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Development of a Line Source Dispersion Model for Gaseous Pollutants by Incorporating Wind Shear near the Ground Under Stable Atmospheric Conditions

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Abstract: Transportation sources are a major contributor to air pollution in urban areas. The role of air quality modelling is vital in the formulation of air pollution control and management strategies. Many models have appeared in the literature to estimate near-field ground level concentrations from mobile sources moving on a highway. However, current models do not account explicitly for the effect of wind shear (magnitude) near the ground while computing the ground level concentrations near highways from mobile sources. This study presents an analytical model based on the solution of the convective-diffusion equation by incorporating the wind shear near the ground for gaseous pollutants. The model input includes emission rate, wind speed, wind direction, turbulence, and terrain features. The dispersion coefficients are based on the near field parameterization. The sensitivity of the model to compute ground level concentrations for different inputs is presented for three different downwind distances. In general, the model shows Type III sensitivity (i.e. the errors in the input will show a corresponding change in the computed ground level concentrations) for most of the input variables. However, the model equations should be re-examined for three input variables (wind velocity at the reference height and two variables related to the vertical spread of the plume) to make sure that the model is valid for computing ground level concentrations.

Keywords: Line Source; Gaseous Pollutants; Wind shear

1. Introduction

Air pollution can be either from natural sources or man-made sources. Combustion of fossil, biomass, and other non-renewable fuels is the primary contributor to man-made emissions we face today [1]. Nearly more than 55% of people in the world are currently living in urban areas and 68% are projected to live in urban areas by 2050 [2]. Transportation sources such as cars and trucks are extensively used in urban areas to carry out day to day living. Air pollution caused by transportation sources contributes to smog and poor air quality, which have negative impacts on public health [3]. The air pollution impact of transportation sources is studied using either dispersion models or field studies. Air quality modeling helps to establish a relation between the pollution sources and their impacts. The mathematical techniques are used to simulate ground-level concentrations in air quality models. Inputs of air quality modeling include meteorological data, source information, and surrounding terrain [4].

The air quality models are developed to predict the concentrations of current and future situations. Most of the models are developed using the standard input parameters and evaluated

with the real-time experimental data. The main aim of these models is to provide suggestions and ideas about the future air quality condition for the policymakers to make regulatory decisions to protect public health [5]. There are different types of models based on sources (such as point, line, and area sources). Line sources are the models used to calculate and predict the concentration of pollutants that are continuously emitted from the automobiles on highways. The effect of pollution from line sources is high in an urban environment due to their major contribution. Vehicular density, vehicle speed, and emission rate are the major variable to be considered for the prediction analysis of air quality involving mobile sources [6–8]. The air quality models, in general, are divided based on attributes and model category as mentioned in Table 1.

Table 1. The major classification of air quality models based on different model categories [7].

<i>Attributes</i>	<i>Model category</i>
Source	Point, line, area, volume, flare
Receptor	Street Canyon, intersection model
Frame	Lagrangian, Eulerian
Dimensionality	Single, double, triple, or multidimensional
Scale	Microscale and mesoscale, small synoptic, large synoptic, planetary
Structure	Analytical, statistical
Approach	Numerical, experimental
Applicability	Simple terrain, complex terrain, rural flat terrain, urban flat terrain, coastal terrain
Complexity	Screen models, refined models

2. Literature Review

The literature review indicates that many line source air quality models have been developed over the last 50 years. The mathematical formulation of these models is analytical, statistical, or numerical. The solution of the convective-diffusion equation for a line source was available in the 50s [9]. During the 60s and 70s, many Gaussian-based dispersion models were introduced. These formulations were a function of meteorology, receptor locations, and highway geometry. The differences in formulations was due to the assumption made during the solution of the convective-diffusion equation or the specification of plume spread rates. However, these models did not perform very well when the predicted results were compared with the observed values. The primary reason was difficulty in accounting for atmospheric dispersion and turbulence [10]. Subsequently, many experimental field studies were conducted to improve the models.

HIWAY1 was developed in the early '70s to predict mobile source emissions near roadways [11]. In 1978, Chock formulated the GM line source model by incorporating wind speed correction and modified values for vertical dispersion coefficients to address wake turbulence from the vehicles [12]. In 1980, Rao and Keenan evaluated the existing models and suggested new dispersion curves for pollution dispersion near highways [13-14]. Model development continued from the 80s onward to address vehicle induced turbulence, surface roughness, averaging time, new provisions for plume spread, and other turbulence mixing parameters [15].

USEPA Office of Research and Development introduced a CALINE model in 1972 based on the Gaussian plume model using Pasquill-Gifford atmospheric stability classes. CALINE was developed by focusing on the prediction of CO concentration near roadways [16]. In 1975, formulations for depressed roadways were added to develop CALINE2 [17]. In 1979, the vertical and horizontal dispersion curves were updated along with updating vehicle-induced turbulence, averaging time, and introducing a finite line source to develop CALINE3 to reduce over predictions. In 1984, CALINE4 was introduced with the addition of chemistry for NO₂ and PM, intersections, and updating lateral plume spread and vehicle induced turbulence. CALINE, CALINE2, and CALINE3

are open-source models and are available freely to the public, unlike CALINE4 [18]. Around the early '90s, CAL3QHC screening model was developed to auto-estimate the queue lengths of vehicles at the intersections. The enhanced version of CAL3QHC is CAL3QHR, a more flexible model than CAL3QHC with a two-tiered approach [19]. In the same decade, ISCST2 was introduced by the incorporation of mixing height algorithms. It could estimate the concentration of pollutants with varying emissions from point sources. ISCST3 was developed in 1995 by incorporating the new area source option and algorithms of dry deposition [20]. A commonly used line source model CALINE4 uses a range of traffic and fleet characteristics, and a diffusion equation to assess the impacts of a road at a small scale. It is specifically designed for assessing air quality impacts at roadways or intersections and used to predict impacts of changing traffic volumes, signal phasing, or adding additional lanes to a roadway [21]. In New Zealand, a similar model named VEPM is developed, which uses real and lab-based emissions data to predict emissions up to the year 2040 from a roadway [22].

In 1989, Luhar and Patil developed General Finite Line Source Model (GFLSM) based on the Gaussian diffusion equation and evaluated based on data collected at intersections in, Mumbai and New York [23]. Later the GFLSM was improved by Sharma (1999) based on experiments conducted at intersections in Delhi, India [24]. According to Eerens, the CAR model was developed in 1993 and evaluated with the data collected in urban areas of the Netherlands [25]. A road network dispersion model named CAR-FMI was developed like a CAR model to predict concentrations of pollutants from automobiles near industrial areas [26]. ROADWAY model was developed while studying the vehicle wakes and the dispersion phenomena in pollutants from the vehicles [27]. COPERT and CEM are also other major models used to calculate the concentration of pollutants from vehicular emissions [28].

The research has continued to develop, assess, and evaluate the pre-existing models and increase the scope of accuracy for future models. In 2002, Christoffer mentioned that the spread of the pollutant dispersion about the center of mass is non-spherical under shear conditions and the pollution shape reflects the vertical wind shear profile experienced by the puff within 4 hours of the time scale for the point releases [29]. In 2007, Gokhale developed a simple semi-empirical box model based on the 'traffic flow rate' at the busiest traffic road intersections in Delhi. He estimated hourly average carbon monoxide (CO) concentrations and optimized specific vehicle emission rates based on vehicle category. Through this study, he was able to show that the nature of the vehicle flows influences the rate and nature of the dispersion of pollutants which influence pollutant concentration in the road vicinity [30]. In 2018, Milando conducted a study near high traffic roads in Detroit. He evaluated the RLINE by comparing predicted concentrations of NO_x, CO, and PM_{2.5}. The model performance for CO and NO_x was found to be best at sites close to major roads, during downwind conditions, during weekdays, and in certain seasons [31]. In 2018, Bowatte investigated longer-term effects of traffic-related air pollution exposure for individuals with or without existing asthma, and with or without lower lung function. Middle-aged adults who are living less than 200m for a major road influence both the development and persistence of asthma. These findings have public health implications for asthma prevention strategies in primary and secondary settings [32]. In 2011 Xie conducted a research study on both the daily and hourly concentration levels of CO, PM₁₀, NO₂, and O₃ during the Beijing Olympic Games and conformed to the Grade II China National Ambient Air Quality Standards. A notable reduction of concentration levels was observed in different regions of Beijing, with the traffic-related air pollution in the downwind northern and western areas. According to Xie, "TRS policy was therefore effective in alleviating traffic-related air pollution and improving short-term air quality during the Beijing Olympic Games"[33]. In 2018, Liang conducted a dorm room inhalation study due to vehicle emissions using a near-road monitor as a surrogate for true exposure and observed acute health effects. This study was conducted near-road measurements of several single traffic indicators at six indoor and outdoor sites. [34]. Later in 2020, Amoatey made a comparative study between COPERT and CMEM models. The correlation coefficient for these two models was found to be statistically significant from 0 in the case of combined model comparison

across all the traffic locations for both CO and NO_x. He concluded that due to the terrain features of certain roads, weak performance is observed and needs to be considered in future study [35].

In 2005, the USEPA replaced the ISC model with AERMOD which contains an updated atmospheric stability scheme and the ability to characterize the Planetary Boundary Layer through both surface and mixed layers. The latest line source model RLINE is being incorporated in AERMOD by the USEPA [36]. Some of the popular air quality models related to transportation sources and their key features are mentioned in Table 2.

Table 2. Various popular air quality models and some of their key features.

<i>Model</i>	<i>Some Key features</i>
GFLSM	<ul style="list-style-type: none"> ◦ Better performance with a finite length line source. ◦ Any orientation of wind direction with roadways can be used. ◦ No constraint on infinite line source. ◦ Used for both gaseous pollutants and particulate matter. ◦ Effectively predicts the pollutant concentration near intersections.
CAL3QHR	<ul style="list-style-type: none"> ◦ Allowed for refined analyses. ◦ Processes up to a week of hourly data from the input file. ◦ Used in both rural and urban conditions. ◦ Calculates the 9 highest 8-hour running average concentrations for each receptor.
COPERT	<ul style="list-style-type: none"> ◦ National, regional, or local scale emissions are computed and especially when a particular vehicle type is ‘artificially’ promoted or discouraged from circulation. ◦ Includes all main pollutants (e.g.: greenhouse gases, air pollutants, and toxic species). ◦ All relevant road vehicle operation mode emissions are estimated. ◦ Choice of the calculation method. ◦ Non-exhaust emissions such as fuel evaporation from vehicles are not included.
CALINE4	<ul style="list-style-type: none"> ◦ Can predict concentrations of pollutants for receptors within 500 meters of the roadway and includes a mixing zone concept. ◦ Special options for intersections, street canyons, and parking facilities are available. ◦ Can predict gaseous pollutants and suspended pollutants as well. ◦ More flexibility in terms of input parameter complexity. ◦ Easy to implement the model and various options for additional input parameters.
AERMOD	<ul style="list-style-type: none"> ◦ Use stack tip downwash, gradual plume rise, buoyancy-induced dispersion, and calms-processing routines. ◦ Calculate wind profiles and vertical potential temperature gradients. ◦ Incorporated line source modeling option.

The literature review indicates that available line source dispersion models do not account for wind shear near the ground explicitly under different atmospheric conditions. Therefore, this study is focused on developing a line source dispersion model considering the wind shear near the ground under stable conditions. The model is applied to gaseous pollutants released from mobile sources on a highway. This paper presents a line source model (SLINE) by incorporating wind shear near the ground surface to predict the impact of mobile sources moving on a highway in nearby areas during stable atmospheric conditions. The sensitivity analysis is performed by considering the selected variables in the model which have an impact on the computed concentrations.

3. SLINE Model Development

The basic approach to develop this model is the incorporation of wind shear during the dispersion from a line source using the convective-diffusion equation. It is important to consider the variation of the wind velocity magnitude near the ground for the dispersion of pollutants released from the tailpipe of mobile sources. This physical phenomenon is incorporated in the derivation of the dispersion and transport equation for the SLINE model. The model is based on the analytical solution of the convective-diffusion equation of a line source given in the book by Sutton [9]. The assumptions used in deriving the equation are: (i) the wind direction is always perpendicular to the highway, (ii) the dispersion is of the non-fumigation type, (iii) the velocity profile with height above the ground level is assumed to be the same for all downwind distances, (iv) a power-law profile is assumed for the velocity i.e. the magnitude of the wind velocity near the ground level changes rapidly and follows a power law, and (v) the eddy diffusivity profile is a conjugate of velocity profile as given in Equation (3) below.

3.1. Dispersion model

The analytical solution of the convective-diffusion equation to calculate the concentration of pollutants at any downwind distance is given by Equation (1):

$$C_{(x,z)} = \frac{q}{u_1 * \gamma(s)} * \left[\frac{u_1}{(m-n+2)^2 * K_1 * x} \right]^s * \exp \left[-u_1 * \frac{z^{m-n+2}}{(m-n+2)^2 * K_1 * x} \right] \quad (1)$$

where, C is the concentration of pollutants at a point (x, z), x is the downwind distance, z is the vertical height of the receptor above the ground, q is the emission rate of the mobile source per unit length, m and n are the exponents of power-law velocity profile and eddy diffusivity profile respectively, s is the stability parameter based on m and n, u_1 and K_1 are the wind velocity and eddy diffusivity at a reference height z_1 respectively (see Equations (2) and (3)), and $\gamma(s)$ is the gamma function of s.

The velocity and eddy diffusivity profiles are:

$$u = u_1 * \left(\frac{z}{z_1} \right)^m \quad (2)$$

$$K = K_1 * \left(\frac{z}{z_1} \right)^n \quad (3)$$

The value of u_1 is based on the measurement and K_1 is computed using the Equation (4) used by Rao *et al* [37]; Nimmatoori and Kumar *et al* [38].

$$K = \left(\frac{\sigma_z^2 u}{2x} \right) \quad (4)$$

The Equations (4) and (3) indicate that K as well as K_1 is a function of downwind distance x. However, the derivation of Equation (1) assumes that K is constant as the plume moves downwind. It is assumed during the application of Equation (1) that the concentration is predicted in the SLINE model at a downwind distance by updating the value of K_1 in the model for that downwind distance. It is expected that this approach will improve the model performance.

3.2. Turbulence Parametrization

The vertical spread for stable conditions for low-level sources is based on theoretical considerations and experimental data and is given by Snyder *et al* [39] as Equation (5).

$$\sigma_z = a * \frac{x u_*}{U_e} * \frac{1}{\left(1 + b_s \frac{u_*}{U_e} \left(\frac{x}{L}\right)^{\frac{2}{3}}\right)} \quad (5)$$

where, U_e is the effective wind velocity, u_* is the surface friction velocity, and L is the Monine-Obukhov length. The formulation for $U_{\bar{z}}$, U_e , σ_v , and \bar{z} are provided in Equations (2), (6), (7), and (8) respectively. Equations (6), (7), and (8) are from Snyder et al [39]. The values for a and b_s are 0.3 and 3 taken from Snyder's RLINE formulation [39].

$$U_e = \sqrt{2\sigma_v^2 + U_{(\bar{z})}^2} \quad (6)$$

$$\sigma_v = \sqrt{(0.6w_*)^2 + (1.9u_*)^2} \quad (7)$$

$$\bar{z} = \sigma_z \sqrt{\frac{2}{\pi}} \exp\left[-\frac{1}{2} \left(\frac{z_s}{\sigma_z}\right)^2\right] + z_s \operatorname{erf}\left(\frac{z_s}{\sqrt{2}\sigma_z}\right) \quad (8)$$

$U_{\bar{z}}$ velocity is the wind velocity at the reference height \bar{z} , z_s is the height from the ground surface to the tailpipe (emission source) of the mobile source.

However, the vertical spread in the current model incorporates the additional spread (m_t) due to the turbulence created by moving vehicles. Then, the modified equation used to calculate σ_z is given in Equation (9).

$$\sigma_z = \frac{a u_* x}{U_e * \left(1 + b_s \frac{u_*}{U_e} \left(\frac{x}{L}\right)^{\frac{2}{3}}\right)} + m_t \quad (9)$$

m_t is assumed equal to 50% of the effective height of the mobile sources on the highway.

For the current model $\sigma_v = 1.9u_*$ because the convective velocity scale w_* for stable conditions is approximately 0 since the heat flux is either very small or zero. An expression of K_1 is obtained as follows by substituting Equation (9) in Equation (4) with the help of Equation (3):

$$K_1 = \frac{\sigma_z^2 u_1}{2x} = \left[\frac{a u_* x}{u_1 + b_s u_* \left(\frac{x}{L}\right)^{\frac{2}{3}}} + m_t \right]^2 * \frac{u_1}{2x} \quad (10)$$

Substitute Equation (10) in Equation (1) to obtain Equation (11), which represents the final developed concentration equation for the SLINE line source dispersion model. Equation (11) is used in the calculation of the downwind concentrations.

$$C = \frac{q}{u_1 * \gamma(s)} * \left[\frac{u_1}{(m-n+2)^2 * \left[\frac{a u_* x}{u_1 + b_s u_* \left(\frac{x}{L}\right)^{\frac{2}{3}}} + m_t \right]^2 * \frac{u_1}{2}} \right]^s * \exp \left[-u_1 * \frac{z^{m-n+2}}{\left((m-n+2)^2 * \left[\frac{a u_* x}{u_1 + b_s u_* \left(\frac{x}{L}\right)^{\frac{2}{3}}} + m_t \right]^2 * \frac{u_1}{2} \right)} \right] \quad (11)$$

3.3. Input data

A case study is considered in this paper for the calculation of carbon monoxide (CO) emissions near the ground surface under stable atmospheric conditions. The line source model (SLINE) is used. The model inputs are: the traffic density is 8000 vehicles/hour, the average vehicle speed is 40 miles per hour, the average emission rate is 0.02 g/veh./s, the number of vehicles per meter is 0.125, the line source emission rate (q) of pollutants is 0.025g/m-s, the wind velocity (u_1) is 1.4 m/s, the exponents of power-law velocity profile (m) and eddy diffusivity profile (n) are 0.3 and 0.7 respectively, the

stability parameter (s) based on m and n is 0.813, the convective velocity scale (w_*) for stable conditions is approximately 0 due to very low heat flux, the value lateral turbulent wind component (σ_v) is 0.095m/s, the average height of the mobile sources on the highway is 1.65m, the coefficients a , b_s , and d_s are 0.57, 3, and 2.5 respectively, Monine-Obukhov length (L) value is 134m, the surface friction velocity (u_*) is 0.05m/s, and the average height from the ground surface to the tailpipe of the mobile sources (z_s) is 0.5m. The spread due to mobile turbulence (m_t) is 0.825m.

In the next section, the sensitivity analysis is performed with the above input values for the base case.

4. Sensitivity Analysis

The sensitivity analysis is the quantification of uncertainty in the output of a model (concentration in this study) based on its inputs. There are many techniques to perform sensitivity analysis. In this study, the sensitivity analysis is performed on the current model using the ASTM Guide technique (1994) [40]. The sensitivity of a model to a variable is classified into four categories, namely Type I, Type II, Type III, and Type IV (see Figure 1 and Table 3).

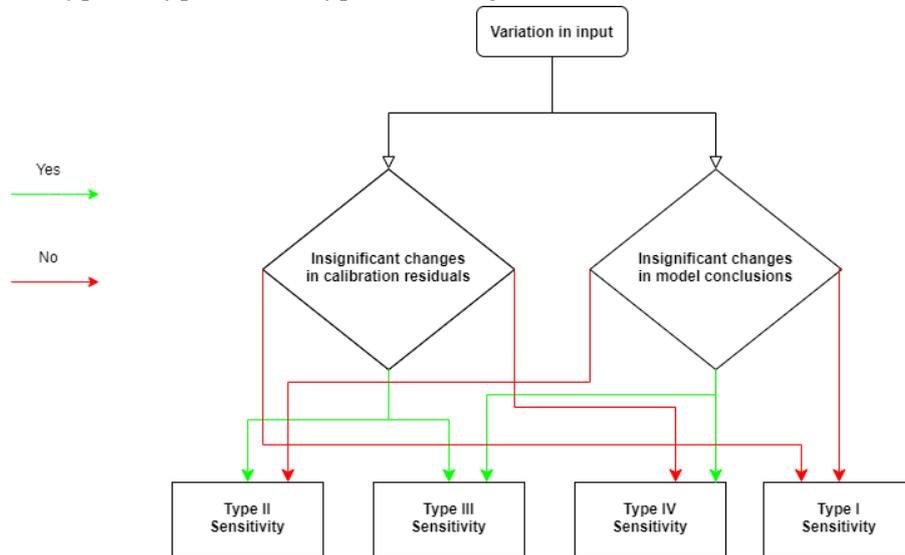


Figure 1. Flowchart represents the four types of sensitivity analyses.

Table 3. The categories' sensitivity analysis and output changes.

	Categories	Changes in calibration residuals	Changes in model conclusions
Variation in input parameters	Type I	X	X
	Type II	✓	X
	Type III	✓	✓
	Type IV	X	✓

Note: ✓- Indicates that there are a change and X- Indicates that there is no change.

The following steps are followed to complete the sensitivity analysis. Initially, different input parameters were varied to identify the potential sensitive parameters. In the current study q , u_1 , u_* , m , a , b_s , and m_t are identified parameters to perform the sensitivity analysis. A summary of the ranges for each parameter is given in Table 4.

Table 4. Ranges of the independent input variable used for the sensitivity analysis.

Run. S.No.	Emission rate of pollutants q (g/m/sec)	Wind velocity u_1 (m/s)	Coefficient m	Surface friction velocity u_* (m/s)	Coefficient a	Coefficient b_s	Vertical spread due to the height of the vehicle m_t (m)
1	0.0001	0.9	0.25	0.03	0.32	2.04	0.6
2	0.0024	1.2	0.32	0.04	0.4	2.56	0.7
3	0.003	1.5	0.4	0.06	0.5	3.2	0.8
4	0.0036	1.8	0.48	0.07	0.6	3.84	0.9
5	0.0043	2.1	0.57	0.08	0.72	4.6	1

The simulations are executed for each input run varying the variables in the considered range as given in Table 4. The values are selected based on the possible errors in the specification of each variable. The model calibration values and the predicted output results are generated by running the model. The difference between the predicted output results and the base values are the residuals. The residuals are derived by comparing calculated output results and the output concentration values for the base case input values. The base case input values considered are given in Table 5.

Table 5. Standard input values considered for sensitivity analysis.

q (g/m/sec)	u_1 (m/s)	m	u_* (m/s)	a	b_s	m_t (m)
0.0025	1.4	0.57	0.05	0.3	3	0.825

The residuals are calculated at three different distances 10m, 50m, and 250m. The graphs are plotted by comparison of variation of input parameters in the considered ranges with the residuals and model conclusions output values. Each variable input parameters are varied to see the change in concentrations for a given downwind distance. The graphs (Figures 2 to 8) represent the variation in concentration with considered independent variables. The sensitivity analysis for the emission rate of pollutants q , wind velocity u_1 , the coefficient a , coefficient b_s , vertical spread due to the wake caused by the vehicle m_t , surface friction velocity u_* , respectively. The type of sensitivity (Type I, Type II, Type III, and Type IV) is determined for each variable parameter depending on changes to the residual values and model conclusion output values. The results are compared and discussed in the results section.

5. Results

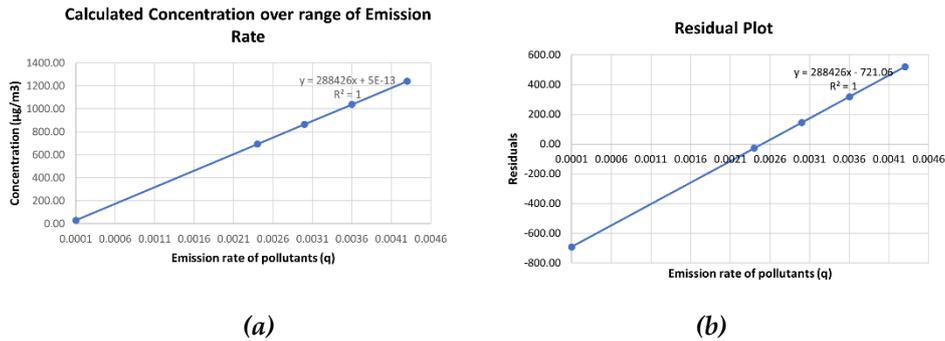
The variable parameters considered in the sensitivity analysis are emission rate of pollutant (q), wind velocity at the reference height (u_1), coefficient a , coefficient m , coefficient b_s , surface friction velocity (u_*), and additional vertical spread due to the turbulence created by the vehicles (m_t). The parameters are vital in describing the sensitivity of the gaseous dispersion model. The plots given in the following figures between the modeled outputs and residuals determine the type of sensitivity for each parameter.

The sensitivity of model output to the emission rate of pollutants (q):

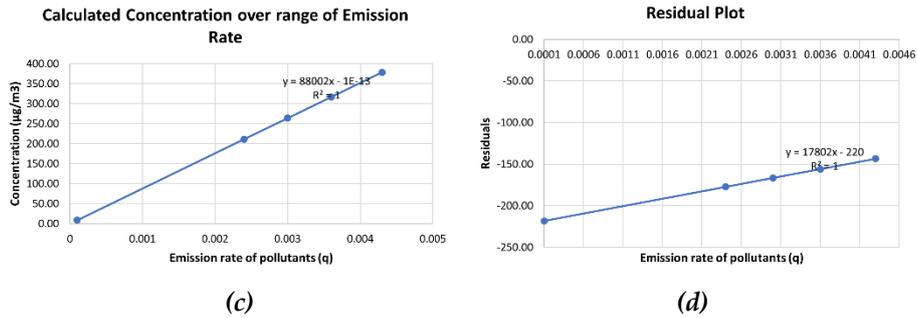
The graphs are plotted in Figure 2 for the computed concentrations and residuals for three downwind distances. The base case value for emission rate of CO (q) is 0.0025g/m/sec. The plots 2a, 2c, and 2e represent the variation in concentrations, and plots 2b, 2d, and 2f represent residual plots. In the plots between the emission rate of pollutants and output concentrations for each downwind

distance, it was observed that the output concentrations increase with an increase in emission rate, as expected. The slope equations and the R^2 values for a linear fit are mentioned in Figure 2. The calculated concentration and residuals varied with the changes in the input parameter. Significant changes are observed in model conclusions and model residuals at 10m and 250m and show Type III sensitivity (see plots 2a, 2b, 2e, and 2f). At 50m, a significant change in the model conclusions is observed but the change in calibration results may not be significant (see plots 2c and 2d). These characteristics may lead to Type IV sensitivity instead of Type III sensitivity at 50m.

At Distance = 10m



At Distance = 50m



At Distance = 250m

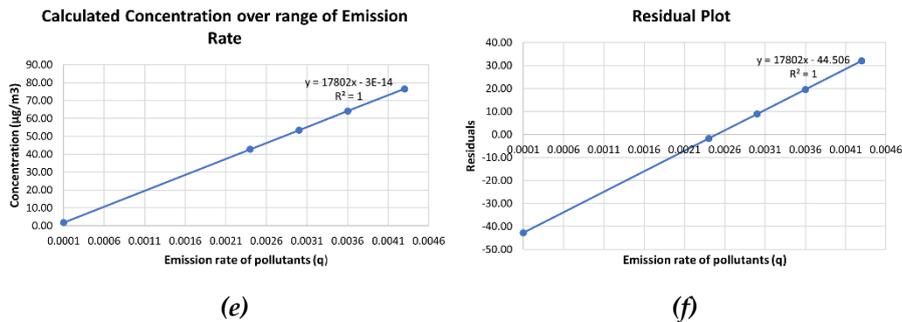


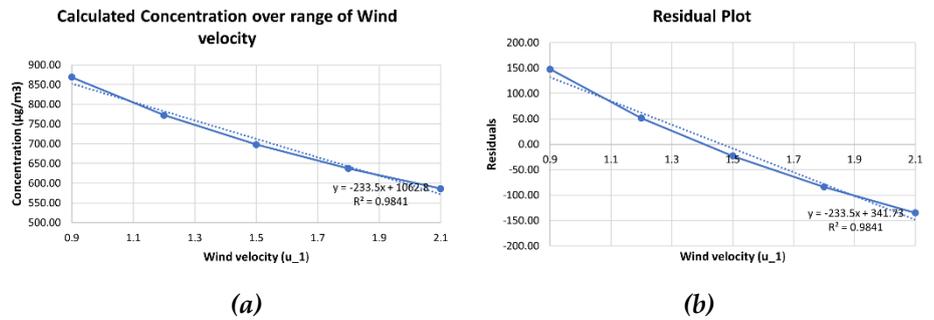
Figure. 2. Variation of concentration with emission rate of pollutants

The sensitivity of model output to wind velocity u_1 :

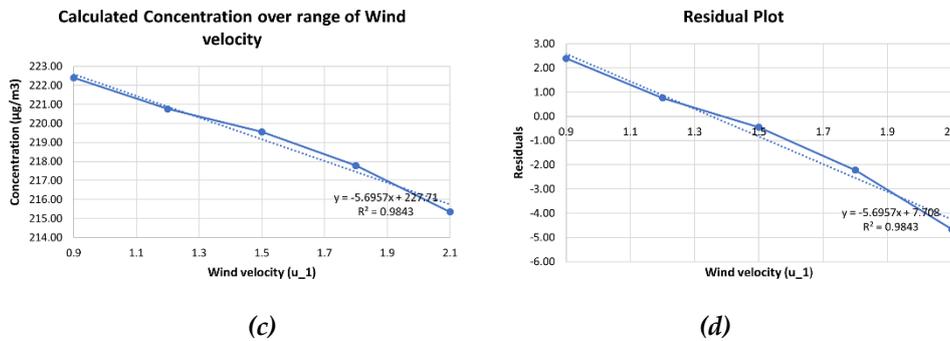
The graphs for the computed concentrations and residuals for three downwind distances are given in Figure 3. The base case value for wind velocity considered is 1.4 m/s. The plots 3a, 3c, and 3e represent the variation in concentrations, and 3b, 3d, and 3f represent residual plots. These plots show that output concentrations decrease with an increase in wind velocity. There is a slight increase in the concentration as wind velocity increases at 250m downwind distance and it is difficult to explain the increase in concentration with wind velocity. However, the concentrations are decreasing for a given downwind distance for a wind velocity run. The slope equations and the R^2 values for a linear fit are mentioned in plots in Figure 3. Significant changes are observed in model conclusions

and model residuals at 10m. At 50m no significant changes are observed in model conclusions but there are changes in calibration residuals. Moreover, no significant changes in model conclusions and residuals are observed at 250m. These characteristics show that the model is exhibiting Type III sensitivity at 10m, Type II sensitivity at 50m, and Type I at 250m downwind distances. The model equations should be reexamined to check the sensitivity results.

At Distance = 10m



At Distance = 50m



At Distance = 250m

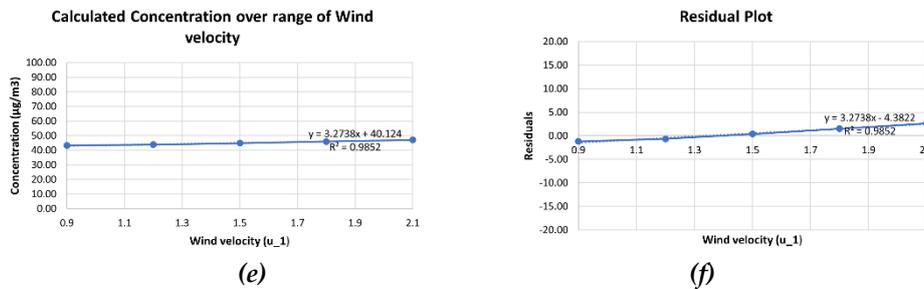
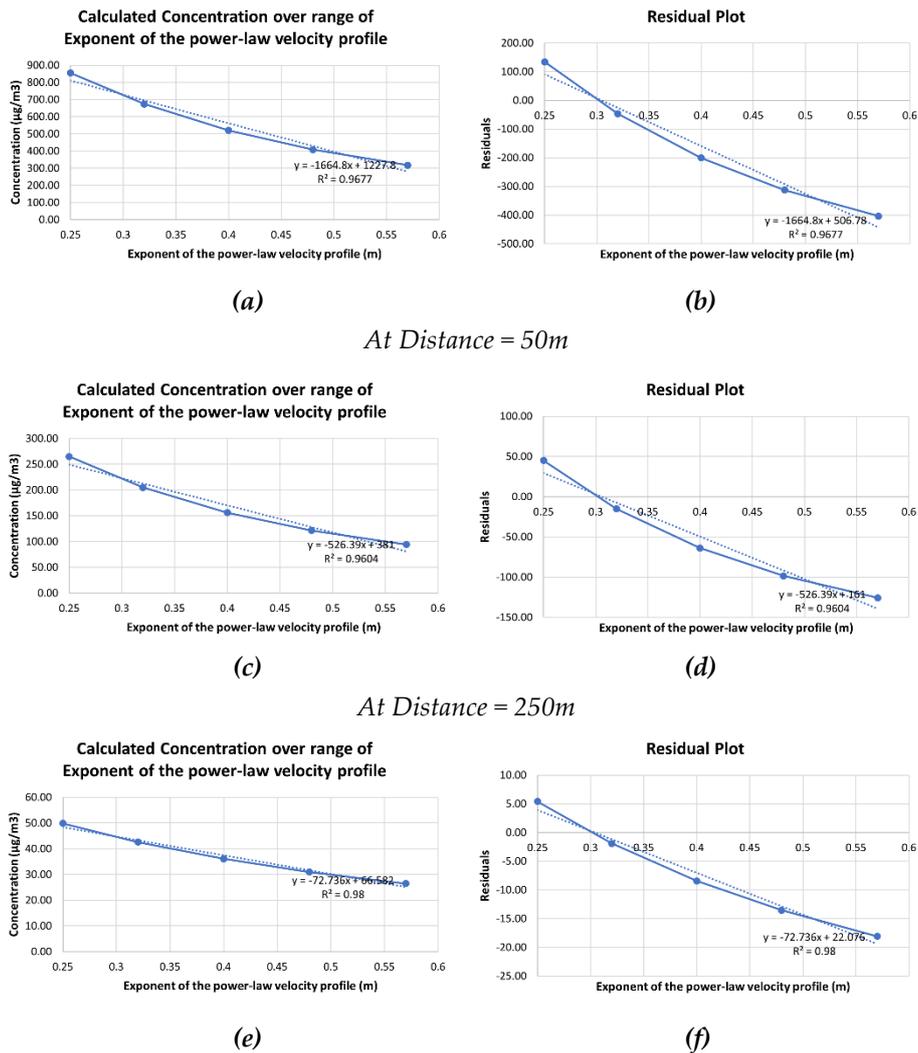


Figure 3. Variation of concentration with wind velocity

The sensitivity of model output to the exponent of power-law velocity profile (m):

The graphs are plotted in Figure 4 for the computed concentrations and residuals for three downwind distances. The base case value for the exponent of the power-law velocity profile (m) considered is 0.3. The plots 4a, 4c, and 4e represent the variation in concentrations, and plots 4b, 4d, and 4f represent residual plots. In the plots between the exponent of the power-law velocity profile and output concentrations for different distances, it was observed that the output concentrations decrease with an increase in the exponent of the power-law velocity profile. The slope equations and the R^2 values for a linear fit are mentioned in plots in Figure 4. Note that the calculated concentration and residuals varied significantly in all cases. Overall, it was observed that there are significant changes in the model conclusions and residuals at 10m, 50m, and 250m. These characteristics show Type III sensitivity to the exponent of the power-law velocity profile at each downwind distance considered.

At Distance = 10m



At Distance = 50m

At Distance = 250m

At Distance = 10m

Figure 4. Variation of concentration with the exponent of the power-law velocity profile (m)

The sensitivity of model output to Surface friction velocity (u_*):

The graphs are plotted in Figure 5 for the computed concentrations and residuals for three downwind distances. The base case value for surface friction velocity (u_*) considered is 0.05m/s. The plots 5a, 5c, and 5e represent the variation in concentrations, and plots 5b, 5d, and 5f are for residual plots. In the plots between the surface friction velocity (u_*) and output concentrations for each downwind distance, it was observed that the output concentrations decrease with an increase in surface friction velocity. The slope equations and the R^2 values for a linear fit are mentioned in plots in Figure 5. The calculated concentrations and residuals varied significantly. Thus, the model conclusions and residuals change significantly as the values of friction velocity changes. This model shows Type III sensitivity due to surface friction velocity (u_*).

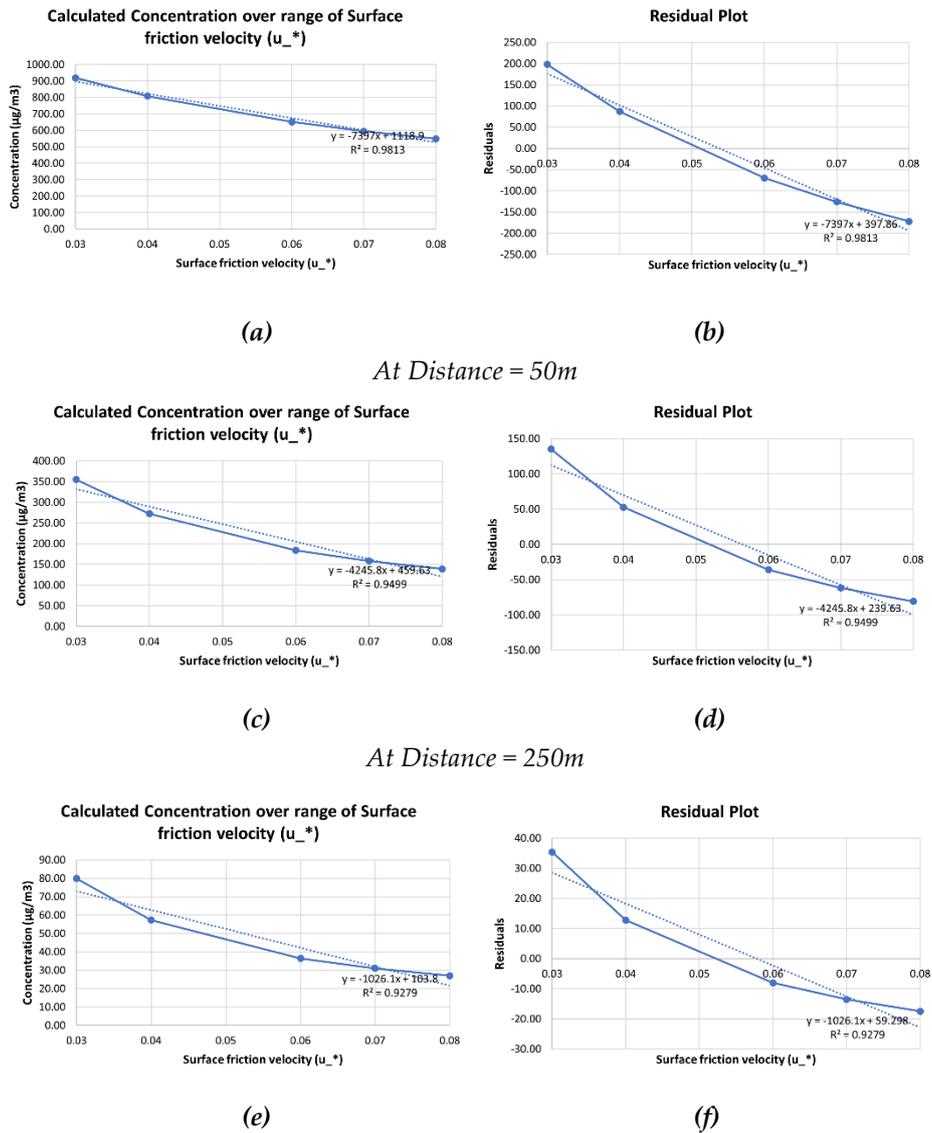


Figure 5. Variation of concentration with surface friction velocity (u_*)

The sensitivity of model output to coefficient a :

The graphs are plotted in Figure 6 for the computed concentrations and residuals for three downwind distances. The base case value for the coefficient a considered is 0.57. The plots 6a, 6c, and 6e represent the variation in concentrations, and plots 6b, 6d, and 6f represent residual plots. In the plots between the coefficient a and output concentrations with incremental distance, it was observed that the output concentrations decrease with an increase in coefficient a , as expected. The slope equations and the R^2 values for a linear fit are mentioned in plots in Figure 6. The calculated concentration and residuals varied significantly for 10m, 50m, and 250m. These characteristics show Type III sensitivity to the coefficient a at 10m, 50m, and 250m.

At Distance = 10m

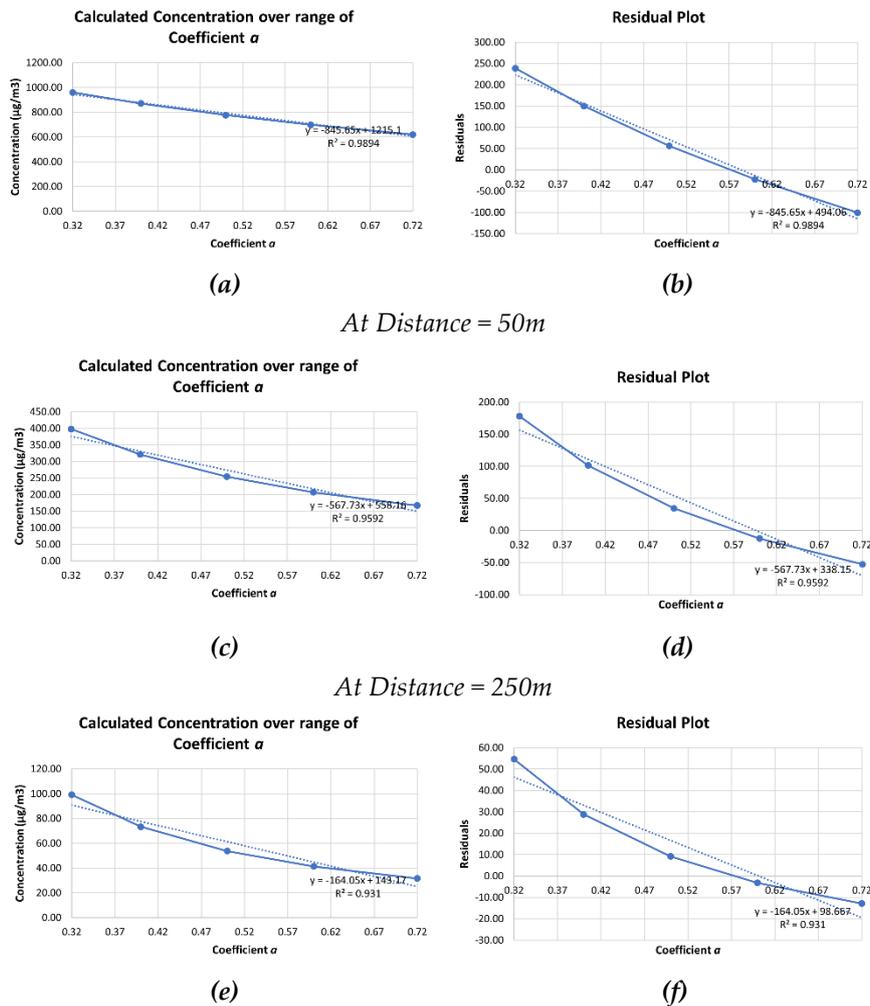
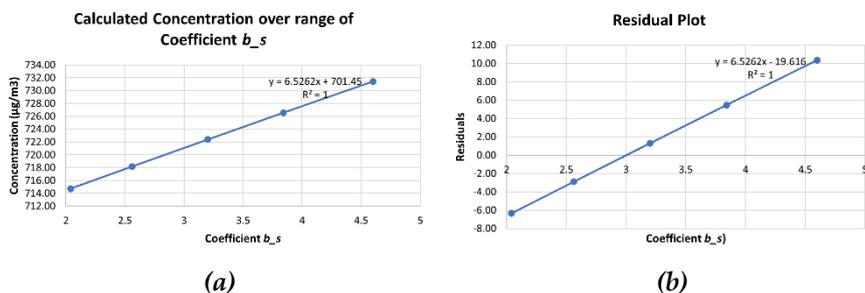


Figure. 6. Variation of concentration with coefficient a

The sensitivity of model output to coefficient b_s :

The graphs are plotted in Figure 7 for the computed concentrations and residuals for three downwind distances. The base case value for coefficient b_s considered is 3. The plots 7a, 7c, and 7e represent the variation in concentrations, and plots 7b, 7d, and 7f represent residual plots. In the plots between the Coefficient b_s and output concentrations with incremental distance, it was observed that the output concentrations decrease with an increase in the coefficient b_s . The slope equations and the R^2 values for a linear fit are mentioned in plots in Figure 7. The calculated residuals varied significantly with the changes in b_s . However, it can be observed that there is not much significant change observed in the model conclusions at 10m, 50m, and 250m (see plots 7a, 7c, and 7e) and the model shows Type II sensitivity at all downwind distances to the coefficient b_s .

At Distance = 10m



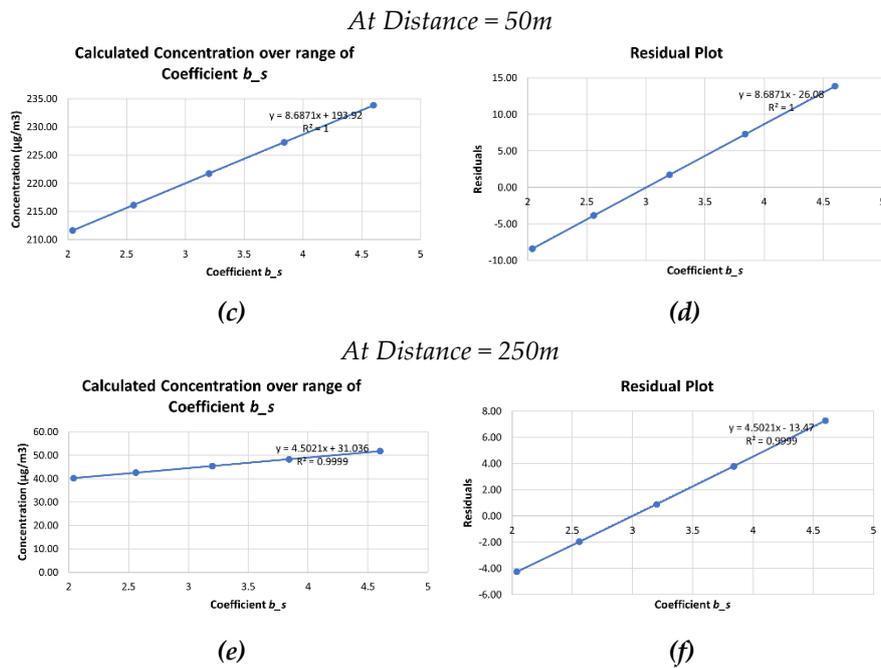
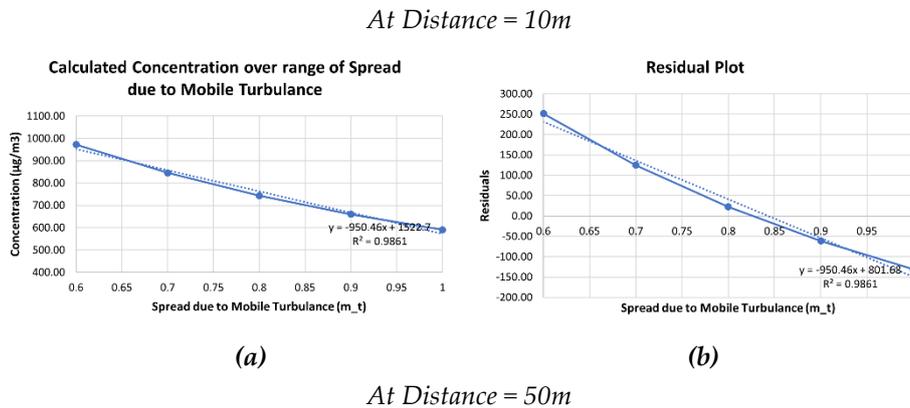


Figure. 7. Variation of concentration with the coefficient b_s

The sensitivity of model output to the additional spread due to the wake turbulence m_t :

The graphs are plotted in Figure 8 for the computed concentrations and residuals for three downwind distances. The base case value for m_t considered is 0.825. The plots 8a, 8c, and 8e represent the variation in concentrations, and plots 8b, 8d, and 8f represent residual plots. In the plots between m_t and output concentrations with incremental distance, it was observed that the output concentrations decrease with an increase in m_t . It is observed from the plots that there is a significant change in model conclusions and residuals at 10m and 50m downwind distances. The calibration residuals at 250m shows significant change. However, it can be observed that there is not much significant change observed in the model conclusions at 250m. These characteristics show Type III sensitivity at 10m and 50m. The model shows closer to Type II sensitivity at 250m.



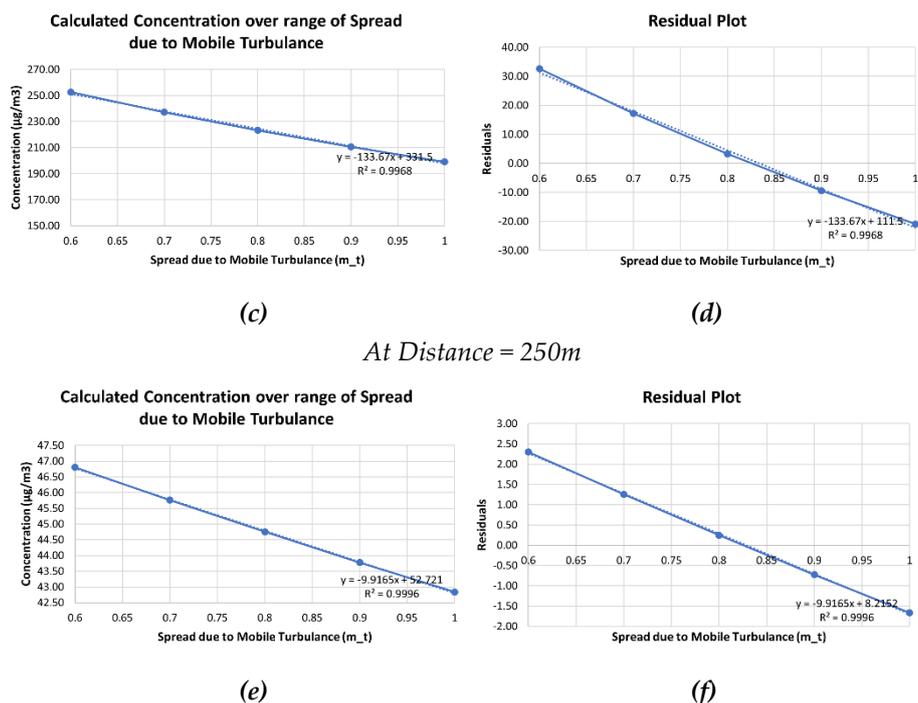


Figure. 8. Variation of concentration with spread due to mobile turbulence (m_t)

The above figures show that the model concentrations and residuals change significantly with the change in the value of the model in most of the cases. A summary of the type of sensitivity of the model is as follows:

- The model shows Type III sensitivity for the emission rate, meteorological variables m , and u_* and turbulent variables a , and m_t .
- The sensitivity of the model to the reference wind velocity is Type III, Type II and Type I depending on the downwind distance.
- The sensitivity of the model is Type II due to coefficient b_s .
- Overall, the model equations should be reexamined for u_1 , b_s , and m_t to make sure that that the model is valid for computing ground level concentrations.

6. Conclusions

A new model SLINE is presented to compute downwind concentrations from line sources on a highway. The sensitivity analysis shows that the model does not exhibit Type III sensitivity for all the input variables. However, the model show Type III sensitivity for the input parameters q , m , u_* , a and mt in computing concentration at all the downwind distance. One of the vertical spread variables b_s to compute the vertical spread of the plume shows Type II sensitivity. The type of model sensitivity for the reference wind velocity is mixed at different downwind distances. It is important to note that the model formulation should be reexamined for u_1 , b_s , and m_t so that the model is not invalidated as outlined in the ASTM Guide (1994). Further study should focus on evaluating the model against the observed data and to determine the sensitivity of the model using simultaneous changes in model inputs.

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