1$  and  $\langle H_u \rangle = v_2$  the mass of the lightest exotic state  $\chi_1$  is given by

$$m_{\chi_1} \simeq m_{\chi_1^\pm} - \Delta_1, \quad \Delta_1 \simeq \frac{(\tilde{f}_{11} v_2 + f_{11} v_1)^2}{2(\tilde{\mu}_1 - m_{\chi_1^\pm})}.$$

- The contribution of  $\chi_1$  to the dark matter density can be estimated as

$$\Omega_{\tilde{H}} h^2 \simeq 0.1 \left( \frac{\mu_{11}}{1 \text{ TeV}} \right)^2.$$

- Thus in the phenomenologically viable scenarios  $\mu_{11} < 1.1 \text{ TeV}$ .
- Since the couplings of gravitino to the SM particles are negligibly small, the interactions of the dark matter with the baryons are determined by the couplings of  $\chi_1$ .

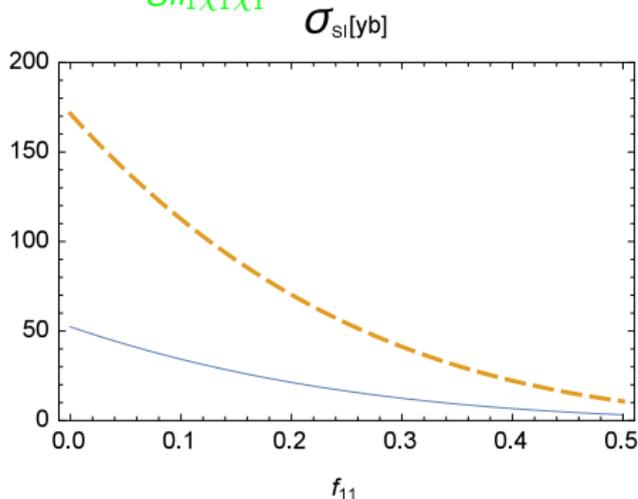
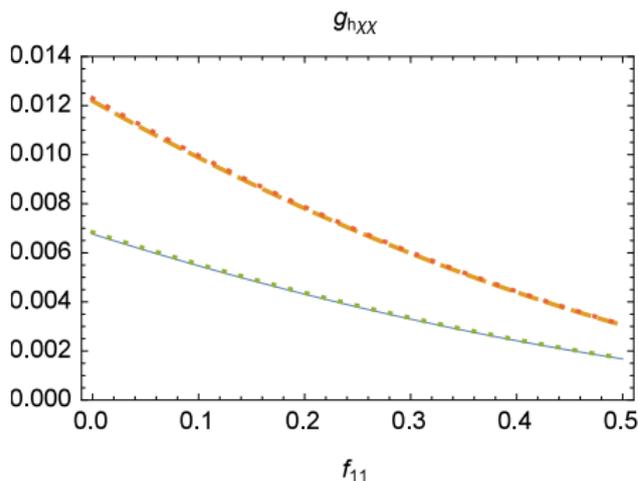
- The dominant contribution to the spin-independent (SI) dark matter-nucleon scattering cross section  $\sigma_{SI}$  comes from the t-channel exchange of the lightest CP-even Higgs boson  $h_1$  with mass  $m_{h_1}$

$$\sigma_{SI} = \frac{2m_r^2 m_N^2}{\pi v^2 m_{h_1}^4} |g_{h_1 \chi_1 \chi_1} F^N|^2, \quad F^N = \sum_{q=u,d,s} f_{Tq}^N + \frac{2}{27} \sum_{Q=c,b,t} f_{TQ}^N,$$

$$m_r = \frac{m_{\chi_1} m_N}{m_{\chi_1} + m_N}, \quad m_N f_{Tq}^N = \langle N | m_q \bar{q} q | N \rangle, \quad f_{TQ}^N = 1 - \sum_{q=u,d,s} f_{Tq}^N.$$

- Here  $v = \sqrt{v_1^2 + v_2^2} \simeq 174 \text{ GeV}$ ,  $g_{h_1 \chi_1 \chi_1} \simeq \Delta_1 / (\sqrt{2} v)$  and hadronic matrix elements  $f_{Ts}^N \simeq 0.0447$ ,  $f_{Td}^N \simeq 0.0191$  and  $f_{Tu}^N \simeq 0.0153$ .

- We set  $\tilde{f}_{11} = -0.5$ ,  $\tan \beta = \frac{v_2}{v_1} = 2$  and  $\tilde{\mu}_1 = 2 \text{ TeV}$ .
- The values of  $\sigma_{SI}$  remain smaller than **60 yb** for  $m_{\chi_1} \simeq \mu_{11} = 200 \text{ GeV}$  (solid lines) and **300 yb** for  $m_{\chi_1} \simeq \mu_{11} = 1 \text{ TeV}$  (dashed lines) which are the values of the experimental bounds on  $\sigma_{SI}$  obtained by the LZ experiment [J. Aalbers, et al. [LUX-ZEPLIN Collaboration], arXiv:2207.03764].
- The suppression of  $\sigma_{SI}$  is caused by large  $\tilde{\mu}_1$  as well as by the partial cancellation of different contributions to  $g_{h\chi_1\chi_1}$ .



# Conclusions

- We explored the  $SE_6SSM$  scenarios in which cold dark matter density is formed by the gravitino and the lightest exotic neutralino  $\chi_1$ .
- The phenomenological viability of these scenarios implies that the gravitino mass  $m_{3/2}$  should be smaller than 1 GeV and the reheating temperatures  $T_R$  has to be lower than  $10^6$  GeV.
- Even for so low  $T_R$  the decays of the lightest right-handed neutrino/sneutrino can induce the observed baryon asymmetry.
- In the scenarios under consideration there is a part of the  $SE_6SSM$  parameter space in which the dark matter–nucleon scattering cross section is substantially smaller than the present experimental limits.
- In these scenarios the lightest exotic chargino  $\chi_1^\pm$  as well as the lightest exotic neutralino states  $\chi_2$  and  $\chi_1$  are nearly degenerate and have masses below 1.1 TeV.
- Since the mass splitting between these states is very small the decay products of  $\chi_2$  and  $\chi_1^\pm$  are too soft so that they escape detection.