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NATURAL TIME ANALYSIS: RESULTS RELATED TO TWO EARTHQUAKES IN GREECE DURING 2019

Nicholas V. Sarlis ^{1,2} , Efthimios S. Skordas ^{1,2}  and Panayiotis A. Varotsos ^{1,2} *

¹ Section of Solid State Physics, Department of Physics, National and Kapodistrian University of Athens, Panepistimiopolis, Zografos 157 84, Athens, Greece

² Solid Earth Physics Institute, Department of Physics, National and Kapodistrian University of Athens, Panepistimiopolis, Zografos 157 84, Athens, Greece

* Correspondence: pvaro@otenet.gr; Tel.: +30-2107276737

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Abstract: The following two earthquakes occurred in Greece during 2019: First, a Mw5.4 earthquake close to Preveza city in Western Greece on 5 February and a Mw5.3 earthquake 50km East of Patras on 30 March. Here, we present the natural time analysis of the Seismic Electric Signals (SES) activities that have been recorded before these two earthquakes. In addition, we explain how the occurrence times of these two earthquakes can be identified by analyzing in natural time the seismicity subsequent to the SES activities.

Keywords: seismicity; earthquake prediction; natural time; seismic electric signals; Greece

1. Introduction

According to the United States Geological Survey (USGS) [1], a strong earthquake (EQ) of moment magnitude M_w 6.8 occurred on 25 October 2018 22:55 UTC at an epicentral distance around 133 km SW of the city of Patras, Western Greece (see Figure 1). It was preceded by an anomalous geoelectric signal that was recorded on 2 October 2018 at a measuring station 70km away from the epicenter[2]. Upon analyzing this signal in natural time, it was found[2] that it conforms to the conditions suggested (e.g., see [3–5]) for its clarification as precursory Seismic Electric Signal (SES) activity[4,6,7]. Notably, the observed lead time of 23 days lies within the range of values that has been very recently identified[8] as being statistically significant for the precursory variations of the electric field of the Earth. Moreover, the analysis in natural time of the seismicity subsequent to the SES activity in the area candidate to suffer this strong earthquake has revealed[2] that the criticality conditions were obeyed early in the morning of 18 October 2018, i.e., almost a week before the strong earthquake occurrence, in agreement with earlier findings[4]. The application[2] of the recent method of nowcasting earthquakes[9–13], which is based on natural time, has revealed that an earthquake potential score around 80% was observed just before the occurrence of this M_w 6.8 earthquake. Here, we focus on the recording[14] of additional SES activities after the occurrence of the latter earthquake in the beginning of January 2019 (see below) that preceded the following two earthquakes in Greece during 2019: First, a Mw5.4 earthquake[15] close to Preveza city in Western Greece on 5 February 2019 and a Mw5.3 earthquake[16] on 30 March 2019 a few tens of km East of Patras SES measuring station (labeled PAT in Figure 1).

2. Results

Two SES activities have been recorded[14] by the VAN telemetric network[3] operating in real time in Greece on 3 January 2019 and 9 January 2019 at the measuring stations PAT and PIR, respectively (see Figure 1).

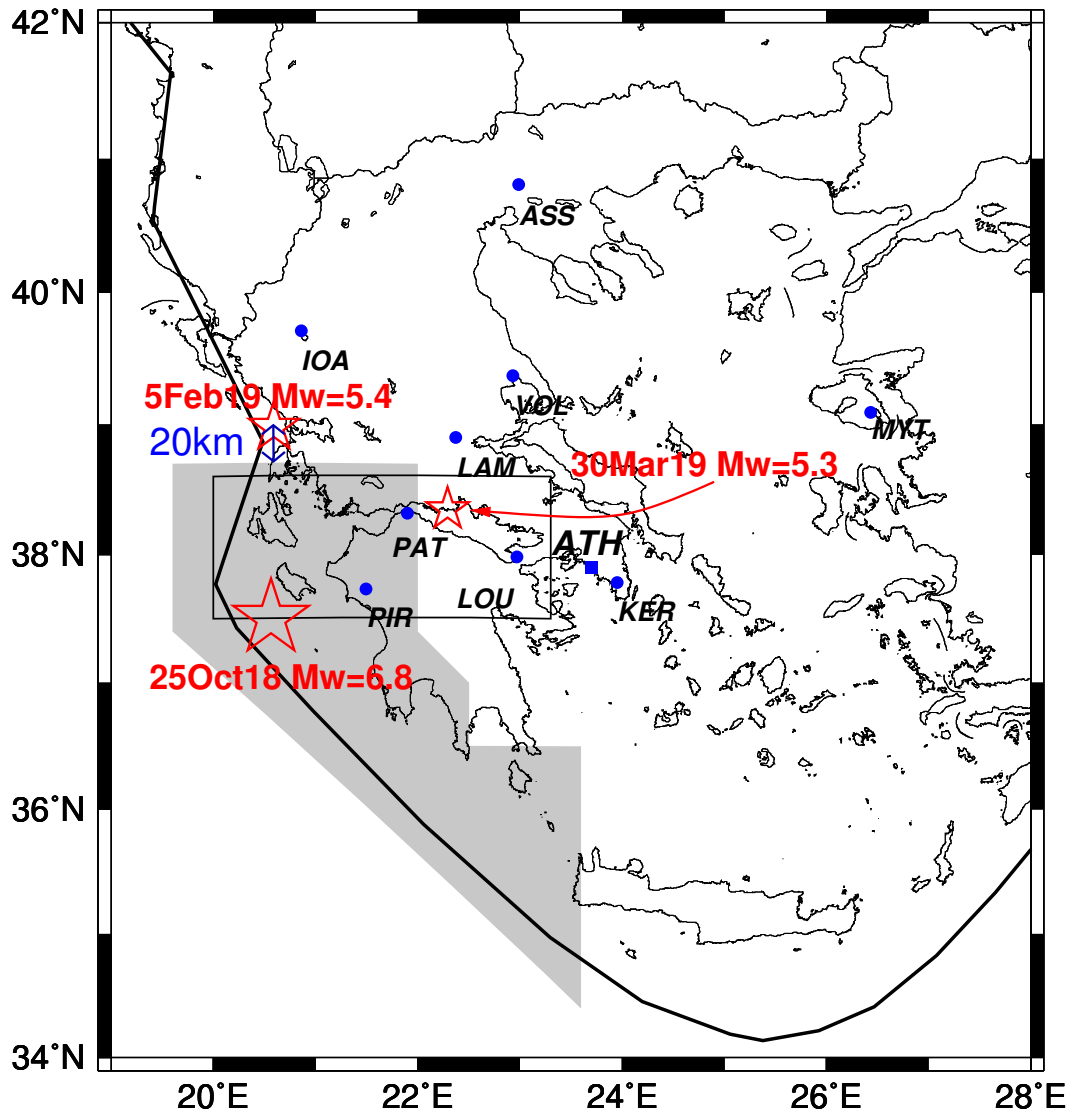


Figure 1. Map of the area $N_{34}^{42}E_{19}^{28}$ in which the locations of the SES measuring stations of the VAN telemetric network[3] operating in Greece are shown by the blue circles. The blue square corresponds to the central station operating at Glyfada, Athens (ATH), where the data are collected. The thick black line depicts the Hellenic arc[17] while the gray shaded area and the black rectangle the selectivity map of Pirgos (PIR) measuring station (see Fig.1 of [2]) and Patras (PAT) measuring station (see the rectangle with solid lines in Fig.8 of [18]), respectively. After the recording of the SES activities on 3 January 2019 at PAT and on 9 January 2019 at PIR, the areas corresponding to the selectivity maps of these two measuring stations have been reported in [14] as probable to suffer a strong EQ. The red stars correspond to the epicenters of the M_w 6.8 EQ on 25 October 2018, the M_w =5.4 EQ on 5 February 2019, and the M_w =5.3 EQ on 30 March 2019.

31 According to the VAN method of short-term earthquake prediction[3,4,6,7,19–21], the electric
 32 signals that are emitted from the future focal area as the stress increases prior to the EQ -due to
 33 the collective (re)orientation (cf. such a cooperativity is a hallmark showing that the region enters
 34 the critical stage) [22] of the anyhow pre-existing electric dipoles[23] in the ionic constituents of
 35 the rocks, e.g., see Fig.1 of [24]- follow[7] conductive paths in the solid Earth crust and become
 36 detectable at certain (SES sensitive) sites on the Earth's surface giving rise to the so-called selectivity
 37 phenomenon[7,17,25–31]. This means that an SES measuring station is capable of recording SESs
 38 emitted from certain EQ prone areas. After long experimentation (cf. SES research in Greece has
 39 started since 1980s, e.g. see [32,33]), for each measuring station one may construct a selectivity map of

40 this station by considering the EQs that have been preceded by SES recorded in the station as well as
 41 by using geological and geophysical data (since faults are usually highly more conductive than their
 42 surroundings, they constitute conductive paths, e.g. see [25]). The gray shaded area in Figure 1 depicts
 43 the selectivity map of the PIR measuring station as reported in [2] while the black rectangle in the same
 44 figure corresponds the selectivity map of the PAT measuring station[14,18].

45 The SES activity recorded on 3 January 2019 at PAT station can be seen in Fig.5 of [14]. The analysis
 46 in natural time has led[14] to values of κ_1 , S and S_- which are compatible with those observed for SES
 47 (see Section 4.1). After applying the methodology suggested in [34] for the analysis of the SES activity
 48 recorded on 3 January 2019 at PAT we obtain $\kappa_1 = 0.075(22)$, $S = 0.071(22)$, and $S_- = 0.075(30)$. More
 49 or less similar results are found for the SES recorded on 9 January 2019 at PIR.

50 After these observations and in order to estimate the occurrence time of the impending EQs, we
 51 started to analyze in natural time the seismic activity occurring after the SES within the respective
 52 selectivity maps of each measuring station, i.e., the gray shaded area of Figure 1 for PIR and the one
 53 shown by the black rectangle in Figure 1 for PAT. We observed (see Fig.7 of [35]) that when analyzing
 54 the seismicity within the PIR selectivity map, the criticality condition $\kappa_1 = 0.070$ has been fulfilled upon
 55 the occurrence of a ML(ATH)=3.5 EQ at 12:50 UTC on 29 January 2019 at 37.69°N 20.61°E exhibiting
 56 magnitude threshold invariance. Here, ML(ATH) stands for the local magnitude reported by the
 57 Institute of Geodynamics of the National Observatory of Athens. A week later, i.e., at 02:26 UTC on
 58 5 February 2019, an Mw5.4 EQ occurred with an epicenter at 38.98°N 20.59°E lying very close to the
 59 NorthWestern edge of the PIR selectivity map, see Figure 1. The corresponding natural time analysis
 60 of the seismicity within the PAT selectivity map (see the black rectangle in Figure 1) after the SES
 61 activity on 3 January 2019 has shown that upon the occurrence of the ML(ATH)=3.2 EQ at 06:53 UTC
 62 on 23 March 2019 at 37.69°N 20.61°E the condition $\kappa_1 = 0.070$ has been met for various magnitude
 63 thresholds (see Fig.9 of [35]). Interestingly, almost a week later the Mw=5.3 EQ of Figure 1 occurred at
 64 10:46 UTC on 30 March 2019 with an epicenter at 38.35°N 22.29°E lying inside the PAT selectivity map
 65 at a distance around 30km from the PAT measuring station.

66 3. Discussion

67 It is notable that the occurrence of the two EQs under study took place almost a week after
 68 the criticality condition $\kappa_1 = 0.070$ has been met for various magnitude thresholds. This compares
 69 favorably with the time window of a few days up to one week already found from various SES
 70 activities in Greece, Japan and United States [2,4,18,36–39].

71 4. Materials and Methods

72 4.1. Natural Time Analysis (NTA)

73 In a time series comprised of N individual events(e.g., electric pulses or EQs), the natural time[4,
 74 40–42] associated with the k -th event is given by $\chi_k = k/N$. In NTA[4,40–42], the pair (χ_k, Q_k) is
 75 studied, where Q_k is proportional to the energy emitted during the k -th event. For example in the case
 76 of SES, Q_k is proportional to the duration of each SES pulse[40,41], while for EQs it may be considered
 77 proportional to the seismic moment[40,42,43]. How the time series coming from a variety of complex
 78 systems are read in natural time can be seen in Fig. 1 of [5].

The pair (χ_k, Q_k) is studied by considering the normalized energy for the k -th event $p_k = Q_k / \sum_{n=1}^N Q_n$, where p_k can be also considered as a probability distribution[5,44]. In view of the latter, the function[4,40–42,44]

$$\Pi(\omega) = \left| \sum_{k=1}^N p_k \exp\left(i\omega \frac{k}{N}\right) \right|^2 \quad (1)$$

provides information about the probability distribution p_k when $\omega \rightarrow 0$. Expanding Eq.(1) around $\omega = 0$, we obtain that $\Pi(\omega) = 1 - \kappa_1 \omega^2 + \dots$, where κ_1 stands for the variance of natural time

$$\kappa_1 \equiv \sum_{k=1}^N \chi_k^2 p_k - \left(\sum_{k=1}^N \chi_k p_k \right)^2, \quad (2)$$

with respect to the distribution p_k . When Q_k are independent and identically distributed random variables, we have that $p_k \rightarrow 1/N$. This is the case of the so-called[4,45,46] ‘uniform’ distribution leading to a value of κ_1 equal to $\kappa_u = 1/12 \approx 0.083$. For critical systems, Varotsos *et al.* [47] have shown that

$$\kappa_1 \approx 0.07 \quad (3)$$

79 for a variety of systems approaching criticality. Thus, κ_1 reaches the value of 0.070 for a critical system
80 or 0.083 for a system exhibiting stationary or quasi-periodic behavior[5].

Apart from κ_1 , another useful quantity in NTA[4,5] is the entropy S given by[40,46,48]

$$S = \langle \chi \ln \chi \rangle - \langle \chi \rangle \ln \langle \chi \rangle, \quad (4)$$

81 where the brackets $\langle \dots \rangle$ ($\equiv \sum_{k=1}^N \dots p_k$) denote averages with respect to the distribution p_k . The
82 entropy S is a dynamic entropy that exhibits[49] positivity, concavity and Lesche[50,51] experimental
83 stability. When Q_k are independent and identically distributed random variables, S reaches[48] the
84 value $S_u \equiv \frac{\ln 2}{2} - \frac{1}{4} \approx 0.0966$ that corresponds to the aforementioned ‘uniform’ distribution. For SES,
85 it has been experimentally observed[4,49] that $S_{\text{SES}} \lesssim S_u$. Upon reversing the time arrow and hence
86 applying the time reversal operator \mathcal{T} to p_k , i.e., $\mathcal{T} p_k = p_{N-k+1}$, the value of S changes to a value S_- .
87 Again, it has been experimentally observed[4,49] that for SES activities: $S_- \lesssim S_u$.

88 5. Conclusions

89 The two strongest earthquakes that occurred in Greece since 1 January 2019, i.e., the Mw5.4
90 earthquake close to Preveza city in Western Greece on 5 February and the Mw5.3 earthquake 50km
91 East of Patras on 30 March have been preceded by Seismic Electric Signals (SES) activities that have
92 been identified as such before the earthquake occurrences[14].

93 The occurrence times of these two earthquakes can be approached by analyzing in natural time
94 the seismicity subsequent to the SES activities within the selectivity maps of the corresponding VAN
95 stations that recorded the SES activities.

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97 Software, N.V.S. and E.S.S.; Validation, E.S.S.; Formal analysis, N.V.S., E.S.S. and P.A.V.; Investigation, N.V.S., E.S.S.
98 and P.A.V.; Resources, E.S.S. and P.A.V.; Data Curation, N.V.S. and P.A.V.; Writing—original draft preparation,
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105 Abbreviations

106 The following abbreviations are used in this manuscript:

107

ATH	Athens
EQ	Earthquake
ML(ATH)	Local EQ magnitude reported by the Institute of Geodynamics of the National Observatory of Athens
Mw	Moment magnitude
108 NTA	Natural time analysis
PAT	Patras SES measuring station
PIR	Pirgos SES measuring station
SES	Seismic Electric Signals
VAN	Varotsos Alexopoulos Nomikos

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