

Constrained Neutrino Masses and Flavour Observables from a Dual Seesaw Framework

Manash Dey[†]

[†]Department of Physics, Maibang Degree College, 788831, India

MOTIVATION & AIM

- ✓ Neutrino oscillation confirms tiny non-zero masses and non-trivial mixing, pointing clearly to physics beyond the Standard Model (SM).
- ✓ Precision measurements of θ_{13} and CP violation rule out simple flavour-symmetric structures, motivating refined and realistic mass textures.
- ✓ A dual seesaw (Type-I + Type-II) framework provides a natural mechanism to generate small Majorana neutrino masses with structured correlations.
- ✓ We construct a constrained and predictive neutrino mass texture by reducing independent parameters while maintaining consistency with oscillation data.
- ✓ The framework reproduces realistic neutrino masses and mixing, and tests its efficacy through measurable observables such as effective Majorana mass ($m_{\beta\beta}$) and branching ratio (BR) of the dominant charged lepton flavour violating (cLFV) decay $\mu \rightarrow e + \gamma$.

THE MODEL

- We extend the SM with additional scalar fields and enforce A_4 and cyclic symmetries.
- The transformation properties of the field content under $A_4 \times Z_3 \times Z_{10} \times SU(2)_L \times U(1)_Y$ are shown below

Field	D_{l_L}	l_R	ν_{l_R}	H	Φ	η	κ	Δ	ξ	ζ
A_4	3	$(1, 1'', 1')$	$(1, 1'', 1')$	3	3	$1''$	$1'$	3	1	1
Z_3	1	(ω, ω, ω)	$(1, 1, 1)$	ω^2	1	1	1	1	1	1
Z_{10}	0	0	$(0, 4, 6)$	0	0	2	8	0	6	4
$SU(2)_L$	2	1	1	2	2	1	1	3	1	1
$U(1)_Y$	-1	-2	0	1	-1	0	0	-2	0	0

- The Yukawa Lagrangian ($-L_Y$) of the model is formulated in the T basis and is presented below

$$y_e(\bar{D}_{l_L} H) e_R + y_\mu(\bar{D}_{l_L} H) \mu_R + y_\tau(\bar{D}_{l_L} H) \tau_R + y_1(\bar{D}_{l_L} \Phi) \nu_{eR} + \frac{y_2}{\Lambda}(\bar{D}_{l_L} \Phi) \nu_{\mu R} \xi + \frac{y_3}{\Lambda}(\bar{D}_{l_L} \Phi) \nu_{\tau R} \zeta + \frac{1}{2} M_1(\nu_{eR}^c \nu_{eR}) + \frac{1}{2} M_2[(\nu_{\mu R}^c \nu_{\tau R}) + (\nu_{\tau R}^c \nu_{\mu R})] + \frac{1}{2} y_{R1}(\nu_{\mu R}^c \nu_{\mu R}) \eta + \frac{1}{2} y_{R2}(\nu_{\tau R}^c \nu_{\tau R}) \kappa + \frac{1}{2} y_\Delta(\bar{D}_{l_L} D_{l_L}^c) \tilde{\Delta} + h.c.$$

- The vacuum alignment associated with the scalar fields is chosen as $\langle H \rangle = v_h(1,0,0)$, $\langle \Phi \rangle = u(0,1,1)$, $\langle \Delta \rangle = v_\Delta(0,1,-1)$, $\langle \eta \rangle = v_\eta$, $\langle \kappa \rangle = v_\kappa$, $\langle \xi \rangle = v_\xi$, $\langle \zeta \rangle = v_\zeta$. The Type-I +Type-II seesaw neutrino mass matrix (M_ν) is obtained as shown below

$$a = \frac{u^2 \tilde{y}_3 (M_3 \tilde{y}_3 - M_2 \tilde{y}_2)}{M_2^2 - M_3 M_4} + \frac{v_\Delta y_\Delta}{3}$$

$$b = \frac{u^2 \tilde{y}_2 (M_4 \tilde{y}_2 - M_2 \tilde{y}_3)}{M_2^2 - M_3 M_4} - \frac{v_\Delta y_\Delta}{3}$$

$$c = u^2 \left(\frac{M_3 \tilde{y}_3^2}{M_2^2 - M_3 M_4} - \frac{y_1^2}{M_1} \right) + \frac{2 v_\Delta y_\Delta}{3}$$

$$d = u^2 \left(\frac{-M_2 \tilde{y}_2 \tilde{y}_3}{M_2^2 - M_3 M_4} - \frac{y_1^2}{M_1} \right)$$

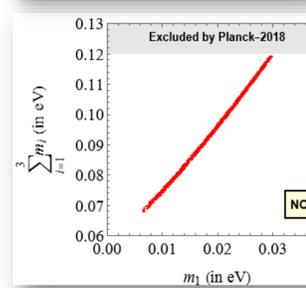
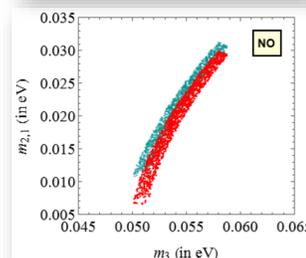
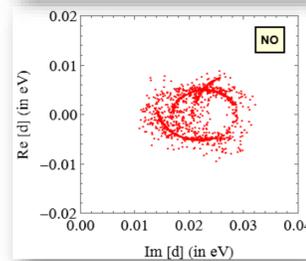
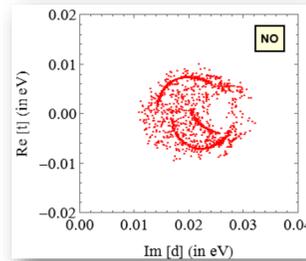
$$t = u^2 \left(\frac{M_4 \tilde{y}_2^2}{M_2^2 - M_3 M_4} - \frac{y_1^2}{M_1} \right) - \frac{2 v_\Delta y_\Delta}{3}$$

$$\begin{pmatrix} a+b & a & b \\ a & c & d \\ b & d & t \end{pmatrix}$$

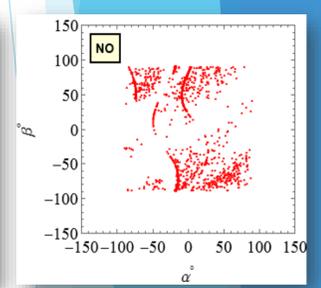
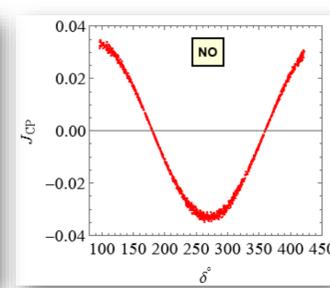
Where, $M_3 = y_{R1} v_\eta$, $M_4 = y_{R2} v_\kappa$,

$$\tilde{y}_2 = \frac{y_2 v_\xi}{\Lambda}, \quad \tilde{y}_3 = \frac{y_3 v_\zeta}{\Lambda}$$

NUMERICAL ANALYSIS & RESULTS

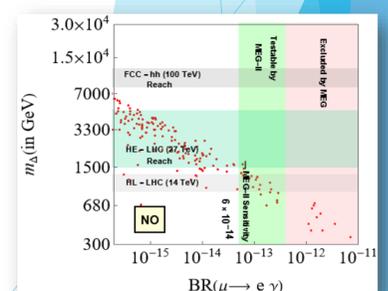
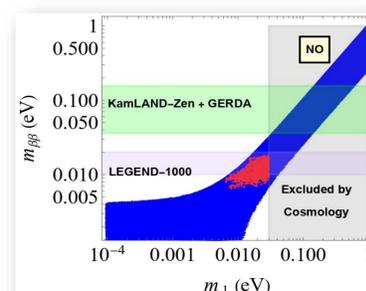


- ❖ $M_\nu \rightarrow M_\nu^{diag} = \tilde{U}^T M_\nu \tilde{U} = \text{diag}(\tilde{m}_1, \tilde{m}_2, 1)$
- ❖ Where, $\tilde{m}_1 = m_1 e^{-2i\alpha}$ and $\tilde{m}_2 = m_2 e^{-2i\beta}$
- ❖ As a result, $a, b, c, d, t \rightarrow \text{Re}[d], \text{Im}[d], \text{Re}[t]$
- ❖ Hence, $\text{Re}[d], \text{Im}[d], \text{Re}[t]$ spans the entire texture and the predictions associated with it.
- ❖ We determine the most compatible parameter space for $\text{Re}[d], \text{Im}[d], \text{Re}[t]$ such that Δm_{21}^2 and Δm_{31}^2 lie within 3σ [1] oscillation bounds and $\sum m_i < 0.12 \text{ eV}$ [2].
- ❖ We find that the model is viable only for Normal Ordering (NO)
- ❖ We predict the three neutrino mass eigenvalues (m_1, m_2, m_3), two Majorana phases (α, β) and Jarlskog invariant (J_{CP})



- ❖ The model predicts the effective Majorana mass: $m_{\beta\beta} = \sum_{i=1}^3 |U_{ei}^2 m_i|$.
- ❖ We analyse CLFV via the decay $\mu \rightarrow e + \gamma$ and compute $\text{BR}(\mu \rightarrow e\gamma)$.
- ❖ The branching ratio arising from Type-I seesaw is strongly suppressed and phenomenologically negligible.
- ❖ The scalar triplet of Type-II seesaw gives the dominant contribution to $\text{BR}(\mu \rightarrow e\gamma)$ [3], making $\mu \rightarrow e + \gamma$ an important experimental test of the model and its parameter space.

Sciforum-153172



SUMMARY

We present a flavour symmetric dual seesaw framework, which constrains the neutrino mass matrix to three effective parameters while reproducing current oscillation data. The model favours NO, predicts non-zero leptonic CP violation, and remains consistent with experimental data. It provides experimentally testable predictions in $m_{\beta\beta}$ and $\text{BR}(\mu \rightarrow e\gamma)$.

SUGGESTED READS & CONTACT INFORMATION



Email: manashdey1272@gmail.com
Phone: +91-8638801196