Proceeding Paper

A monthly Water Balance Model for Assessing Streamflow Uncertainty in Hydrologic Studies †

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Abstract: Accurate assessment of streamflow is crucial for operational water resources management projects. The aim of this study was to estimate the uncertainties in the surface runoff simulated by a monthly water balance model in a mountainous watershed of the Portaikos river, a tributary of the Pinios river, Thessaly, Greece. The University of Thessaly (UTHBAL) monthly water balance model was developed in the R statistical computing environment language, named 'R-UTHBAL', to estimate surface water balance in data-scarce watersheds. Two sources of uncertainties in hydrological modelling were considered: the uncertainties in input data estimation and in model parameters. The uncertainties were estimated with the use of the R-package '*hydroPSO*', a global Particle Swarm Optimisation (PSO) algorithm for the calibration of environmental models. The R-UTHBAL was integrated with the *hydroPSO* algorithm and advanced sensitivity analyses, and user-friendly evaluation plots were estimated to facilitate the interpretation and assessment of the calibration results. Application of R-UTHBAL with the *hydroPSO* showed that the uncertainty in streamflow estimation should always be accounted for and evaluated in operational water resources management projects.

Keywords: water balance model; UTHBAL; *hydroPSO*; optimisation; sensitivity analysis; uncertainty analysis

1. Introduction

Conceptual rainfall-runoff models are frequently used to estimate the runoff generation mechanisms and the water balance components at various temporal and spatial scales. A satisfactory match between observed and simulated outputs is often achieved by calibrating the model parameters. However, the results are quite uncertain due to aleatory and epistemic uncertainty. Inaccuracies in the input data (such as precipitation and temperature), the calibration data (such as streamflow), the model parameters, and the mathematical model structure are the four main causes of epistemic uncertainty in hydrological modeling [1]. While the later two are more model-specific, the first two error sources are influenced by the quality of the data. Hence, assessment of the uncertainties is crucial in hydrological studies, water resources management, climate change assessment, estimation of water balance in ungauged watersheds [2].

The aim of this study is to estimate the uncertainties in the surface runoff simulated by a monthly water balance model in a mountainous watershed of the Portaikos river, a tributary of the Pinios river, Thessaly, Greece. The University of Thessaly (UTHBAL) monthly water balance model [3,4] is developed in the R statistical computing environment language, named 'R-UTHBAL', to estimate surface water balance in data-scarce watersheds. Two sources of uncertainties in hydrological modelling are considered: the un-

certainties in input data estimation and in model parameters. The uncertainties are estimated with the use of the R-package '*hydroPSO*', a global Particle Swarm Optimisation (PSO) algorithm [5] for the calibration of environmental models. The R-UTHBAL is integrated with the *hydroPSO* algorithm and advanced sensitivity analyses, and user-friendly evaluation plots are estimated to facilitate the interpretation and assessment of the calibration results.

2. Materials and Methods

2.1. The R-UTHBAL Model

The monthly water balance model UTHBAL [3] is selected to redesigned in the R-Environment because it has been applied successfully to simulate surface runoff and groundwater recharge in many studies [6,7]. Monthly time series of precipitation, mean temperature, and potential evapotranspiration are used as inputs by UTHBAL. The snowpack and snowmelt are calculated from total precipitation which is divided into rainfall and snowfall. Using a soil moisture mechanism, the model splits the entire watershed runoff into three components: the surface runoff, the interflow, and the baseflow. The model's first objective is to accurately fulfil actual evapotranspiration. Watershed runoff, actual evapotranspiration, groundwater recharge, and soil moisture are the model's outputs. Mathematical details could be found in a recent study [3].

Figure 1 presents the R-UTHBAL model with the flow diagram and the R-Environment framework using the *hydroPSO* algorithm. Six model parameters should be estimated and are usually determined during calibration based on monthly streamflow data. Model parameters are: the *CN* (Curve Number) of the US Soil Conservation Service, the C_m parameter of monthly melt rate factor, the coefficient α of actual evapotranspiration (*aAET*), the coefficient *K* of groundwater recharge, the coefficients β and γ of interflow (*CONMR*) and baseflow (*CONGROUND*), respectively (Figure 1a). Previous application of the UTHBAL model showed that the model parameters are independent, well-defined and simulation streamflow errors are normally distributed [4]. Several command-functions carried out in the R environment, for the operation of the models, input and data preparation and transformation, selection of parameter space, calibration method, optimisation function and statistical analyses (Figure 1b).

2.2. Water Balance Modelling Procedure

The study area is the Portaikos River watershed in the outlet at Pyli hydrometric station. It is a forested mountainous watershed and has an area of about 133 km^2. The mountainous watershed is located in Thessaly Region and Portaikos river is one of the main tributaries of Pinios River. Monthly streamflow data were available for the period October 1990–September 1993. Areal input datasets were estimated for the above period using typical engineering methods (i.e., precipitation/temperature gradients, Thiessen polygons) from the available meteorological stations. Potential evapotranspiration was calculated with the Thorthwaite method based on the estimated mean monthly temperature values.

The Latin-Hypercube One-factor-At-a-Time procedure developed by van Griensven et al. [8] for sensitivity analysis of model parameters is firstly applied to identify significant model parameters and the required mathematical model structure. Then, several objective functions, (i.e., Nash-Sutcliffe Efficiency and variations or adaptations like Kling-Gupta efficiency (KGE) formulations [9,10] and Root Mean Square Error (RMSE)), addressing different parts of the hydrograph have been used to assess both the skill and the robustness of the R-UTHBAL model to perform consistent streamflow predictions using the temporal split-sample test. Confidence intervals in the simulated runoff due to input data uncertainty, parameter uncertainty and total uncertainty were calculated using the *hydroPSO* algorithm. *hydroPSO* implements several state-of-the-art enhancements and fine-tuning options to the Particle Swarm Optimisation (PSO) algorithm to meet specific user needs. *hydroPSO* easily interfaces the calibration engine to different model codes

through simple ASCII files and/or R wrapper functions for exchanging information on the calibration parameters. Then, optimises a user-defined goodness-of-fit measure until a maximum number of iterations or a convergence criterion are met. Finally, advanced plotting functionalities facilitate the interpretation and assessment of the calibration results.
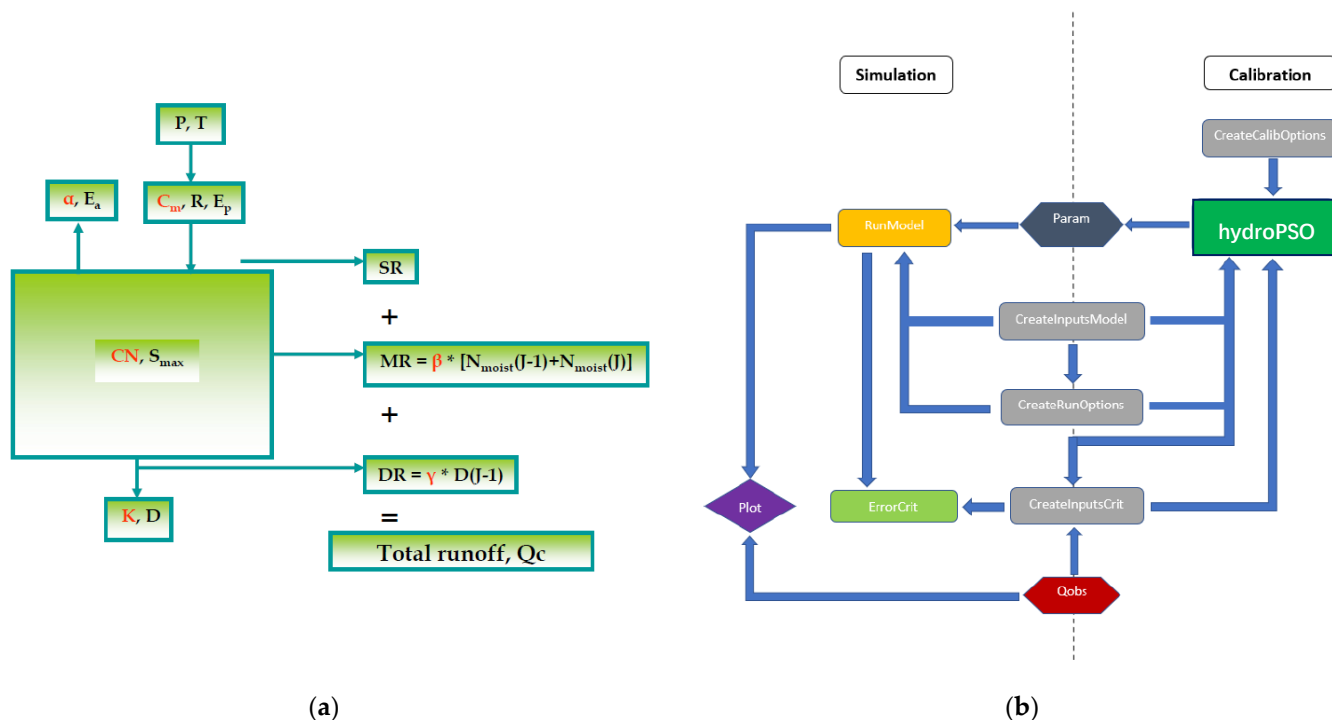

(**a**)   (**b**)

Figure 2. The R-UTHBAL model: (**a**) Flow Diagram and (**b**) the R workflow environment with hydroPSO algorithm.

3. Results and Discussion

Table 1 presents the sensitivity analysis results for the six (6) model parameters using the modified KGE [10] as the objective function, 5000 strata for LH sampling with variance fraction 10%. In this table the parameter ranges are also depicted. Based on Table 1 all model parameters should be included in the mathematical model structure. Using the temporal split-sample test between 1st (October 1960–September 1977) and 2nd period (October 1977–September 1993) the models have been calibrated for half of the years during both 1st and 2nd periods leaving the rest half of the years for validation. The KGE2 values of the optimisation process were 0.79 and 0.87 for the 1st and 2nd period, respectively for 2000 model realisations. Figure 2 presents the results for the 1st period and parameter values versus the corresponding goodness-of-fit values (KGE2) obtained during optimisation procedure.

Table 1. Model parameter range values, sensitivity analysis results and optimised model parameters using the R-UTHBAL model and *hydroPSO* algorithm.

Parameter	Min Value	Max Value	*Ranking Number*	*Normalised Relative Importance (%)*	*Optimised Value 1960–1977*	*Optimised Value 1977–1993*
C_m	0	12	6	09.96	80.244	166.2
CN	30	100	5	14.47	60.300	172.9
K	0	1	4	17.16	24.810	177.3
$\alpha = aAET$	0	1	3	18.70	93.055	200.0
$\beta = CONMR$	0	1	2	19.66	7.979	125.9

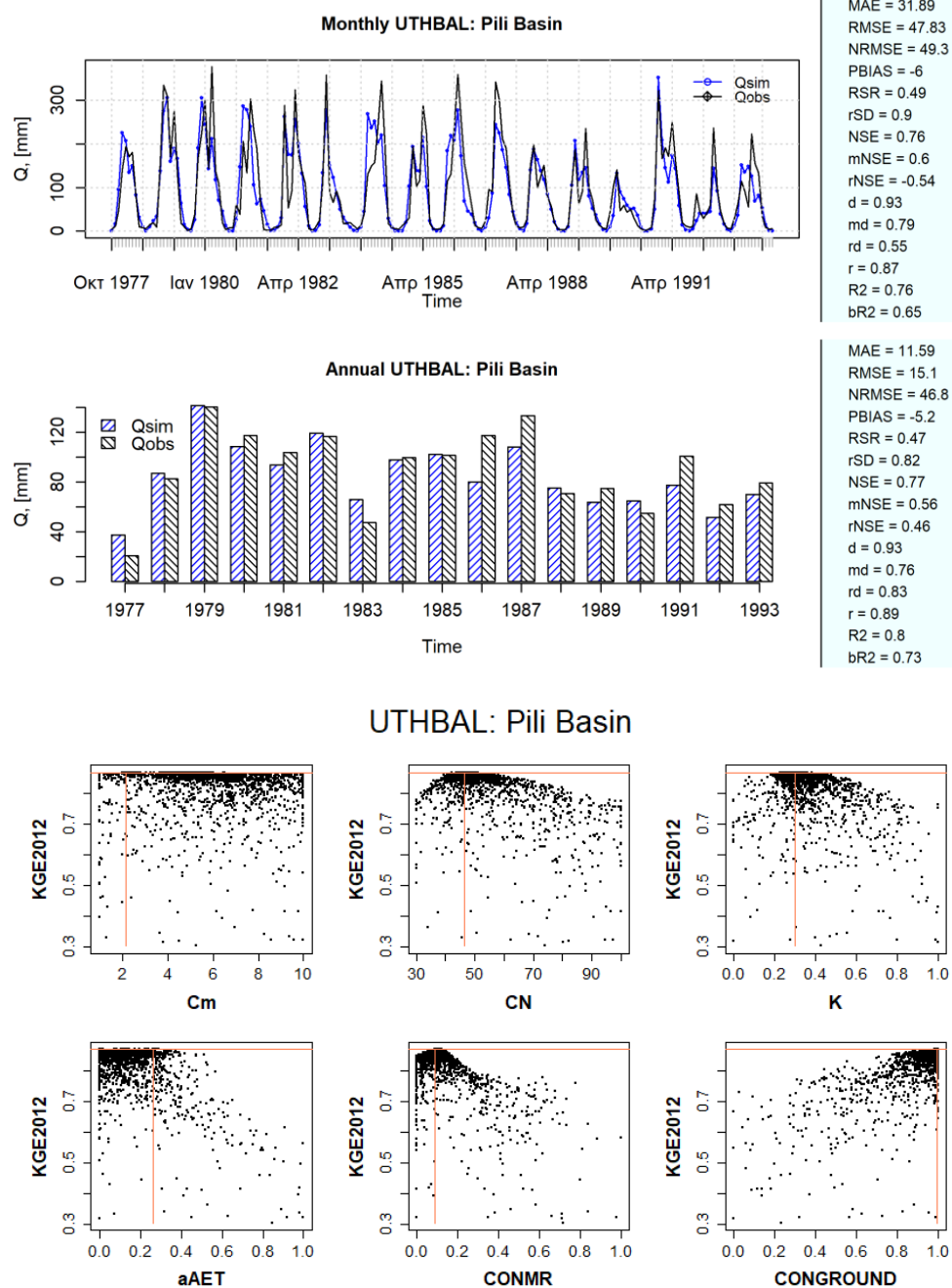|					
γ = CON-GROUND	0	1	1	20.02	192.678	232.9

Figure 2. Validation results (monthly and annual graphs using several performance indices) for the 1st period October 1960–September 1993 and parameter values versus the corresponding goodness-of-fit values (KGE2) obtained during optimisation.

Based on a selected threshold of KGE2 > 0.3 as behavioural threshold all parameter values above the threshold are selected and weighted quantiles of model parameters are calculated to provide an estimate of the uncertainty in each model parameter. Using the **P-factor**, which represents the percent of observations that are within the user-defined uncertainty bounds and the **R-factor** that represents the average width of the user-defined uncertainty bounds divided by the standard deviation of the observations a quantification of the uncertainty is estimated [5]. Figure 3 presents the results of the uncertainty analysis

for the verification period and shows the *best* simulated streamflows along with the 95 Percent Prediction Uncertainty (95 PPU) and Figure 4 presents the uncertainty in flow duration curve using the one of the *best* simulated streamflows, and the flow duration curves for the 2.5 and 97.5 weighted quantiles of model simulations obtained during the verification period.
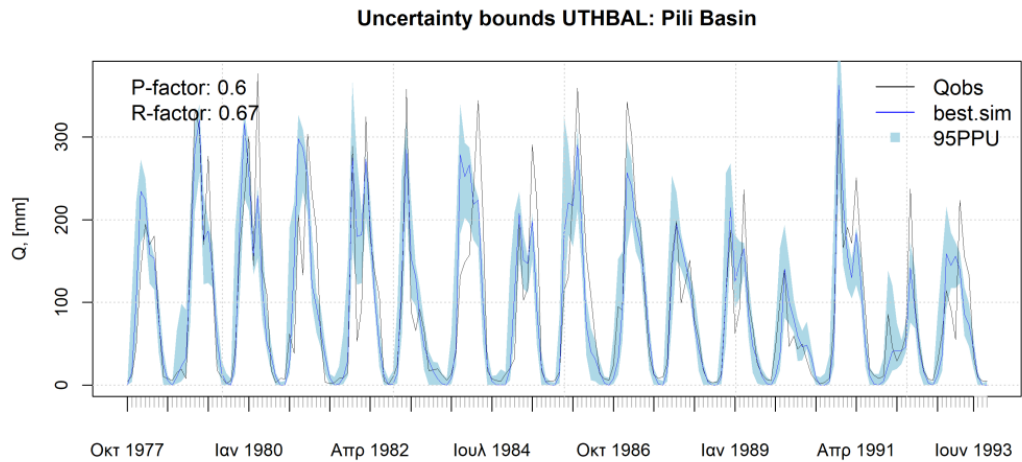

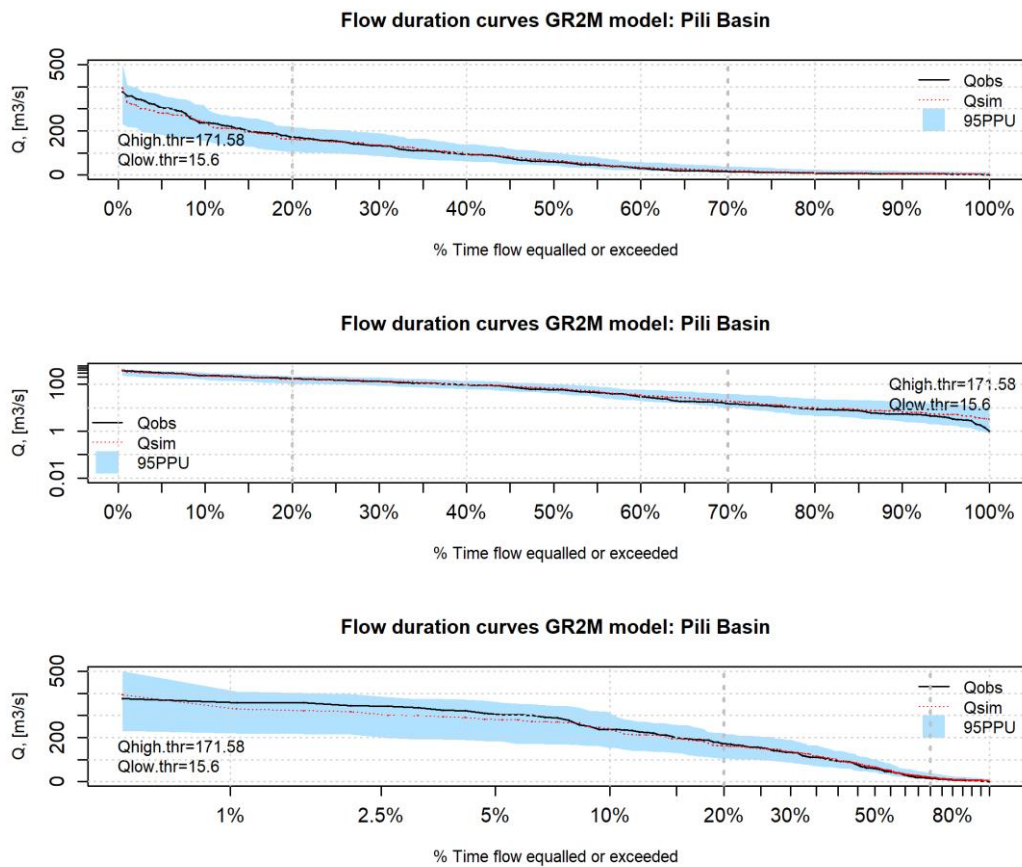**Figure 3.** 95 Percent Prediction Uncertainty (95 PPU) for model simulations during the verifcation period.

Figure 4. Flow duration curve of the observed (black line) and best simulated (blue line) stream-flows. In addition, flow duration curves for the 2.5 and 97.5 weighted quantiles of model simulations

obained during the verification period. The upper panel is the normal flow duration curve, the middle panel has focus on low flows (log = 'y') and the lower panel has focus on high flows (log = 'x').

4. Concluding Remarks

Accurate assessment of streamflow is crucial for operational water resources management projects. This study estimated the uncertainties in the surface runoff simulated by a monthly water balance model in a mountainous watershed of the Portaikos river, a tributary of the Pinios river, Thessaly, Greece. The R-UTHBAL water balance model was integrated with the hydroPSO algorithm and advanced sensitivity analyses, and user-friendly evaluation plots were estimated to facilitate the interpretation and assessment of the optimisation process. Application of R-UTHBAL with the hydroPSO in Portaikos river basin in Thessaly, Greece, showed that the uncertainty in streamflow estimation should always be accounted for and evaluated in operational water resources management projects.

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