

Phase Behavior of Athermal Colloidal Mixtures of Chains and Monomers

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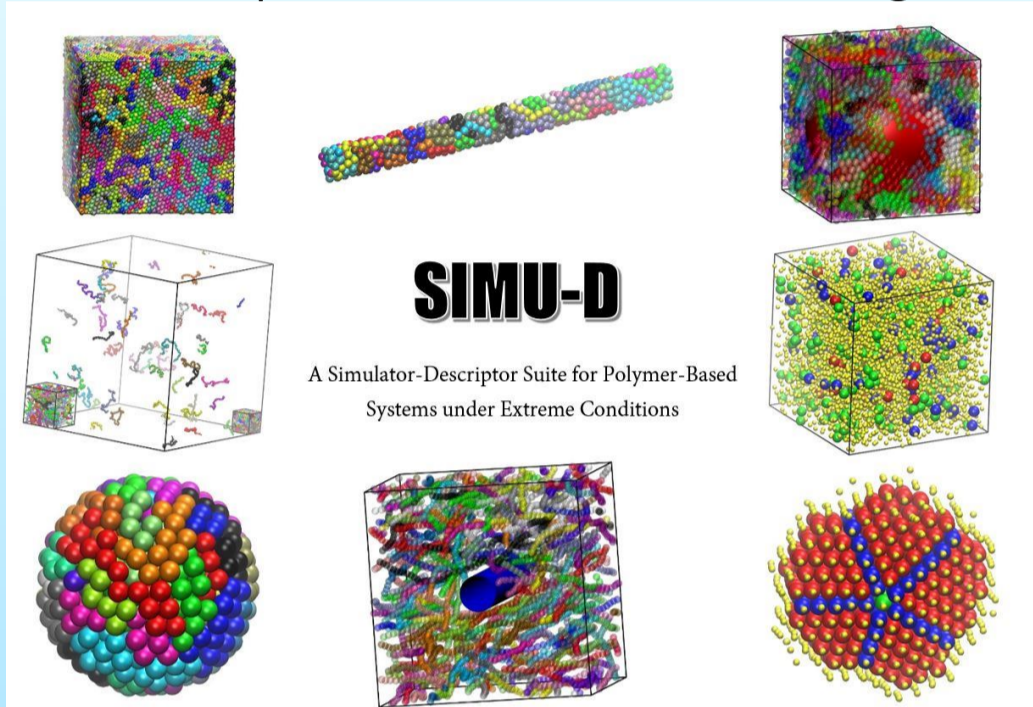
1. Objectives

- Study the **phase behaviour** of mixtures of **hard-sphere chains** and **monomers**
- **Hard-sphere chains** and **monomers** have **different melting points**: $\varphi_{chains}^M \cong 0.57 > 0.545 = \varphi_{monomers}^M$ [1,2,3]
- Explore how **packing density** and **relative molar fraction** affect the ability of the systems to **crystallize**.
- Identify the **entropic origins** of **crystallization** [4] and investigate the possibility of **phase separation** of the **mixture**.

2.A Method: Monte Carlo Simulations

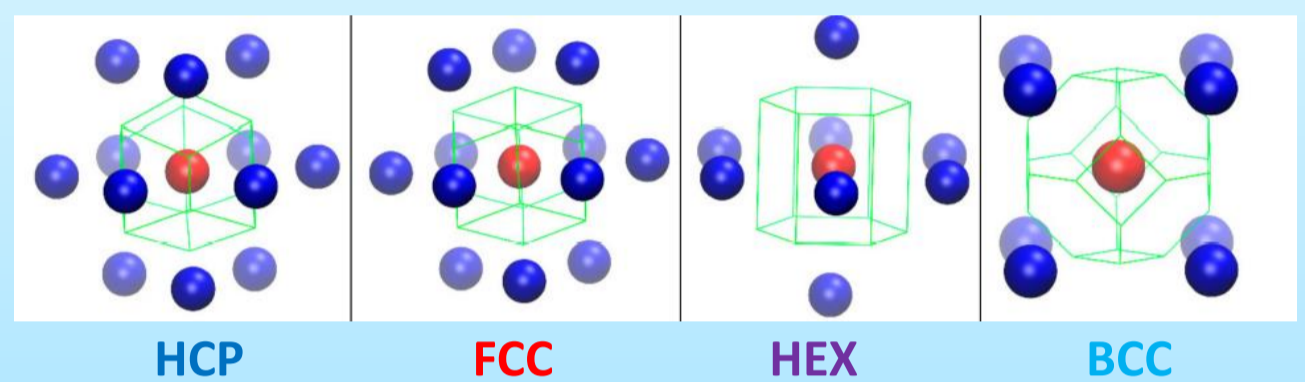
Monte Carlo method: Simu-D simulator-descriptor [5].

- **Simulator** part based on Monte Carlo algorithms



2.B Method: Characterization

- **Structural analysis** of computer-generated configurations of general atomic to **gauge local order**.
- **CCE norm: descriptor** to quantify the **orientational** and **radial deviations** from a specific **reference crystal** [6].

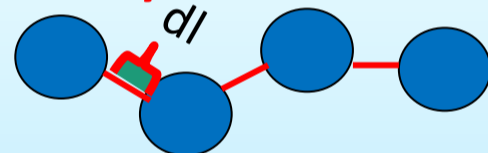


3. Molecular Model and Systems

Hard Sphere model

$$v^{HS}(r_{ij}) = \begin{cases} \infty, & r_{ij} < \sigma \\ 0, & r_{ij} \geq \sigma \end{cases}$$

Freely-Jointed chains



N_{at} spheres being part of chains or individual ones $N_{at} = 1200$
x: relative molar fraction (spheres in chains / total spheres)

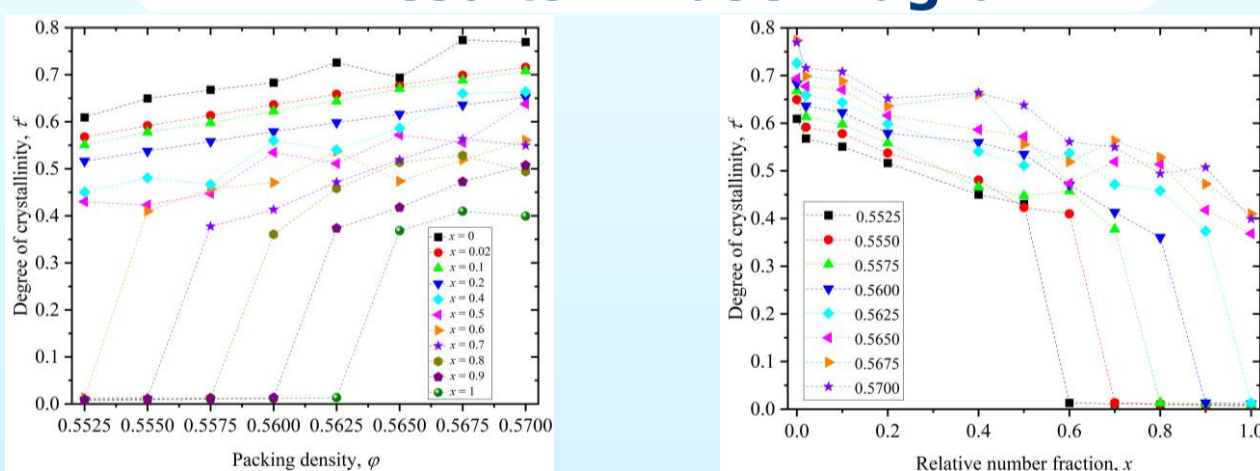
φ : Packing density

Average chain length: $N_{av} = 12$

$$x \in [0, 1]$$

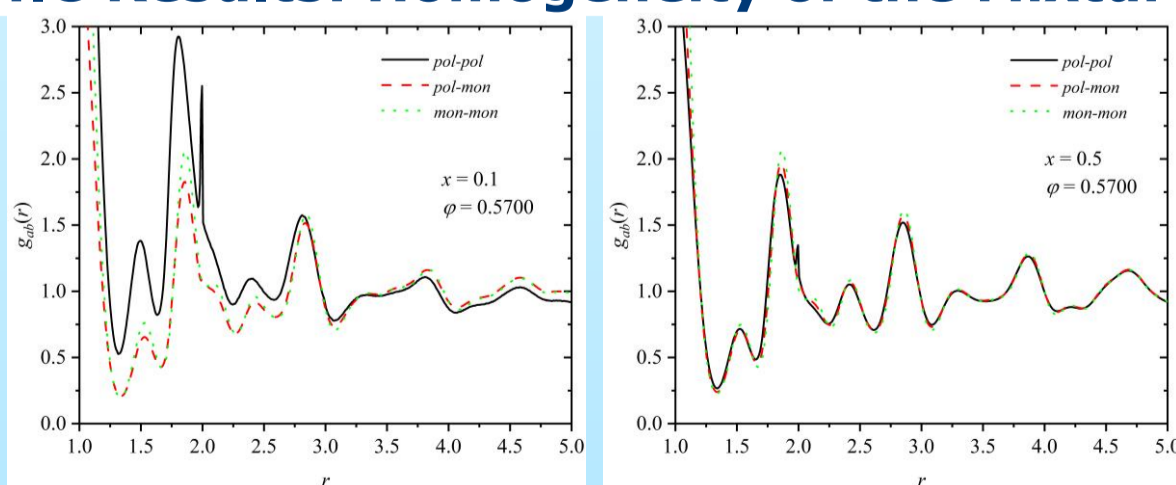
$$\varphi \in [0.55, 0.57]$$

4.B Results: Phase Diagram



- **Crystallinity** drops with increasing x
- **Crystallinity** increases with increasing φ
- Under specific conditions the melting point shifts to higher φ

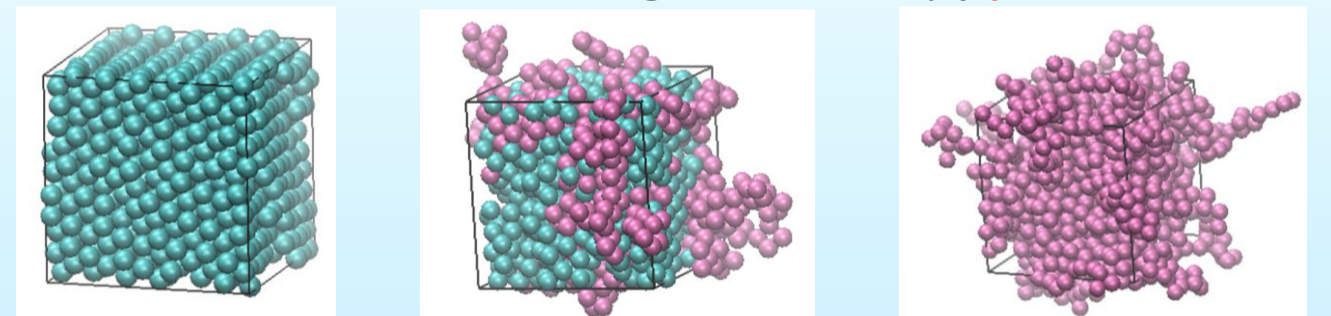
4.C Results: Homogeneity of the Mixture



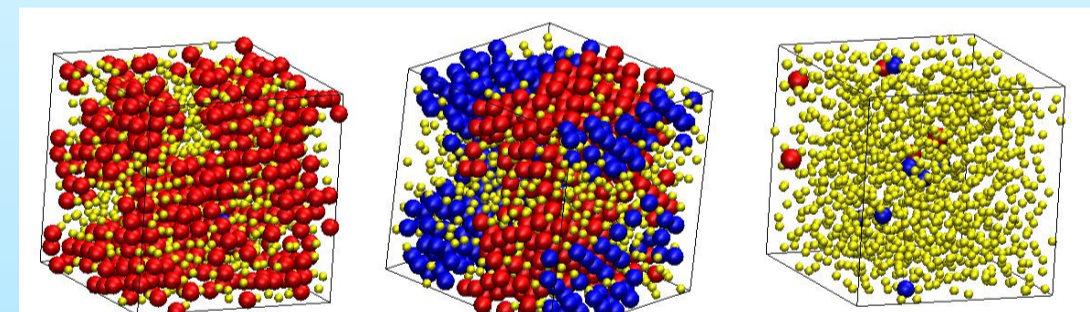
Perfect mixing \Rightarrow no phase separation [7]

4.A Results: Snapshots

Monomers colored according to their identity | $\varphi = 0.5575$

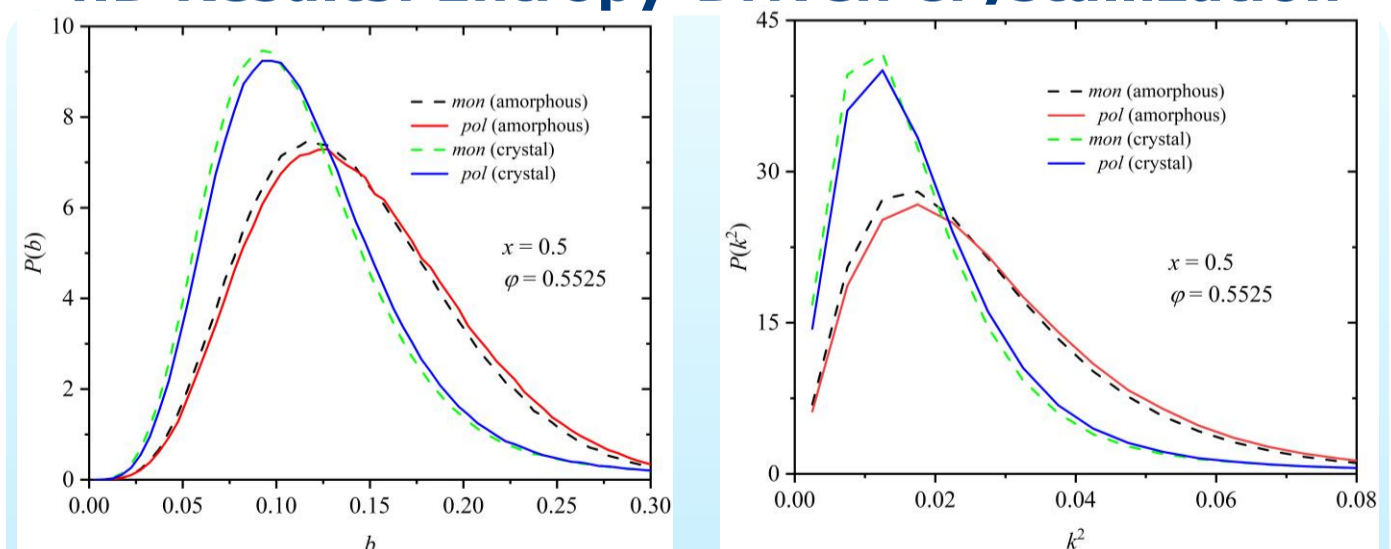


Monomers colored according to CCE norm | $x = 0.8$



● HCP
● FCC
● AMO

4.D Results: Entropy-Driven Crystallization



Asphericity, b and relative shape anisotropy, k^2 of the Voronoi polyhedra

- The **local environment** becomes more **spherical and isotropic** in the crystal phase \rightarrow **increase in translational entropy**
- The **local environment** around **individual spheres** is systematically more **spherical and symmetric** compared to the one of spheres belonging to **chains**.

Acknowledgements

Financial Support through:

- Project "PID2021-127533NB-I00" of MICIU/DEFER (Spain)
- "Programa Propio" UPM-Santander Bank

Computational Support through:

- CeSViMa (UPM, Spain)



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[3] N. C. Karayiannis, K. Foteinopoulou and M. Laso, *Soft Matter* **11**, 1688 (2015).

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[5] M. Herranz et al., *Int. J. Mol. Sci.* **22**, 12464 (2021).

[6] P. Ramos et al., *Crystals* **10**, 1008 (2020).

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