

# Optics of cholesterics with oblique helicoidal director

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ADVANCED MATERIALS AND  
LIQUID CRYSTAL INSTITUTE  
at Kent State University



## Outline

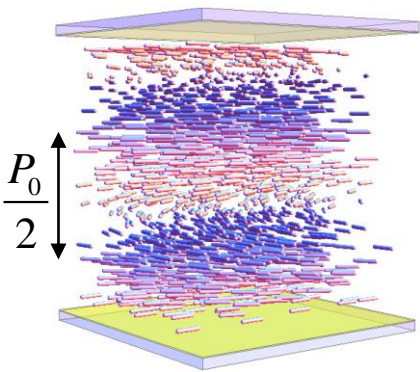
- **Oblique helicoidal cholesteric ( $\text{Ch}_{\text{OH}}$ ) state as continuously tunable 1D photonic crystal**
- **Effect of the surface alignment on Bragg reflection**
- **In-situ measurement of bend elastic constant in Ch phase**
- **Bragg diffraction at oblique incidence; polarization dependency**

# Cholesterics as 1D photonic crystals

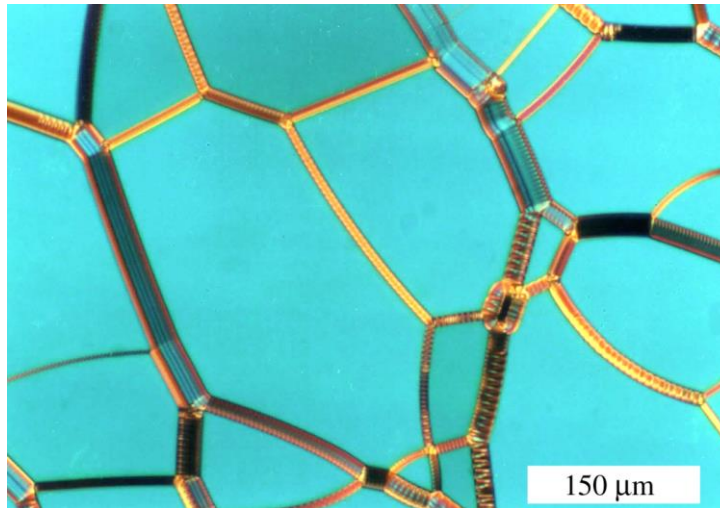


Naturally occurring colors – result of *Bragg reflection* at the periodic structure with the period close to the wavelength of visible light.

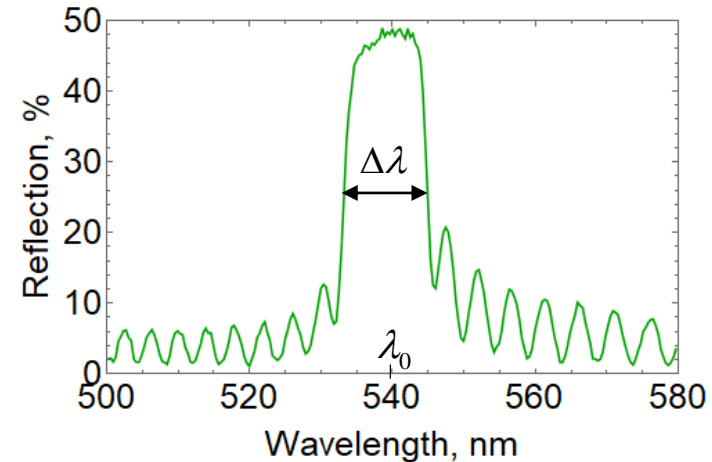
$\lambda_0$  – Bragg wavelength  
 $\Delta\lambda$  – Bandwidth, or width at the half-amplitude



Period  $\sim 0.1-1$  mm



Polarizing microscope texture of the cholesteric liquid crystal



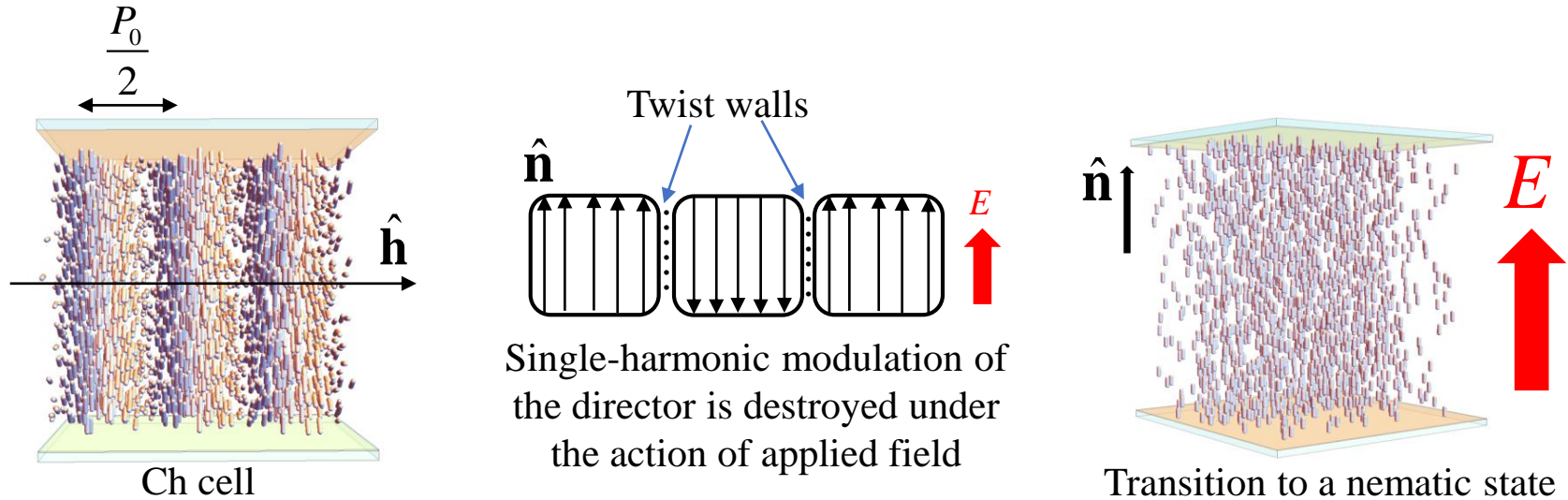
$$\Delta\lambda = \Delta n \frac{P_0}{2}$$

$$\lambda_0 = \bar{n} \frac{P_0}{2}$$

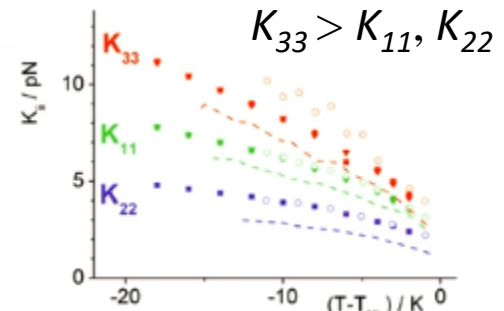
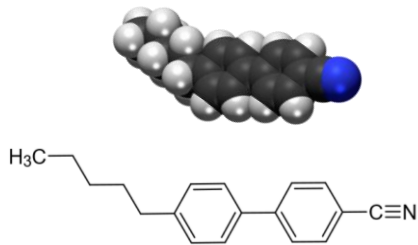
O.D. Lavrentovich, Handbook of liquid crystals, Ch. 6, 2014

# Cholesterics with positive dielectric anisotropy, $\Delta\epsilon > 0$

Attempt to control the pitch by the applied field  $\mathbf{E}$  leads to distortion of the helical structure and transformation to a nematic state (N) with the director  $\hat{\mathbf{n}}$  along the field (here,  $\hat{\mathbf{h}}$  is the helix axis).



**Material:** rod like molecules which are hard to bend, i.e. bend elastic constant  $K_{33}$  is large as compared to twist  $K_{22}$  and splay  $K_{11}$  moduli. Ch period is continuously tuned by the temperature, but *not* by applied field. *Common example:* 5CB molecule



# Oblique helicoidal cholesteric ( $Ch_{OH}$ ) state, $\Delta\varepsilon > 0$

## Theoretical prediction:

R. B. Meyer, Applied Physics Letters **12**, 281 (1968). ;  
 P. G. De Gennes, Solid State Communications **6**, 163 (1968).

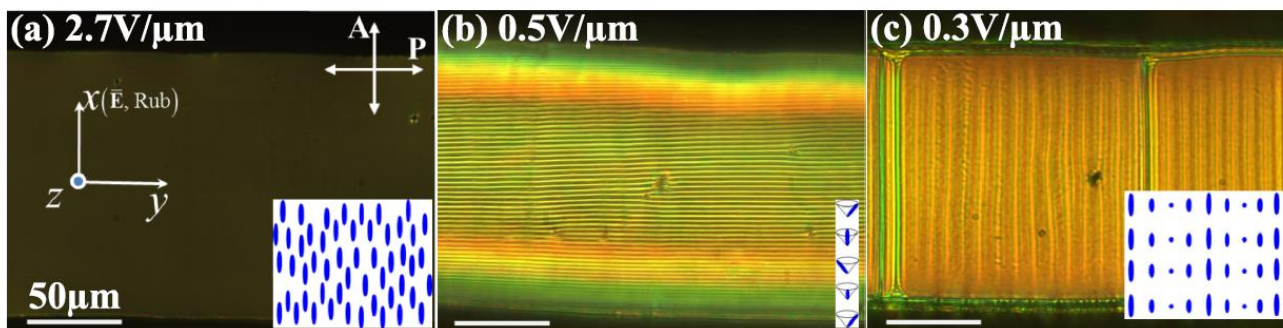
## Experimental observation:

$E_{Ch} < E_{ChOH} < E_N$  when  $K_{33}/K_{22} \leq 0.5$   
 $Ch_{OH}$  pitch  $P$  and cone angle  $\theta$  are both continuously tunable  
 by the applied field  $E_{ChOH}$   
 $K_{22}$  and  $K_{33}$  are elastic constants of twist and bend

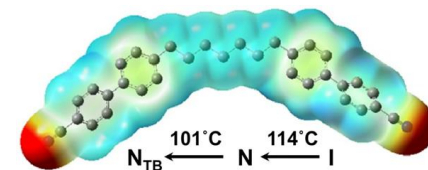
PRL **112**, 217801 (2014)

PHYSICAL REVIEW LETTERS

week ending  
 30 MAY 2014

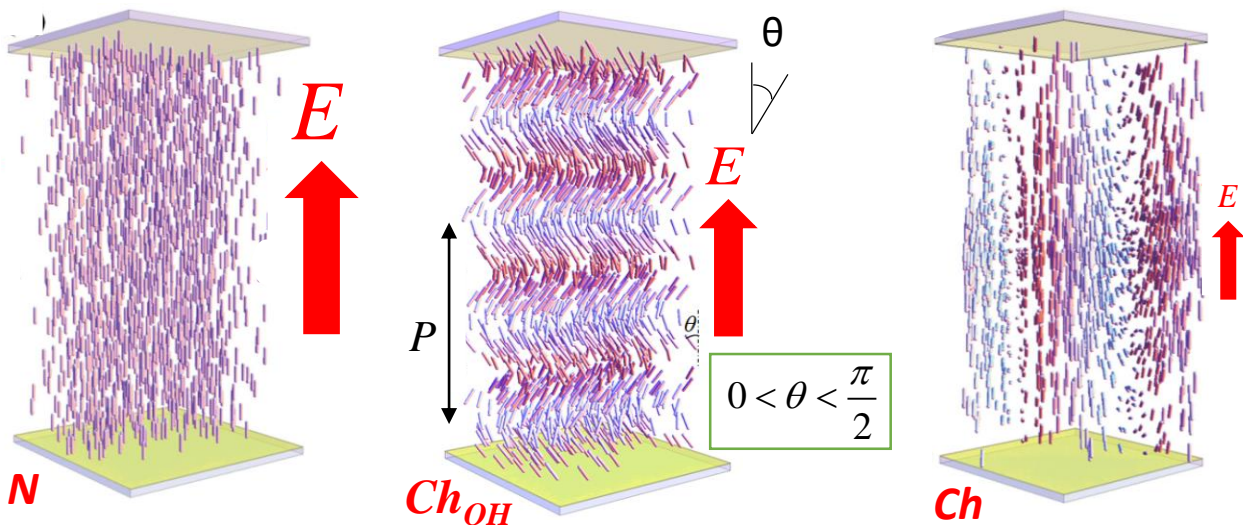


## Material:

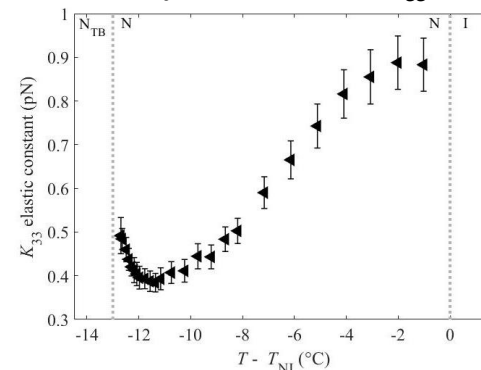


### Flexible dimer

1,7'' - bis(4-cyanobiphenyl-4'-yl)  
 heptane (CB7CB)



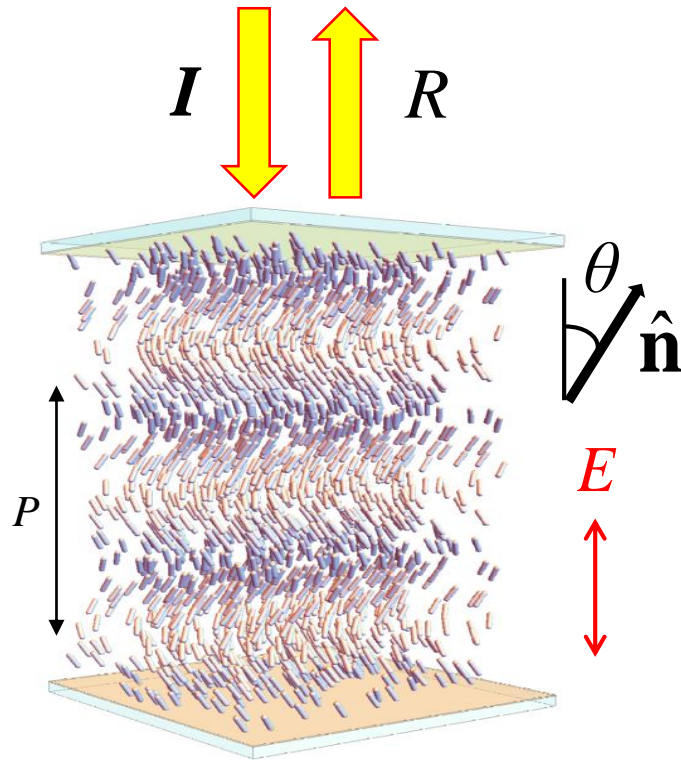
is easy to bend (small  $K_{33}$ )



G. Babakhanova, Z. Parsouzi et al,  
 Phys Rev E **96**, 062704 (2017)

J. Xiang et al, Phys Rev Lett **112**(21), 217801 (2014).

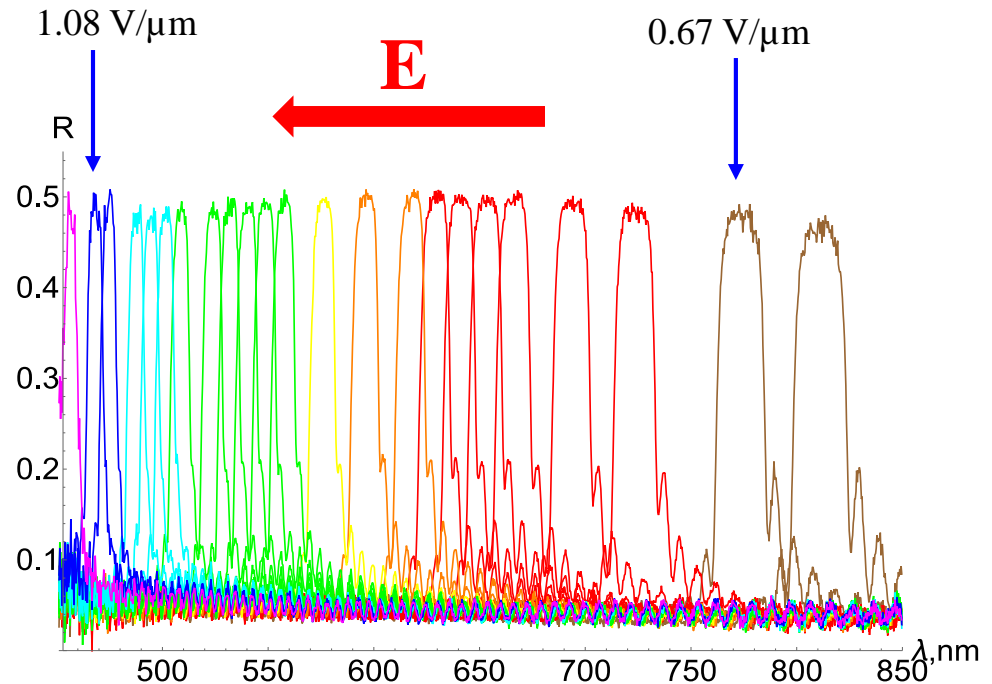
# E-tuned Bragg reflection at normal incidence of light



$$\lambda_{\text{Bragg}} = \bar{n}P, \quad \bar{n} = \frac{(n_e^{\text{eff}} + n_o)}{2}$$

$$n_e^{\text{eff}} = \frac{n_e n_o}{\sqrt{n_e^2 \cos^2 \theta + n_o^2 \sin^2 \theta}}$$

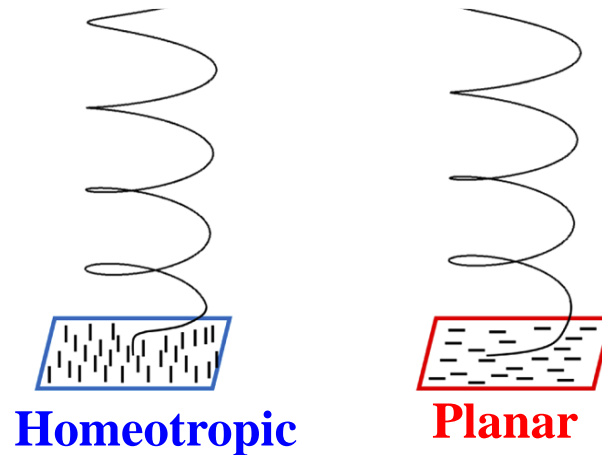
$$\Delta\lambda = \frac{K_{33}^2 E_N P_0 n_o}{2EK_{22}(K_{22} - K_{33})} \left(1 - \frac{n_o^2}{n_e^2}\right) \left(\frac{E_N}{E} - 1\right)$$



$$P = \frac{2\pi}{E} \sqrt{\frac{K_{33}}{\epsilon_0 \Delta\epsilon}}$$

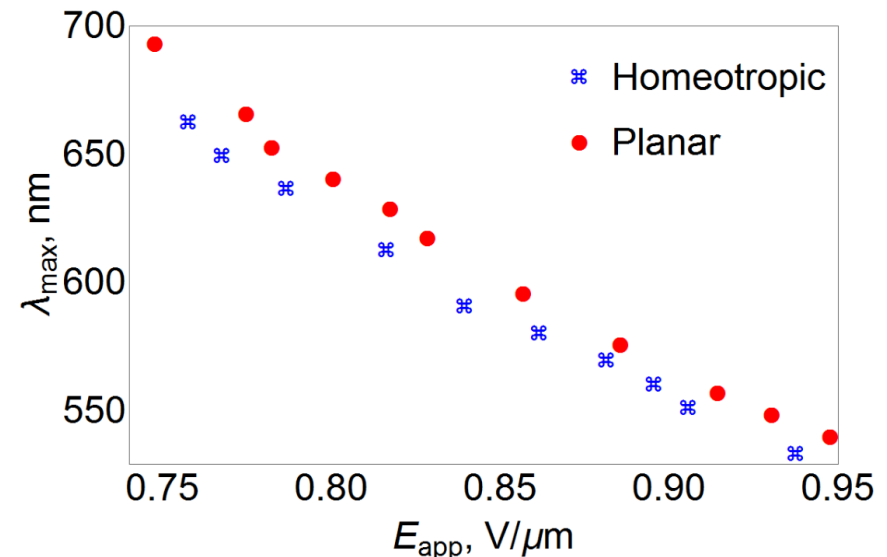
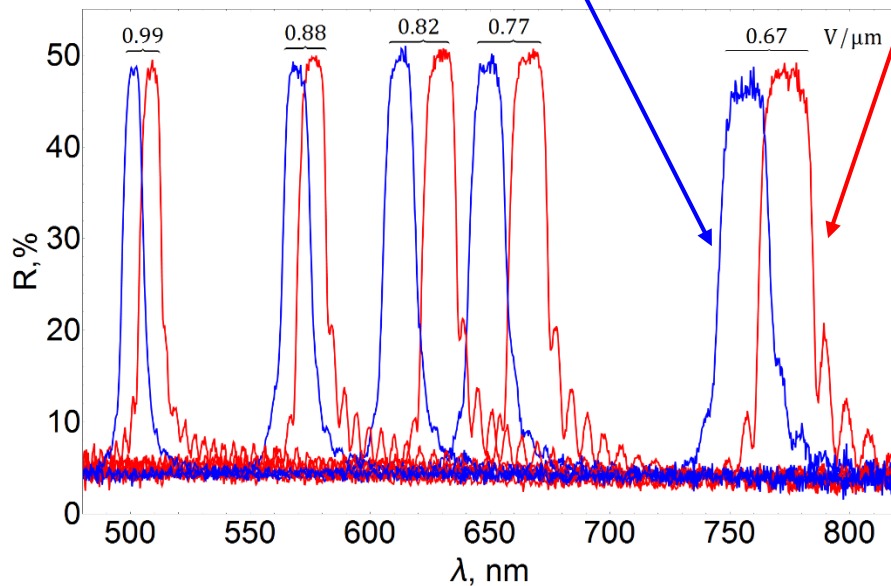
$$\sin^2 \theta = \frac{\kappa}{1 - \kappa} \left(\frac{E_N}{E} - 1\right); \quad \kappa = \frac{K_{33}}{K_{22}}$$

# At constant applied field, reflection wavelength is *different* in planar and homeotropic cells

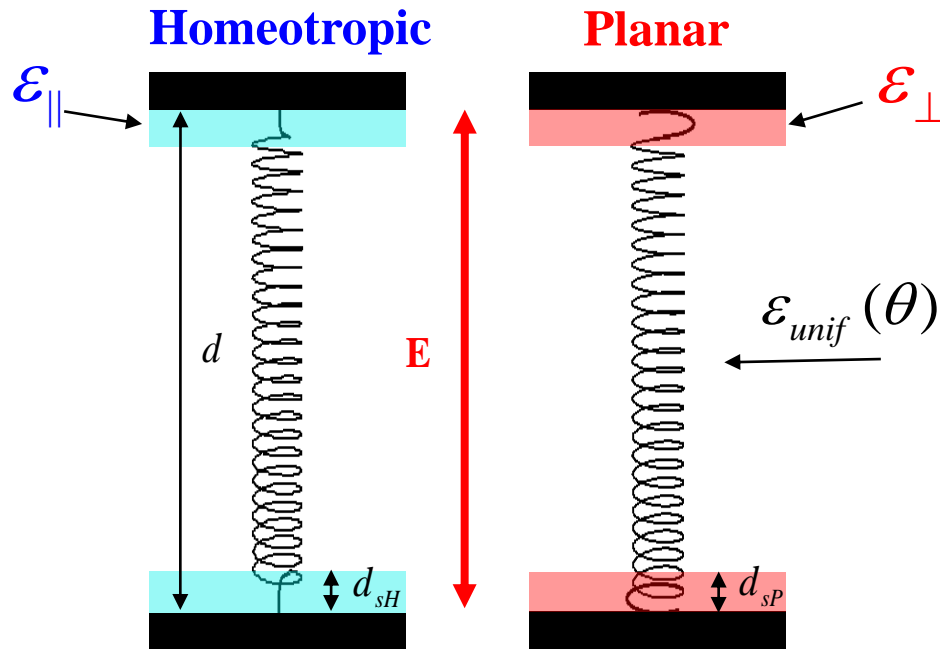


At the same value of the field, spectra in homeotropic  $\text{Ch}_{\text{OH}}$  cells are blue-shifted, and in the planar  $\text{Ch}_{\text{OH}}$  cells are red shifted.

Can be used in sensing applications



# Dielectric properties are not uniform near substrates



$$E_{unif} = \frac{E_{applied}}{1 \pm \text{"correction for } \epsilon_{surface} \text{"}}$$

&

$$\lambda_{Bragg}^{unif} \propto \frac{1}{E_{unif}}$$



$$E_{unif,H} > E_{unif} > E_{unif,P}$$

$$\lambda_{Bragg,H} < \lambda_{Bragg}^{unif} < \lambda_{Bragg,P}$$

$$\langle \epsilon_{surface} \rangle = \frac{\epsilon_{unif} + \epsilon_{\parallel,\perp}}{2}$$

with  $\epsilon_{\parallel} > \epsilon_{unif} > \epsilon_{\perp}$

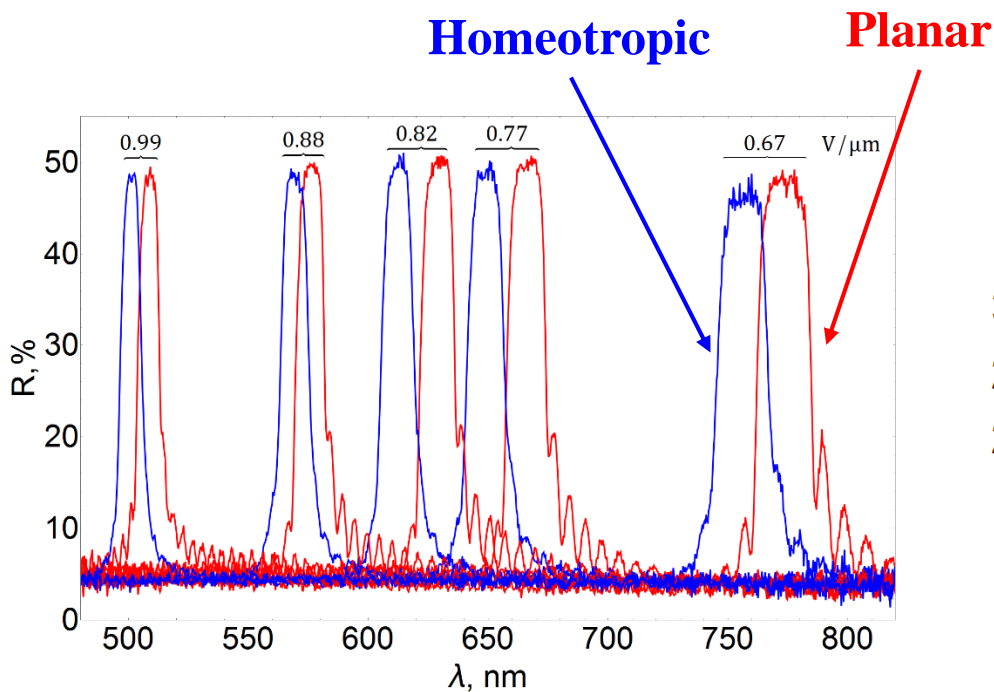
and  $\epsilon_{unif} = \epsilon_{\perp} \sin^2 \theta + \epsilon_{\parallel} \cos^2 \theta$



# Peaks separation is growing towards the red part of spectrum

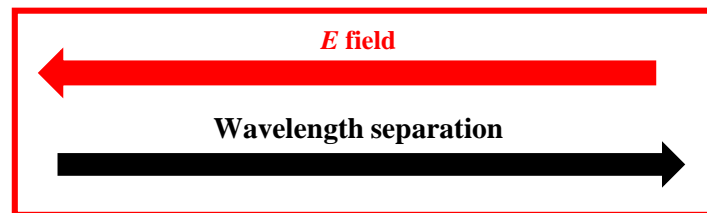
## Experiment

$$\lambda_{\text{Bragg},H} < \lambda_{\text{Bragg},P}$$

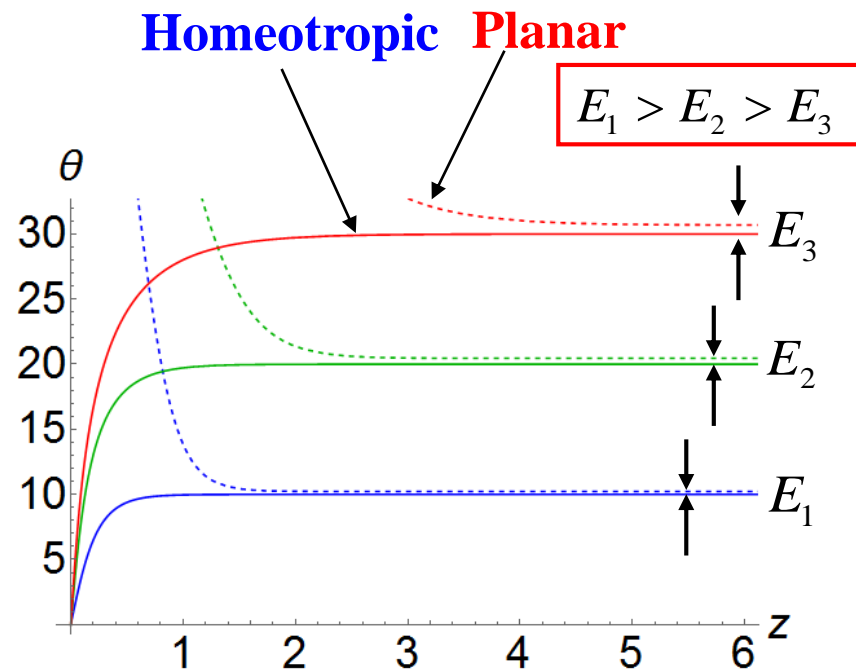


Iadlovská, O.S., et al., *Optics Letters*, 43(8), 1850 (2018).

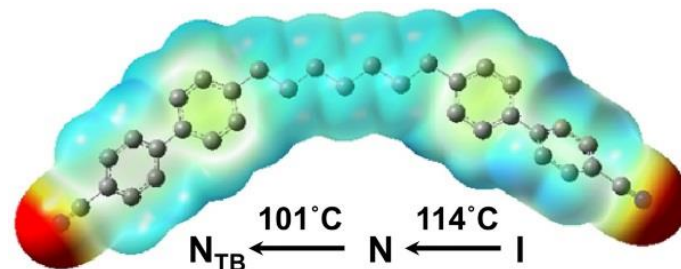
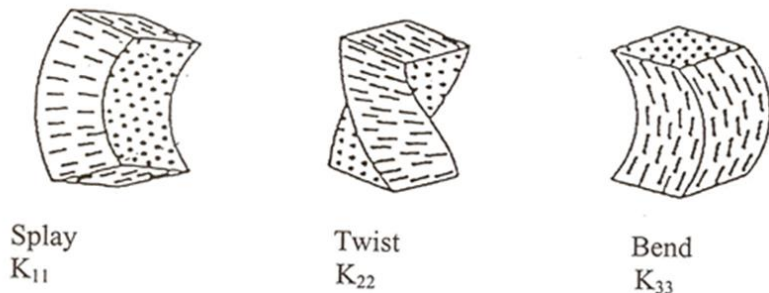
## Simulations



$\text{Ch}_{\text{OH}}$  director model quantifies the director field difference in the two cells

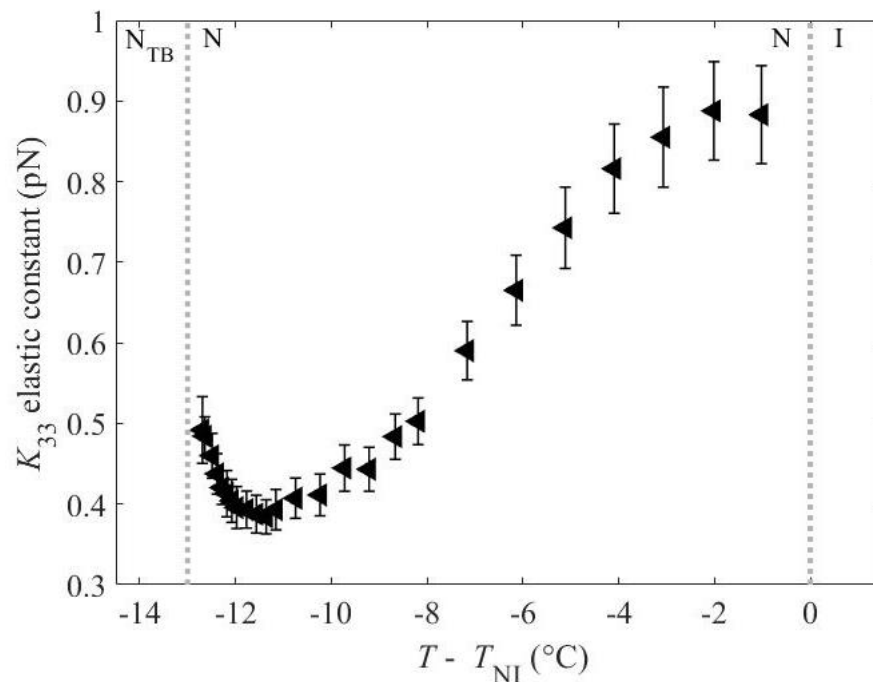
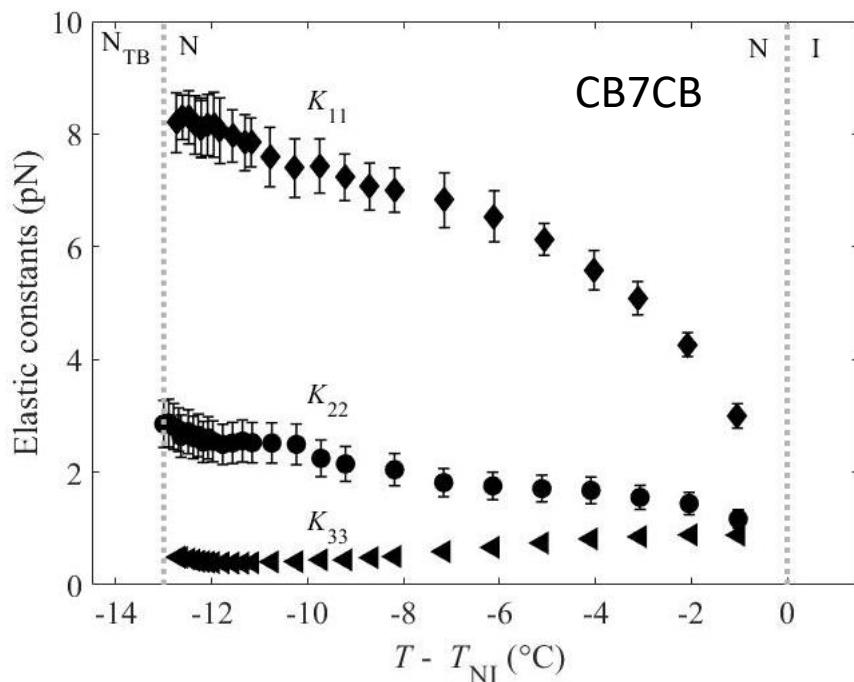


# Elasticity of the flexible dimer CB7CB, the first $N_{tb}$ material



Flexible dimer CB7CB is easy to bend (small  $K_{33}$ )

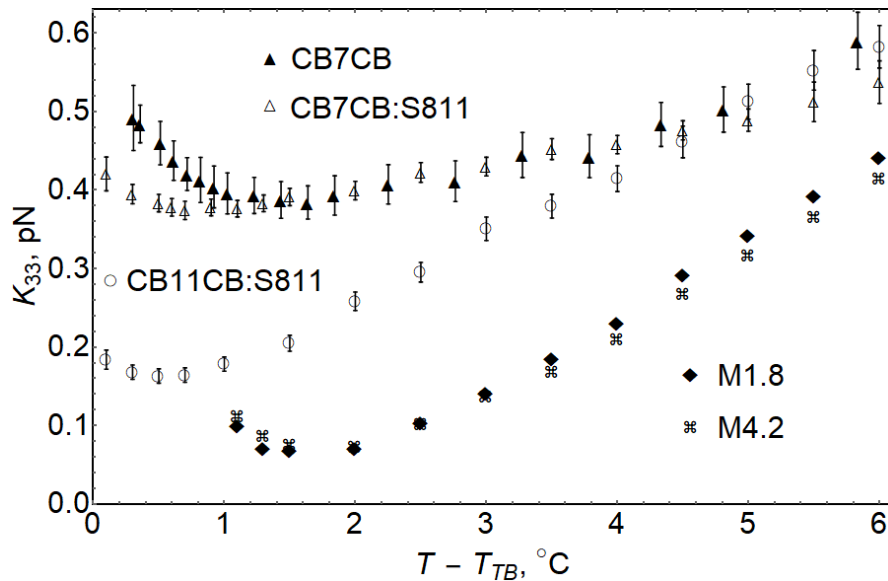
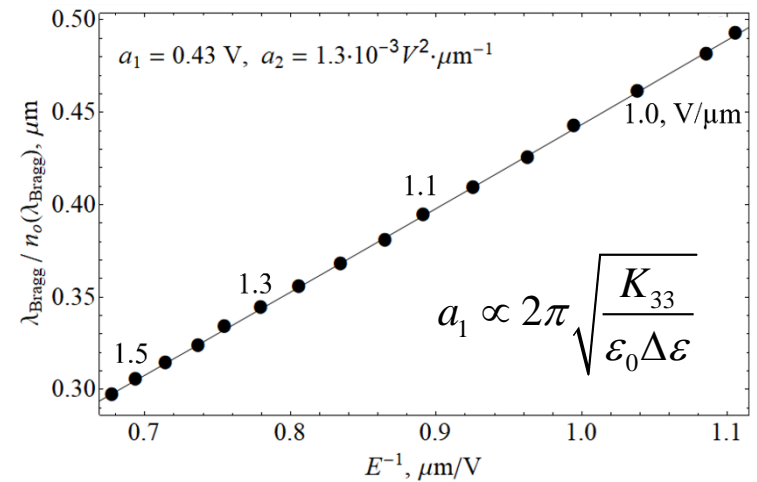
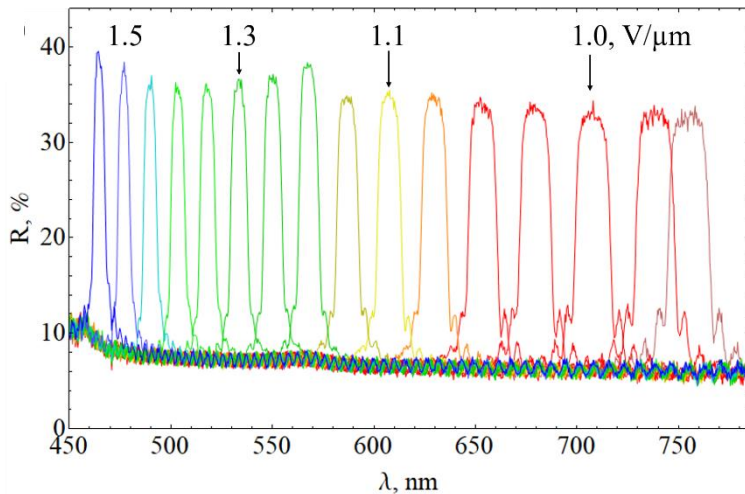
**Elastic constants of Splay  $K_{11}$ , Twist  $K_{22}$ , and Bend  $K_{33}$  measured in nematic phase:**



G. Babakanova, Z. Parsouzi et al, Phys Rev E 96, 062704 (2017)

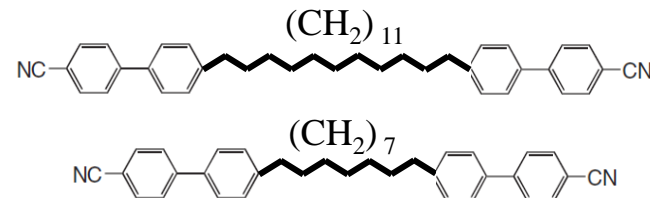
# In-situ measurement of bend elastic constant in Ch

Values of  $K_{33}$  are deduced from the optical spectra.

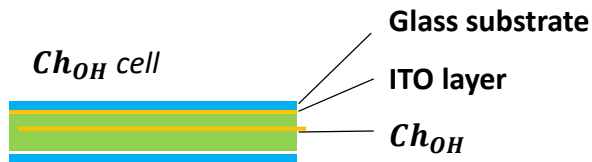


$$\frac{\lambda_{\text{Bragg}}}{n_o} = \frac{2\pi}{E} \sqrt{\frac{K_{33}}{\epsilon_0 \Delta \epsilon}}$$

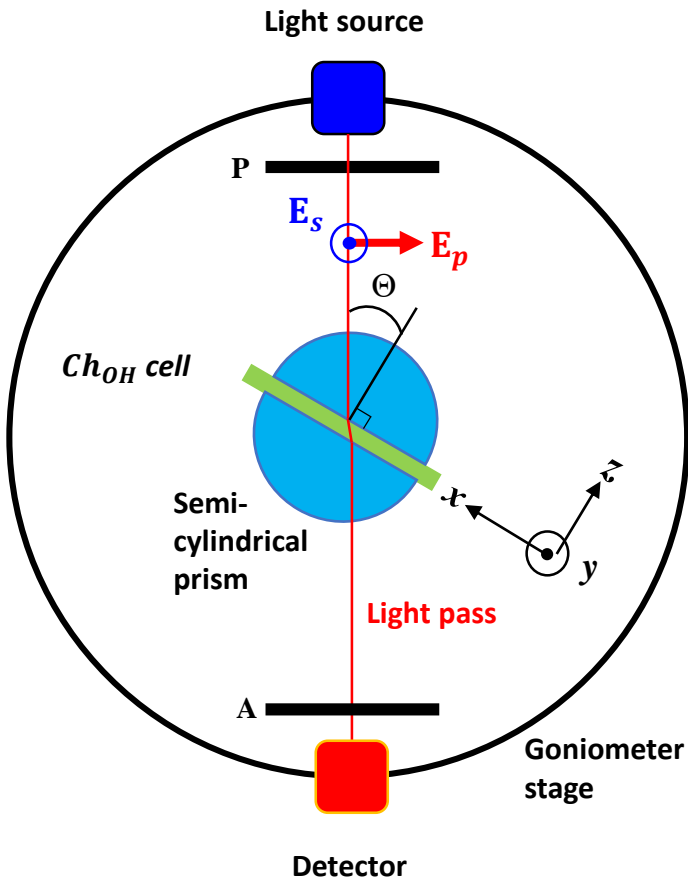
Longer flexible dimer CB11CB has smaller bend modulus as compared to shorter CB7CB molecule.



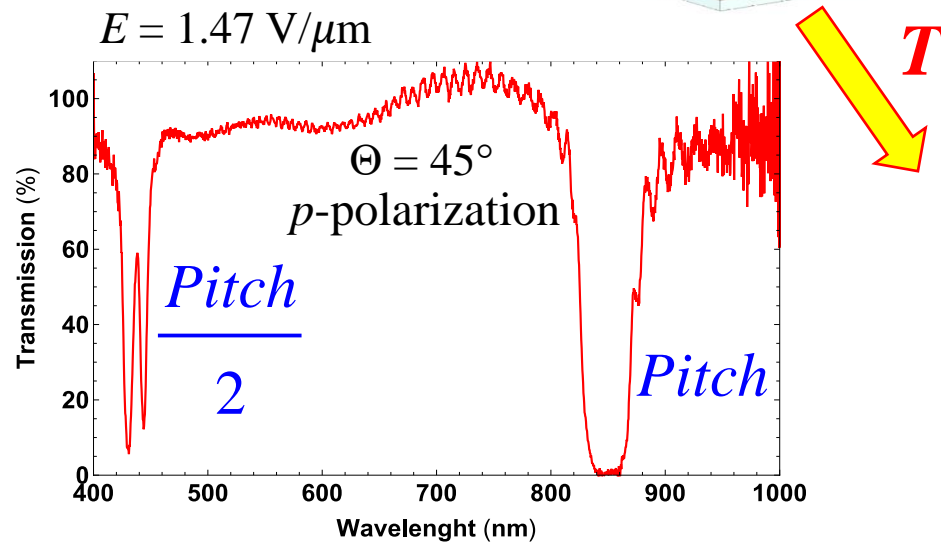
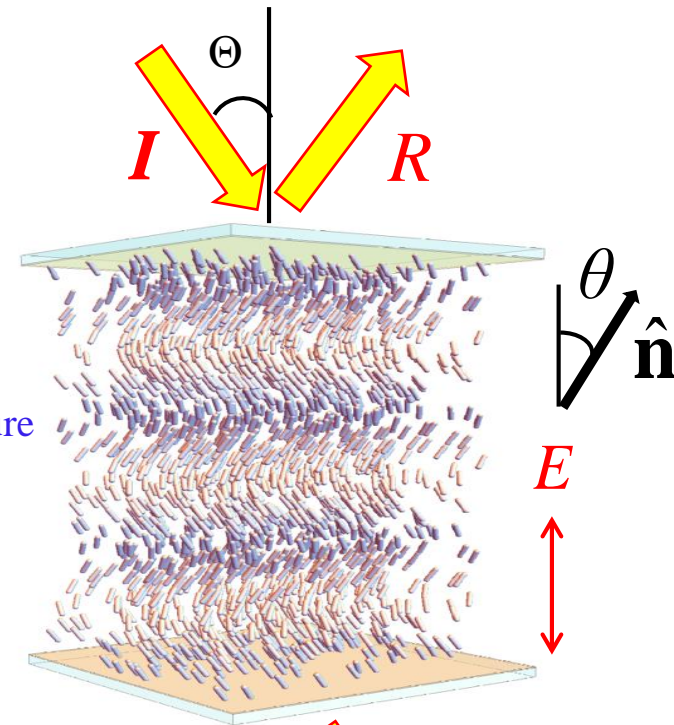
# Oblique incidence at $Ch_{OH}$ structure



Oblique incidence setup  
in transmission mode

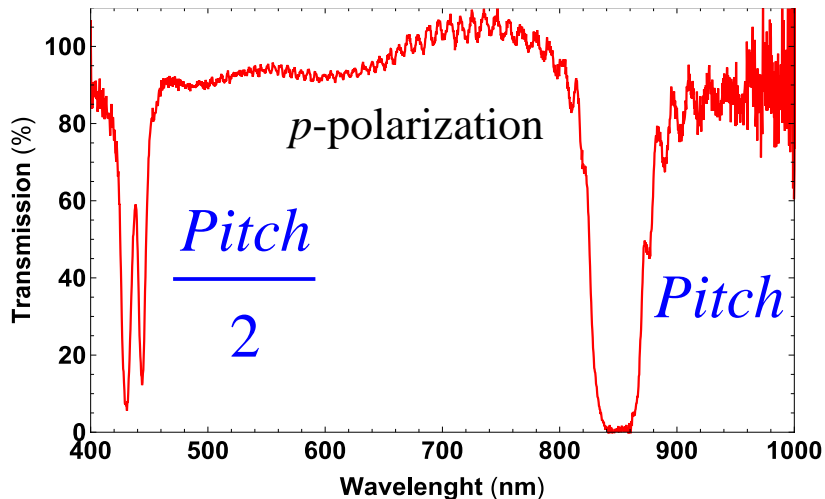


Diffraction from  $Ch_{OH}$  structure  
at oblique incidence of light  
reveals forbidden bands  
associated with the full  
pitch  $P$  and the half-pitch  $P/2$

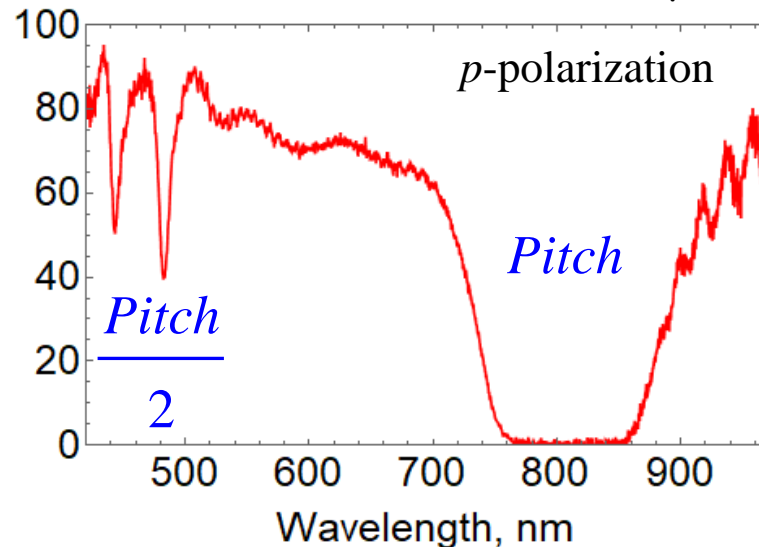


# $E$ - and $\Theta$ -tuned Bragg diffraction at oblique incidence

$\Theta = 45^\circ$        $E = 1.47 \text{ V}/\mu\text{m}$



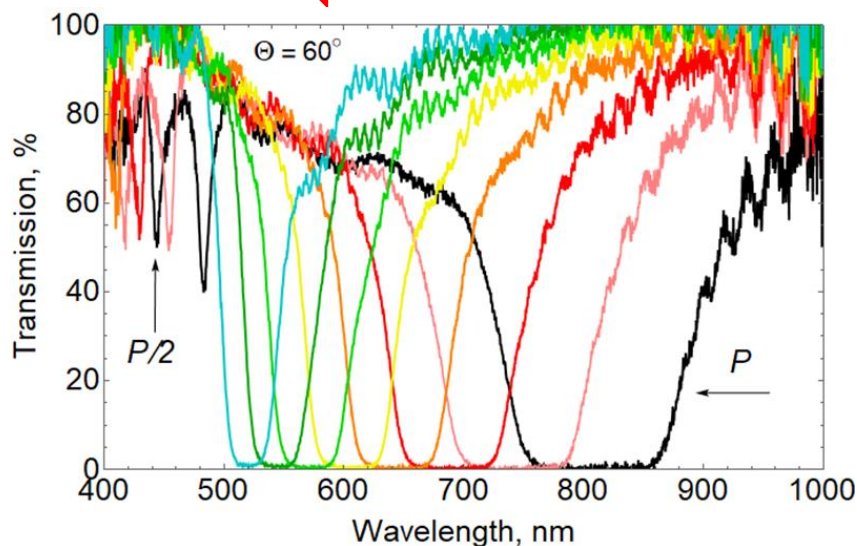
$\Theta = 60^\circ$        $E = 1.11 \text{ V}/\mu\text{m}$



$E$

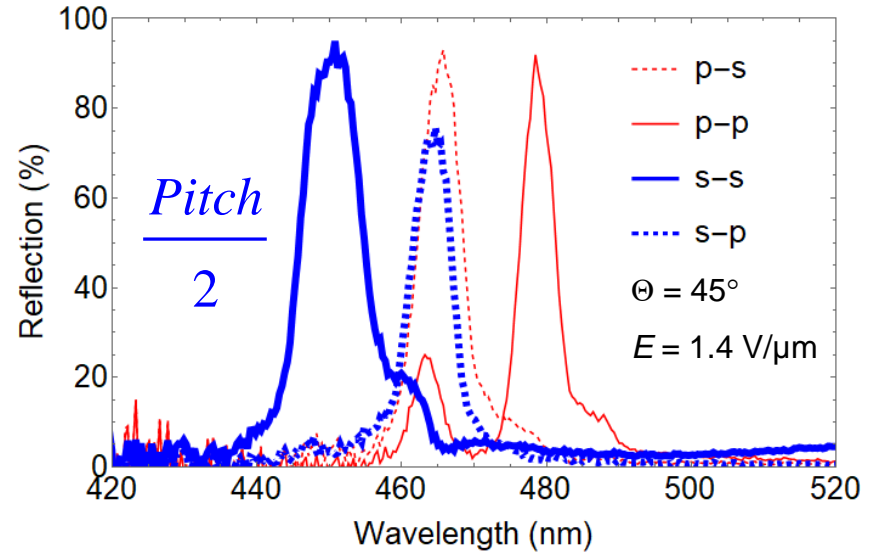
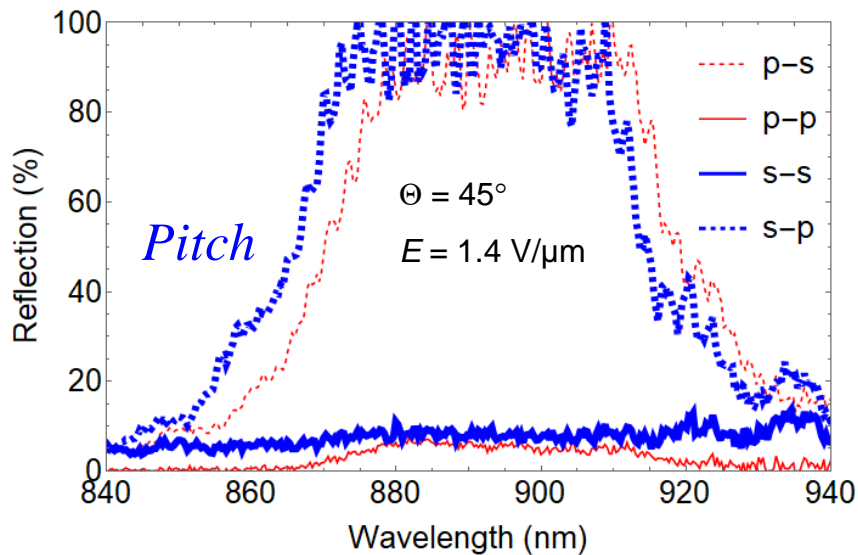
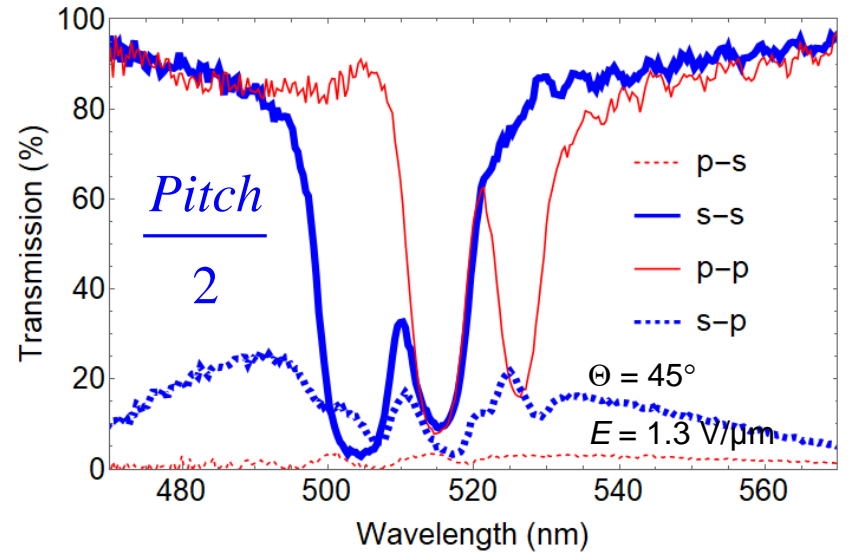
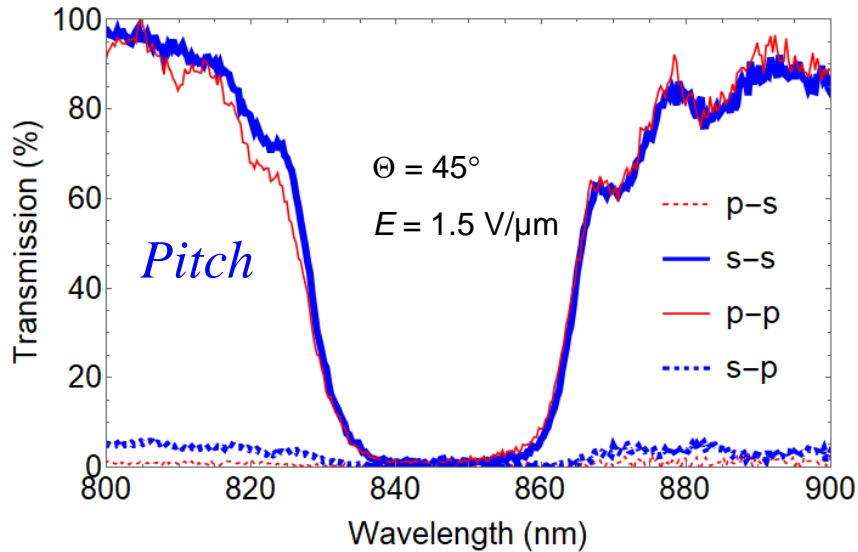


Incidence  $\Theta = 60^\circ$   
 $p$ -polarization



Diffraction at the full pitch  $P$  is characterized by a wide bandwidth and total reflection at a large angles of incidence  $\Theta$

# Oblique incidence: polarization characteristics



The full pitch bandgap is a singlet,  
polarization independent

The half-pitch is a triplet whose lateral peaks are  
polarization dependent, while the central peak is not.

## Summary

- Oblique helicoidal cholesteric ( $\text{Ch}_{\text{OH}}$ ) state is continuously tunable by applied field; the single-harmonic periodicity is preserved
- Bragg reflection from  $\text{Ch}_{\text{OH}}$  is sensitive to the surface alignment: a blue shift of spectra is observed in homeotropic cells and red shift is observed in planar cells
- Bragg spectra at the  $\text{Ch}_{\text{OH}}$  can be used to measure bend elastic constant of the *Ch phase*
- At oblique incidence, diffraction at the half- and full pitch is observed at a varying angle of incidence. Diffraction at the half-pitch is a triplet whose lateral peaks are polarization dependent, while the central peak is not. The full pitch bandgap is a singlet characterized by a wide bandwidth and total reflection at a large angle of oblique incidence

I want to thank my advisors Dr Oleg Lavrentovich and Dr Sergij Shiyakovskii for all their help and guidance, and my colleagues and friends for fruitful discussions and collaboration, as well as our collaborators for supply of the twist-bend materials.



**Graham R Maxwell  
(REU program)**



**Kamal Thapa**

### Synthesis of twist-bend materials:

Quan Li and students Hao Wang, Hari K. Bisoyi, Kent State University, USA

Corrie T. Imrie, and students Daniel Paterson, Grant Strachan and Ewan Cruickshank, University of Aberdeen, Scotland, UK

Georg H. Mehl, Christopher Welch, University of Hull, UK

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