

7th International Electronic Conference on Sensors and Applications  
15-30 November 2020



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# A COMBINED MODEL-ORDER REDUCTION AND DEEP LEARNING APPROACH FOR STRUCTURAL HEALTH MONITORING UNDER VARYING OPERATIONAL AND ENVIRONMENTAL CONDITIONS

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# GENOA (ITALY) 14/08/18, PARTIAL COLLAPSE OF THE MORANDI BRIDGE – 43 PEOPLE KILLED



Marco Grasso, Matteo Indice. Via all'anticipo del maxi-processo sul crollo. *Il secolo XIX*, 22/09/18.

# MIAMI (FLORIDA, USA) 15/03/18, COLLAPSE OF A PEDESTRIAN FOOTBRIDGE - 6 PEOPLE KILLED



Pedro Portal. *Miami Herald*, 15/03/18.

## HEALTH MONITORING UNDER VARYING OPERATIONAL AND ENVIRONMENTAL CONDITIONS

Sensor system recordings

Structural Health Monitoring (SHM)

Damage detection, localization and quantification

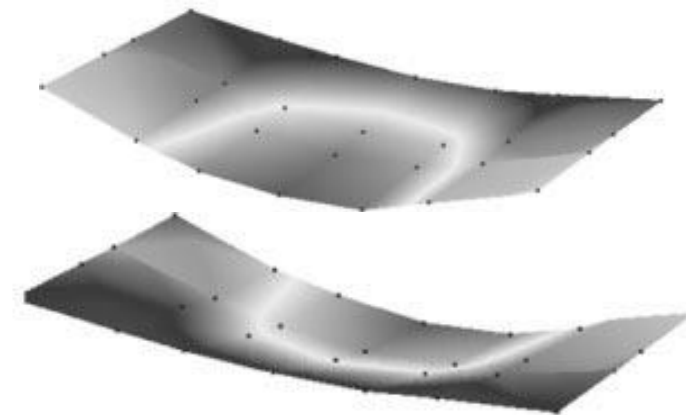
Sources of operational variability:

- load condition;
- load amplitude.

Sources of environmental variability:

- wind;
- humidity;
- **temperature**

expansion/contraction effect;  
softening/stiffening effect.



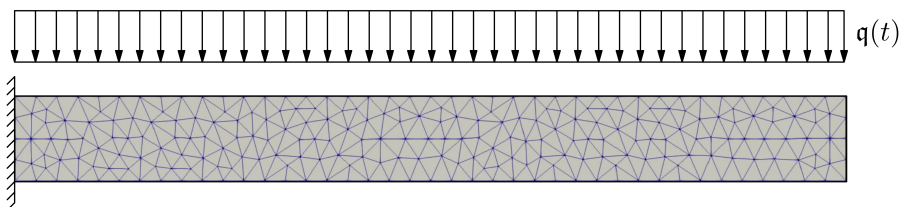
The Alamosa Canyon Bridge: 1<sup>st</sup> mode shape of one span of the Alamosa Canyon Bridge during two times of the day: morning (7.75 Hz); afternoon (7.42 Hz).

## OBJECTIVE: DAMAGE LOCALIZATION UNDER VARYING OPERATIONAL AND ENVIRONMENTAL CONDITIONS

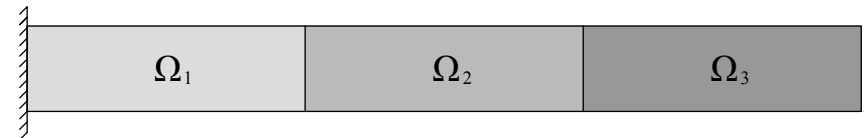
**1. Simulation Based Classification:** the problem is traced back to train a classifier on the basis of numerical data.



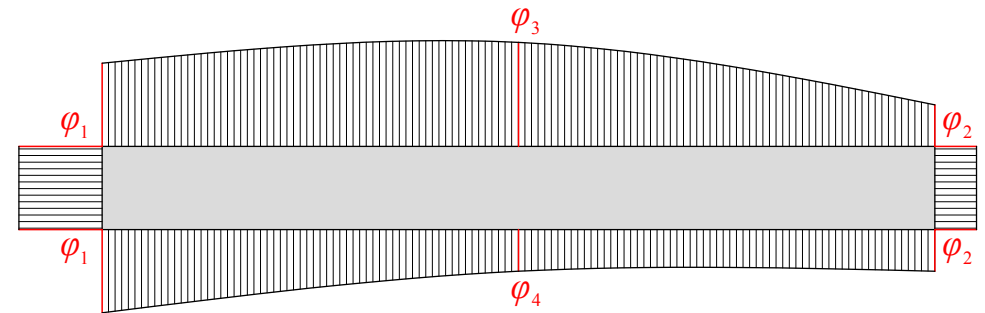
From reality to high fidelity FE modeling



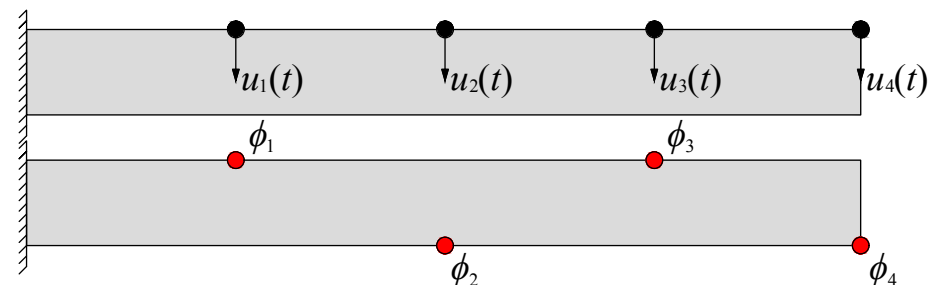
**2. Damage:** local stiffness reduction of predefined subdomains assumed fixed within the observation interval: **linear behavior**.



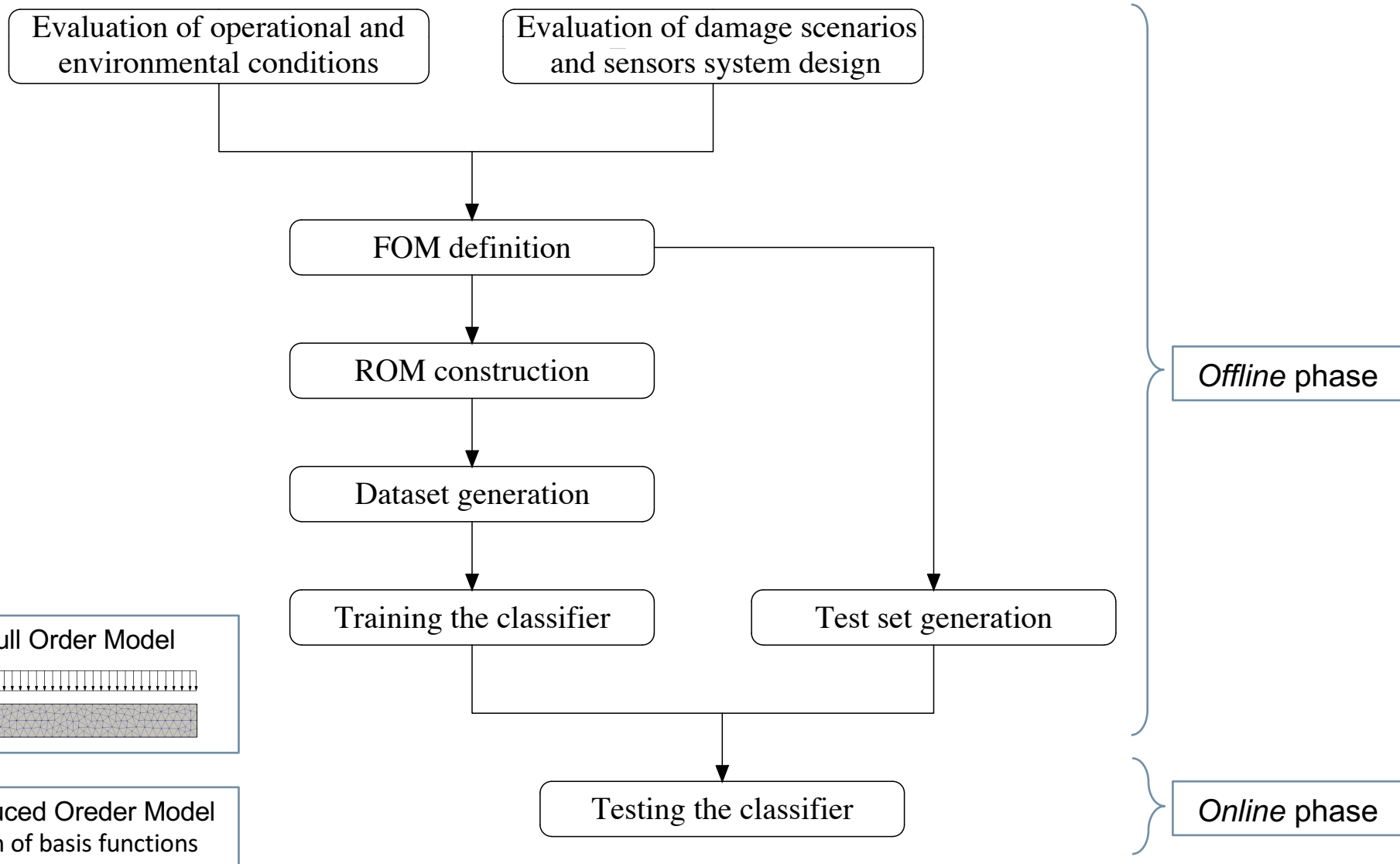
**3. Thermo-mechanical effects** are also simulated.



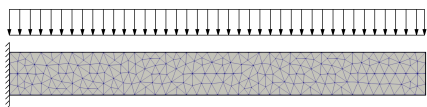
**4. Processed data:** vibrational signals shaped as multivariate time series and temperature measurements, both mimicking the recordings of a **pervasive sensor system**.



## OFFLINE-ONLINE DECOMPOSITION



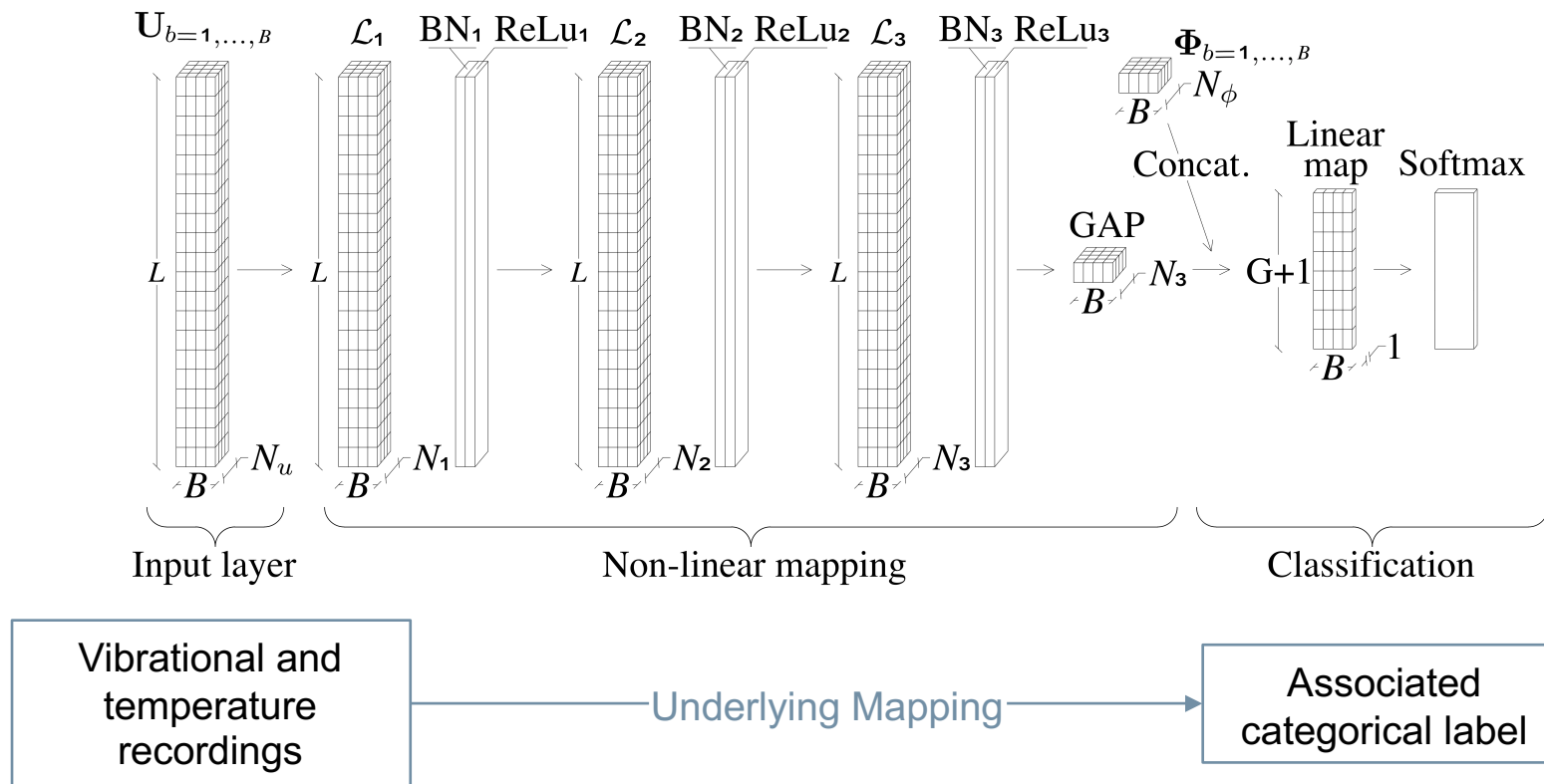
FOM = Full Order Model



ROM = Reduced Order Model  
Combination of basis functions

## FCN-BASED CLASSIFIER

- The **Dataset** includes instances of each considered damage state for several operational/thermal conditions.



- **Training phase:** the classifier *learns* the **mapping** {input instance}  $\Rightarrow$  {associated label (damage state)}.
- **Testing phase:** the classifier should map unseen instance into the current damage condition.

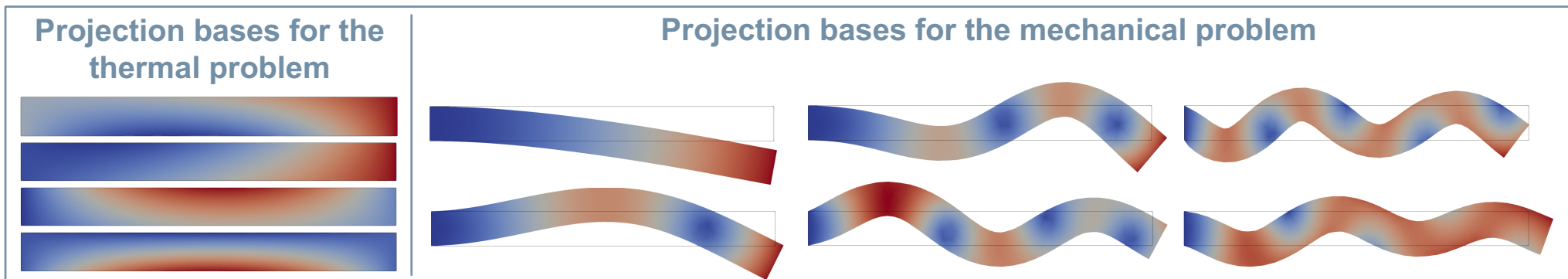
## FULL ORDER MODEL AND REDUCED ORDER MODEL

### ➤ Modeling hypotheses:

- ❖ thermo-elasticity linear theory with a one-way approach;
- ❖ temporal dependence of the thermal field is neglected;
- ❖ damping effects are disregarded;
- ❖ local dependency of the stiffness matrix on the material temperature;
- ❖ damage as a selective reduction (5% ÷ 25%) in stiffness, fixed in time.

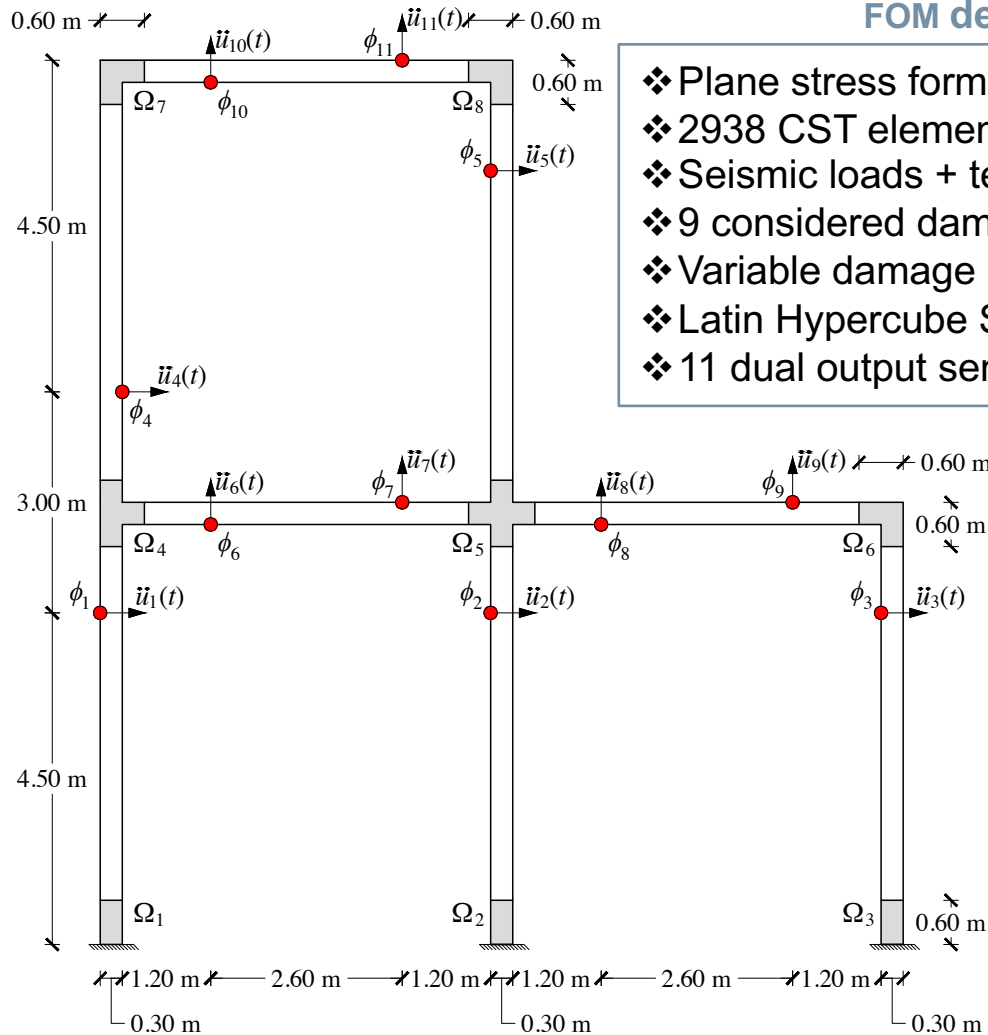
### ➤ The dataset construction is **accelerated exploiting the ROM**:

- ❖ **The ROM** relies on the **Reduced Basis method**;
- ❖ **The projection bases** are built via **Proper Orthogonal Decomposition**.





## NUMERICAL CASE STUDY

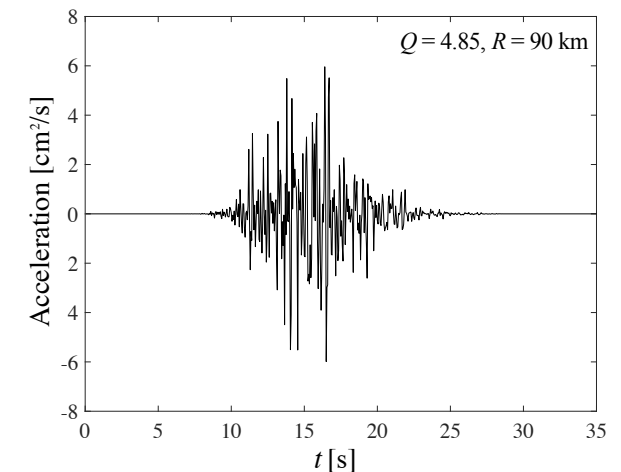


## FOM definition

- ❖ Plane stress formulation.
- ❖ 2938 CST elements - 1469 nodes.
- ❖ Seismic loads + temperature profiles.
- ❖ 9 considered damage conditions.
- ❖ Variable damage level (5% ÷ 25%).
- ❖ Latin Hypercube Sampling.
- ❖ 11 dual output sensors (20 Hz).

## Low intensity seismic loads

- ❖ Local magnitude (4.8 ÷ 5.3).
- ❖ Epicentral distance (80 ÷ 100)km.
- ❖ Rocky conditions.



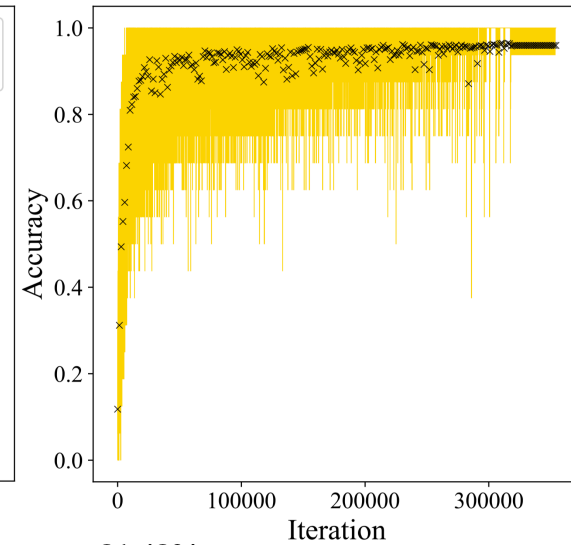
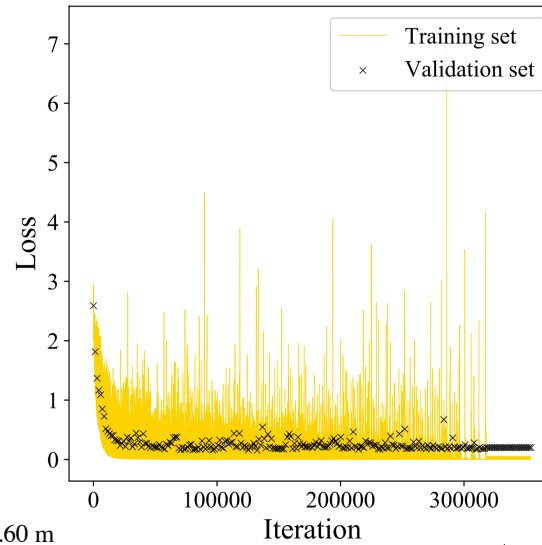
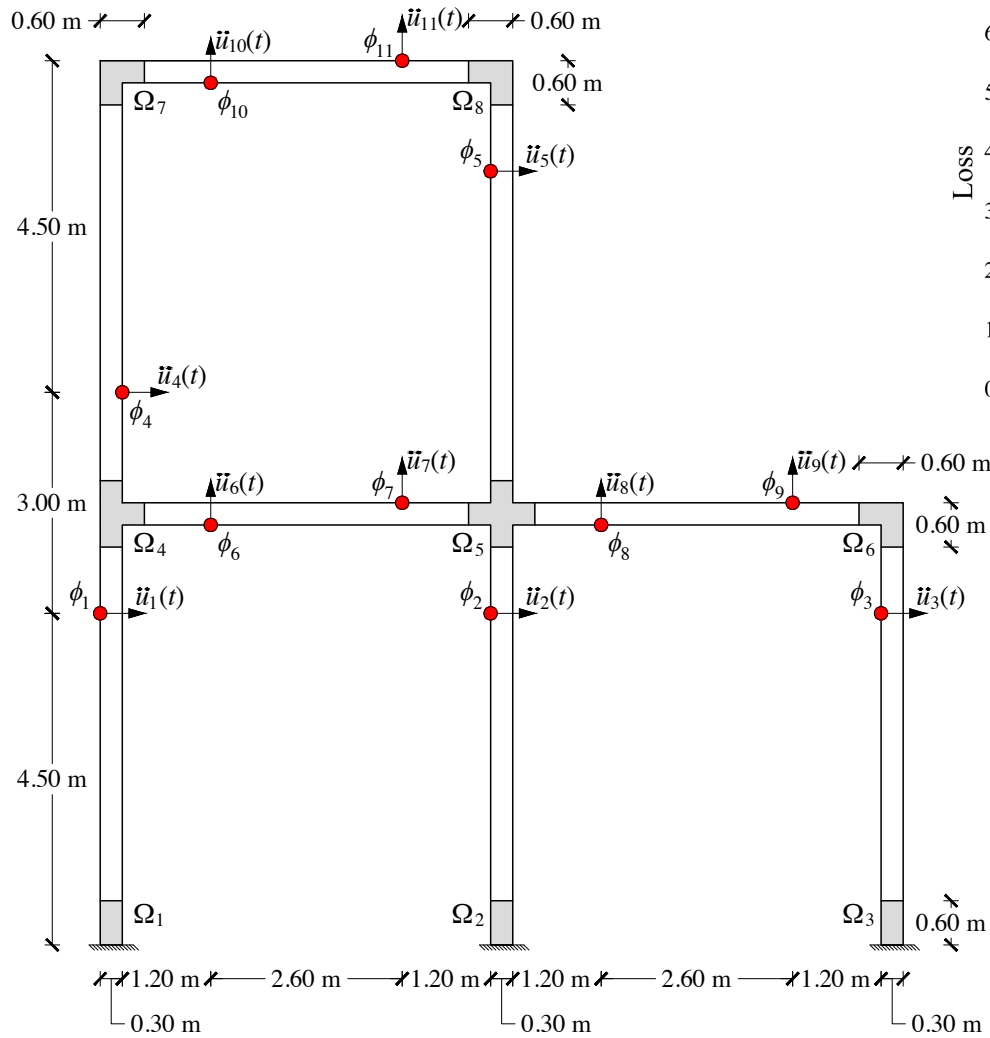
## Model Order Reduction

- ❖ Simulations duration = 35 s – (FOM solutions = 380).
- ❖ FOM CPU time = 421 s – ROM CPU time = 4.9 s.
- ❖ Speed-up = 86.
- ❖ ROM dofs = 63 (mechanical) and 28 (thermal).

R. Paolucci et al. *Broadband ground motions from 3D physics-based numerical simulations using artificial neural networks*. Bulletin of Seismological Society of America, 108, 2018.

F. Sabetta, A. Pugliese. *Estimation of response spectra and simulation of nonstationary earthquake ground motions*. Bulletin of the Seismological Society of America, 86, 1996.

# NUMERICAL CASE STUDY



**Accuracy: 81.48%**

Output Class	$\Omega_0$	$\Omega_1$	$\Omega_2$	$\Omega_3$	$\Omega_4$	$\Omega_5$	$\Omega_6$	$\Omega_7$	$\Omega_8$
$\Omega_0$	50.0%	0.0%	8.3%	8.3%	0.0%	0.0%	33.3%	0.0%	0.0%
$\Omega_1$	6	100.0%	0.0%	33.3%	0.0%	0.0%	0.0%	0.0%	8.3%
$\Omega_2$	1	12	91.7%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%
$\Omega_3$	4	0	11	58.3%	0.0%	0.0%	16.7%	0.0%	0.0%
$\Omega_4$	0	0	0	7	100.0%	0.0%	0.0%	0.0%	0.0%
$\Omega_5$	8.3%	0.0%	0.0%	0.0%	12	100.0%	0.0%	0.0%	8.3%
$\Omega_6$	1	0	0	0	0	12	50.0%	0.0%	0.0%
$\Omega_7$	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	0.0%	100.0%	0.0%
$\Omega_8$	0	0	0	0	0	0	0	12	83.3%
	0	0	0	0	0	0	0	0	10

## CONCLUSIONS

- We have proposed a **data-based strategy for SHM** under varying operational and environmental conditions, integrating **model-order reduction and deep learning**.
- The damage localization task has been performed by making use of **vibrational and temperature measurements**.
- A database of **synthetic recordings** has been built offline for a set of predefined damage conditions.
- A reduced order model has been exploited to **accelerate the dataset construction**.
- A DL-based classifier has been adopted to perform the **automatic features extraction** and to relate raw sensor measurements to structural health conditions.
- The classifier has achieved a **global accuracy of about 81.5%**, which is a very good result in the light of **the heterogeneity of the explored conditions** and of the **damage level variability**.

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**THANK YOU FOR YOUR ATTENTION!**

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# THERMO-ELASTIC PROBLEM - SIMPLIFYING HYPOTHESES

## Fully coupled problem

- Onset of a volumetric deformation for a temperature variation.
- Onset of internal heat for a variation of the volumetric deformation.

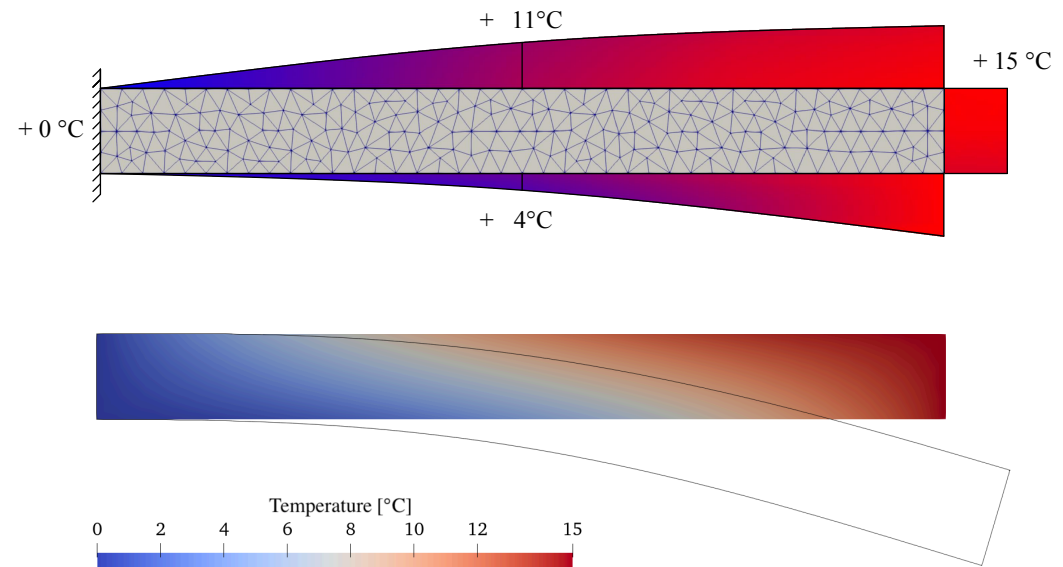
## Simplifying hypotheses

- Small strain rate: one-way coupling approach.
- Short monitoring windows: stationary thermal problem.

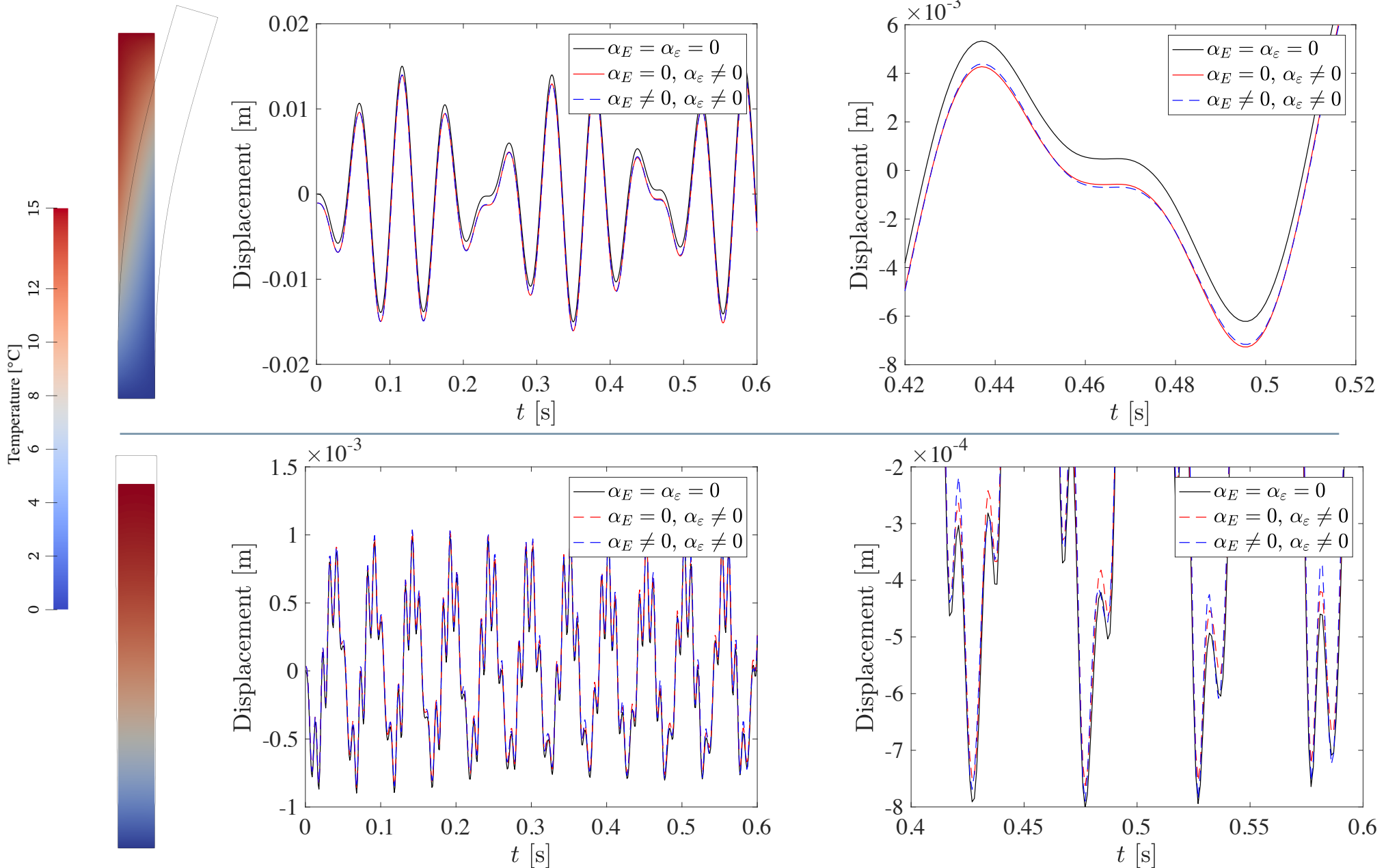
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### Algorithm 1 Thermo-Elastic Problem Solution (FOM).

- 1: Solve  $\mathbf{K}_\varphi \varphi = \mathbf{f}_\varphi \rightarrow \varphi$
  - 2: Solve  $\mathbf{K}_v(\varphi) \mathbf{v} = \mathbf{G}_v \varphi \rightarrow \mathbf{v}_\varphi$
  - 3:  $\mathbf{v}_\varphi$  assumed as initial condition:  $\mathbf{v}_0 = \mathbf{v}_\varphi$
  - 4: WHILE  $t_p < t_{L_S}$  DO
  - 5:     Solve  $\mathbf{M}_v \ddot{\mathbf{v}}(t_p) + \mathbf{K}_v(\varphi) \mathbf{v}(t_p) = \mathbf{G}_v \varphi + \mathbf{f}_v(t_p)$
  - 6: END WHILE
- 



# TEMPERATURE EFFECTS ON THE OBSERVED QUANTITIES: TOP-RIGHT TIP VERTICAL DISPLACEMENT



## POD BASES CONSTRUCTION ALGORITHM

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### Algorithm 2 POD bases construction

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1: *POD FOR THE COUPLED ELASTO-DYNAMIC PROBLEM*

2: FOR  $j = 1, \dots, \mathfrak{N}$  DO

3:     Sample  $\{\boldsymbol{\eta}_u, \boldsymbol{\eta}_\phi, g\}_j$  via LHS

4:     Solve  $\{\mathbf{K}_\varphi \boldsymbol{\varphi}(\boldsymbol{\eta}_\phi) = \mathbf{f}_\varphi(\boldsymbol{\eta}_\phi)\}_j \rightarrow \boldsymbol{\varphi}(\boldsymbol{\eta}_\phi^j)$

5:     Call {Algorithm 1} to Solve  $\{\mathbf{M}_v \ddot{\mathbf{v}}(t, \boldsymbol{\eta}_u, \boldsymbol{\eta}_\phi, g) + \mathbf{K}_v(\boldsymbol{\eta}_u, \boldsymbol{\varphi}, g) \mathbf{v}(t, \boldsymbol{\eta}_u, \boldsymbol{\eta}_\phi, g) = \dots$

6:              $\mathbf{G}_v \boldsymbol{\varphi}(\boldsymbol{\eta}_\phi) + \mathbf{f}_v(t, \boldsymbol{\eta}_u)\}_j \rightarrow \mathbf{v}_j(t_p), \quad p = 1, \dots, L_S^R$

7:     Collect  $\mathbf{S}_v^j = [\mathbf{v}(t_1, \{\boldsymbol{\eta}_u, \boldsymbol{\eta}_\phi, g\}) | \dots | \mathbf{v}(t_{L_S^R}, \{\boldsymbol{\eta}_u, \boldsymbol{\eta}_\phi, g\})]_j$

8:      $\mathbf{W}_v^j = \text{POD}_{time}(\mathbf{S}_v^j)$

9:     IF  $j == 1$  THEN

10:          $\mathbf{W}_v = \mathbf{W}_v^1$

11:     ELSE

12:          $\mathbf{S}_p = [\mathbf{W}_v | \mathbf{W}_v^j]$

13:          $\mathbf{W}_v = \text{POD}_{parameters}(\mathbf{S}_p)$

14:     END IF

15: END FOR

16: *POD FOR THE DIFFUSION PROBLEM*

17: Collect  $\mathbf{S}_\varphi = [\boldsymbol{\varphi}(\boldsymbol{\eta}_\phi^1) | \dots | \boldsymbol{\varphi}(\boldsymbol{\eta}_\phi^{\mathfrak{N}})]$

18:  $\mathbf{W}_\varphi = \text{POD}(\mathbf{S}_\varphi)$

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## REDUCED SOLUTION ALGORITHM

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**Algorithm 3** Thermo-Elastic Problem Solution (ROM).

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- 1: Compute  $\mathbf{K}_\varphi^R = \mathbf{W}_\varphi^\top \mathbf{K}_\varphi \mathbf{W}_\varphi$ ,  $\mathbf{f}_\varphi^R = \mathbf{W}_\varphi^\top \mathbf{f}_\varphi$
  - 2: Solve  $\mathbf{K}_\varphi^R \boldsymbol{\varphi}^R = \mathbf{f}_\varphi^R \rightarrow \boldsymbol{\varphi}^R$
  - 3: Compute  $\boldsymbol{\varphi} = \mathbf{W}_\varphi \boldsymbol{\varphi}^R$
  - 4: Compute  $\mathbf{M}_v^R = \mathbf{W}_\varphi^\top \mathbf{M}_v \mathbf{W}_\varphi$ ,  $\mathbf{G}_v^R = \mathbf{W}_\varphi^\top \mathbf{G}_v$ ,  $\mathbf{K}_v^R = \mathbf{W}_\varphi^\top \mathbf{K}_v(\boldsymbol{\varphi}) \mathbf{W}_\varphi$ ,  $\mathbf{f}_v^R = \mathbf{W}_\varphi^\top \mathbf{f}_v$
  - 5: Solve  $\mathbf{K}_v^R(\boldsymbol{\varphi}) \mathbf{v}^R = \mathbf{G}_v^R \boldsymbol{\varphi} \rightarrow \mathbf{v}_\varphi^R$
  - 6:  $\mathbf{v}_0^R = \mathbf{v}_\varphi^R$
  - 7: WHILE  $t_p < t_{L_S}$  DO
  - 8:     Solve  $\mathbf{M}_v^R \ddot{\mathbf{v}}^R(t_p) + \mathbf{K}_v^R(\boldsymbol{\varphi}) \mathbf{v}^R(t_p) = \mathbf{G}_v^R \boldsymbol{\varphi} + \mathbf{f}_v^R(t_p)$
  - 9:     Compute  $\mathbf{v}(t_p) = \mathbf{W}_\varphi \mathbf{v}^R(t_p)$
  - 10: END WHILE
-



# CONVOLUTIONAL NEURAL NETWORK (CNN)

Inspired by the visual cortex and typically used in computer vision.

