



Biomimetic Design of a Planar Torsional Spring to an Active Knee Prosthesis Actuator using FEM Analysis

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Summary



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Introduction



- Motivation

- Increasing number of hospitalizations due to transfemoral amputations [1]

- Transfemoral amputees' locomotion [2,3]

- Expends more metabolic energy
 - Overcompensates the movement with the intact member
- } Long term damages

- The need to develop better active lower-limb prostheses [3-7]

- Recover the leg movements introducing positive power
- Series Elastic Actuators: greater environment-actuator interaction



Introduction



- Series Elastic Actuators (SEA) [3,5-7]
 - Develop Compliant elements to tolerate impacts
 - Linear springs, torsion springs, etc
- Spring for a knee prostheses [8]
 - Passive store mechanical energy
 - Daily activities have a lot of dissipative phases
 - Match the Knee quasi-stiffness of flexion and extension stages of the stance phase
 - The moment-angle relationship is approximately linear
 - Characteristics
 - Lightweight
 - Compact: Planar torsional springs



Introduction



- SEAs: Planar Torsional Springs

- Flexible component or linear springs tangentially arranged

- Dos Santos et al., 2015 [9]- Flexible component

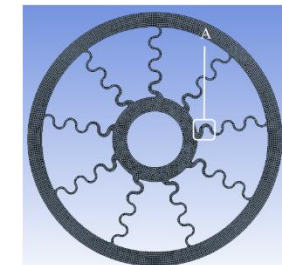
- $\tau_{max} = 15 Nm$
- $S_C = 200 Nm/rad$
- AISI 6150 Steel

- Wang et al., 2017 [10] - Flexible component

- $\tau_{max} = 30 Nm$
- $S_C = 288.5 Nm/rad$
- Maraging Steel 300

- Tsagarakis et al., 2009 [6] - linear springs

- $\tau_{max} = 40 Nm$
- $S_C = 150 Nm/rad$

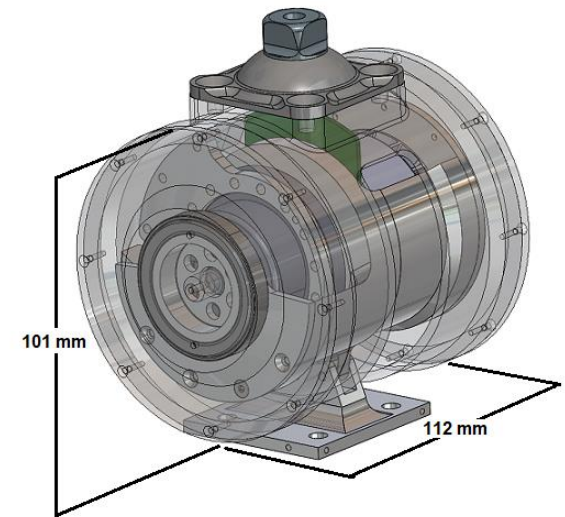


Mechanical Design



- The Knee Prosthesis

- Assist a person with 1.71m and 71.6kg [11]
- Actuator components
 - EC60 Flat 200W – Maxon Motor, Switzerland
 - CSG 17-50-2A-R – Harmonic Drive SE, Germany
- Characteristics*
 - Nominal torque: 27 Nm at 64 rpm
 - Positive peak torque: 80 Nm
 - Resistive peak torque: 90 Nm
 - 1.53 kg



*Without the efficiency factors.

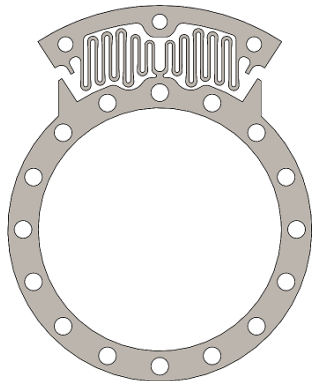
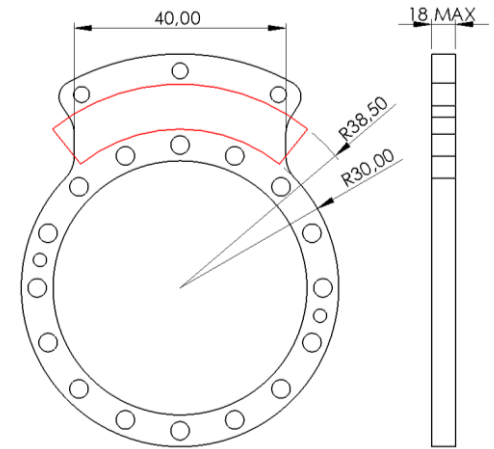


Mechanical Design

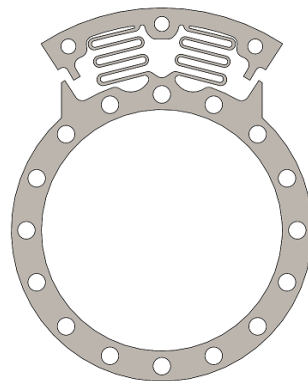


- Torsional Spring Design

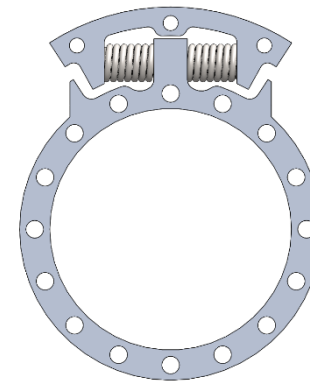
- Shamaei et al, 2013 [8] - Stiffness Target
 - 246 Nm/rad
- Limitations
 - 0.200 kg
 - Width ≤ 18 mm
 - Limited available space (highlighted region)
- Three proposed geometries



First Design



Second Design



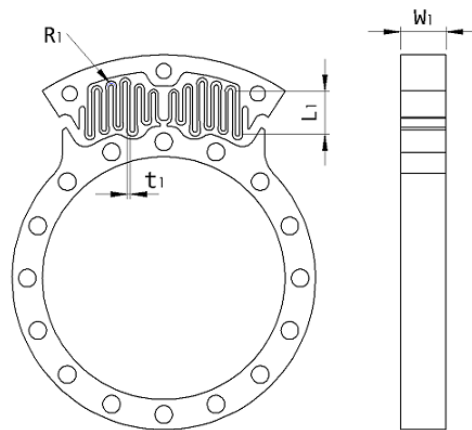
Third Design



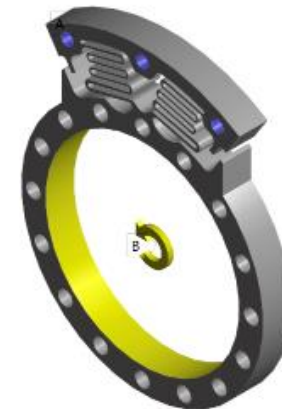
Mechanical Design



- Torsional Spring Analysis – First and Second Design
 - Parameters
 - R_1, t_1, L_1, W_1
 - Boundary conditions in the FEM Analysis
 - Spring Analysis – Maximum Stress and Stiffness = Moment reaction/Angular displacement
 - Mechanical end stop Analysis – Stress when the Moment reaction reaches 90 Nm



A Fixed Support
B Remote Displacement



Mechanical Design



- Torsional Spring Analysis – First and Second Design

- Material Selection

- Alloys [12,13]

- AISI 4340 Steel
- AISI 6150 Steel

- FEM Analysis

- Stiffness
- Safety Factor = 1.8

- Heat Treatment [12]

- Austempering: Greater fatigue life than Q&T for stresses higher than the fatigue limit
- Quenching & Tempering

Table 1. Mechanical properties of the two alloy steels.

Alloy Steel	Elasticity Modulus	Poisson's Ratio	Tensile Yield Strength	Tensile Ultimate Strength
AISI 4340 ^{1,2}	212 GPa	0.30	1475 MPa	1595 MPa
AISI 6150 ¹	205 GPa	0.29	1225 MPa	1240 MPa

¹ Reference [12] ² Reference [13]



Mechanical Design



- Torsional Spring Analysis – Third Design

- Tsagarakis et al., 2009 [6] - Linear Springs Stiffness Target

- $k_s = 2k_a \cdot \left(R^2 + \frac{r_s^2}{3} \right) \cdot (2\cos^2\theta_s - 1)$

- k_s : Torsional spring stiffness
 - k_a : Linear spring stiffness
 - R: Radius where the spring is fixed
 - r_s : External radius of the spring
 - θ_s : Angular displacement

- Manufacturers' catalogs
 - Search springs that fit the space limitations
 - Recalculate the Torsional spring stiffness



Results



- Material Selection – First Design

- The spring parameters are fixed
- Calculus of the stiffness
- Maximum allowable rotation based on the safety factor
- Heat Treatment
 - Austempering: Greater fatigue life than Q&T for stresses higher than the fatigue limit

✓ Austempered AISI 4340 Steel

Table 2. Results of the material selection analysis.

Alloy	Maximum rotation	Spring Stiffness
AISI 4340	2.5 °	74 Nm/rad
AISI 6150	2.2 °	72 Nm/rad



Results



• Spring Analysis – First Design

• R_1 Variation

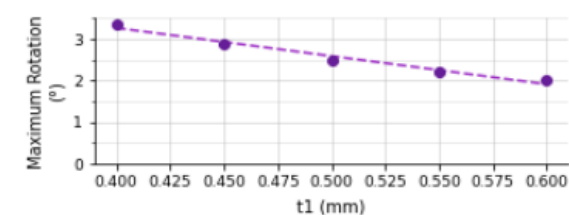
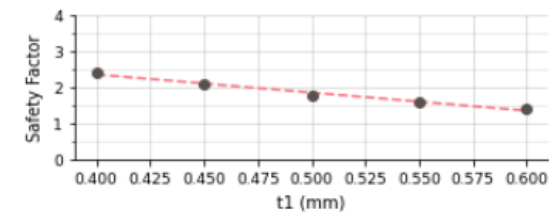
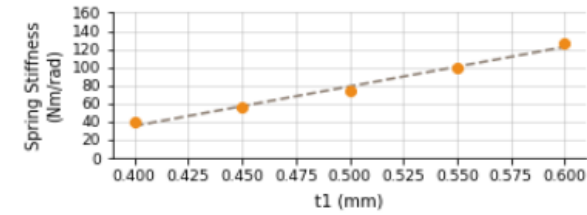
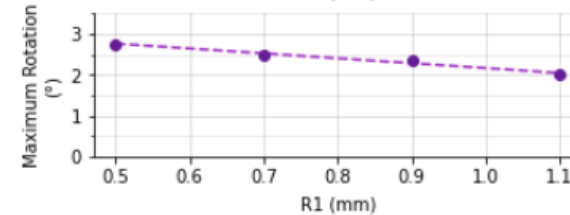
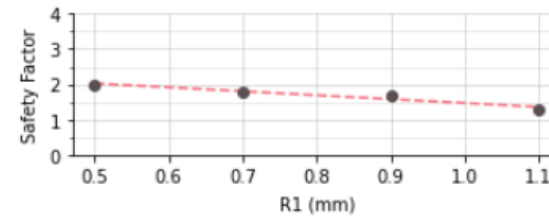
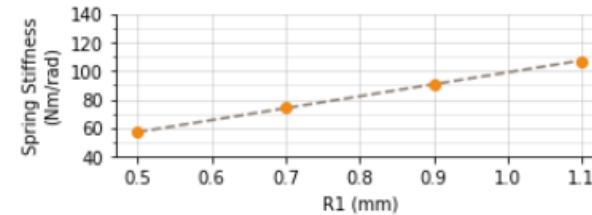
- $W_1 = 10$ mm; $t_1 = 0.5$ mm
- L_1 : varies in function of R_1 and the available space
- ✓ $R_1 = 0.7$ mm

↑ R_1 ↑ Stiffness ↓ Safety fator & Max. Rotation

• t_1 Variation

- $W_1 = 10$ mm; $R_1 = 0.7$ mm; L_1 : fixed
- ✓ $t_1 = 0.5$ mm

↑ t_1 ↑ Stiffness ↓ Safety fator & Max. Rotation



$$k_s = 74 \text{ Nm/rad}; \text{ Rotation up to } 2.50^\circ$$



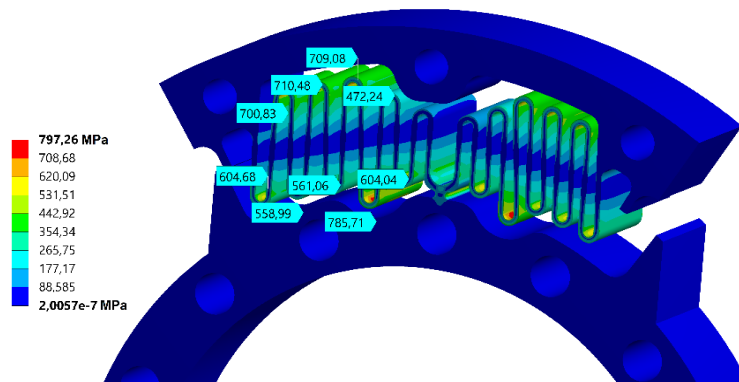
Results



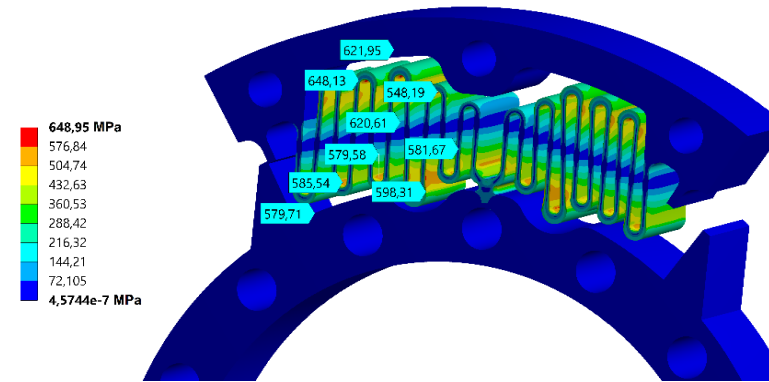
- Spring Analysis – First Design

- Manual enhancements - Probes
 - Augment in Stiffness and Safety Factor
 - Possibility to increase the maximum rotation to 3.20 °
 - Spring mass/width : 0.00927 kg/mm

Before the enhancement



After the enhancement



Stress for a 2.5 ° rotation.

$$k_s = 106 \text{ Nm/rad}; \text{ Rotation up to } 3.20^\circ$$



Results



• Spring Analysis – Second Design

• R_1 Variation

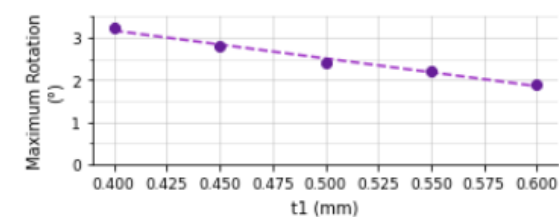
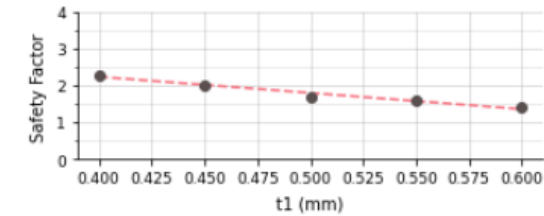
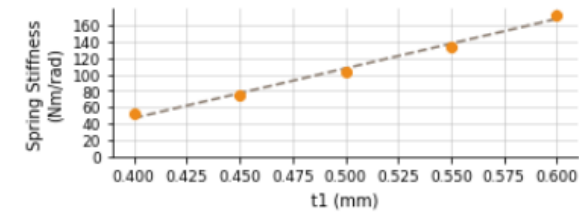
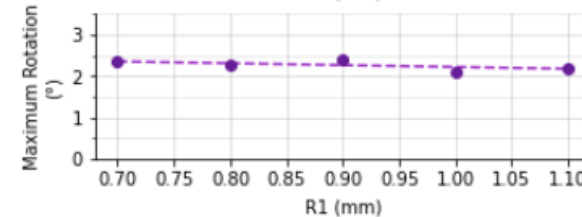
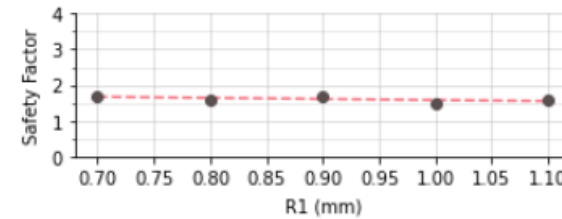
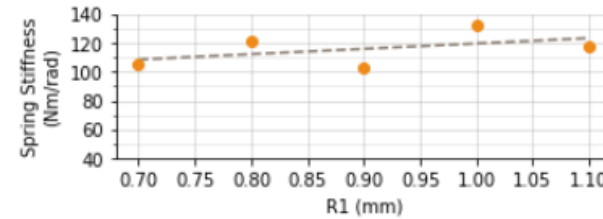
- $W_1 = 10$ mm; $t_1 = 0.5$ mm ; $L_1 = 8.5$ mm
- ✓ $R_1 = 0.9$ mm

↑ R_1 ↑ Stiffness ↓ Safety fator & Max. Rotation

• t_1 Variation

- $W_1 = 10$ mm; $R_1 = 0.9$ mm; $L_1 = 8.5$ mm
- ✓ $t_1 = 0.5$ mm

↑ t_1 ↑ Stiffness ↓ Safety fator & Max. Rotation



$$k_s = 103 \text{ Nm/rad}; \text{ Rotation up to } 2.40^\circ$$

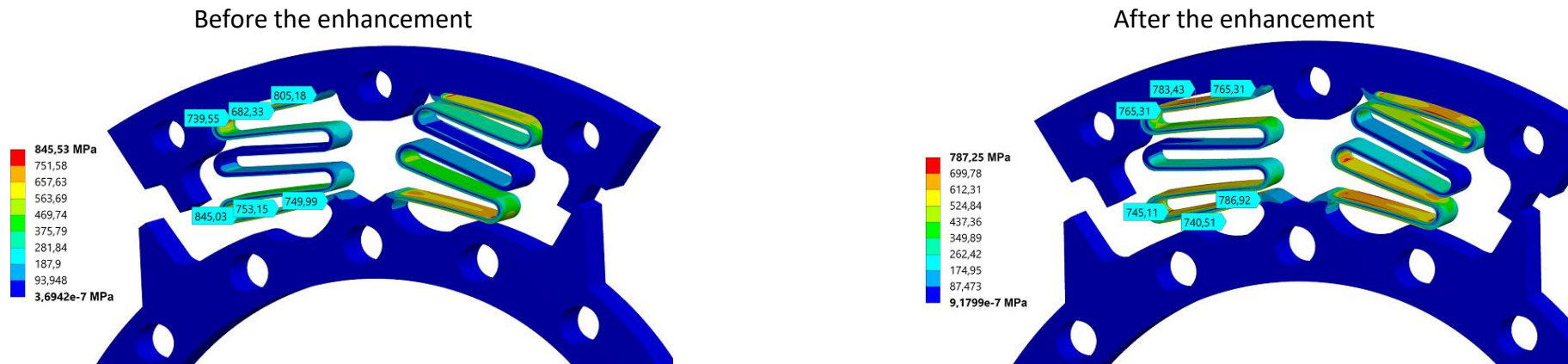


Results



- Spring Analysis – Second Design

- Manual enhancements - Probes
 - Augment in Stiffness and Safety Factor
 - Possibility to increase the maximum rotation to 2.50 °
 - Spring mass/width : 0.00898 kg/mm



$$k_s = 149 \text{ Nm/rad}; \text{ Rotation up to } 2.50^\circ$$



Results



• Spring Analysis – Third Design

- k_a Overvaluation
 - $R = 34 \text{ mm}$; $r_s = 0 \text{ mm}$; $\theta_s = 10^\circ$; $k_s = 246 \text{ Nm/rad}$
 - ✓ $k_a = 113 \text{ N/mm}$

• Catalogs' springs

Table 3. Linear compression springs characteristics.

	External diameter	Undelected Length	Maximum deflection	Stiffness (k_a)
Spring 1	8.1 mm	17.5 mm	7.3 mm	16.81 N/mm
Spring 2	8.1 mm	12.2 mm	4.7 mm	26.43 N/mm

- $k_{s1} = 38.15 \text{ Nm/rad}$
- $k_{s2} = 60.80 \text{ Nm/rad}$

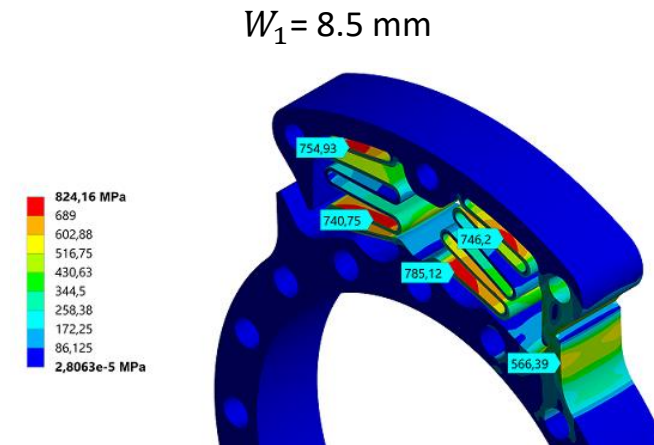
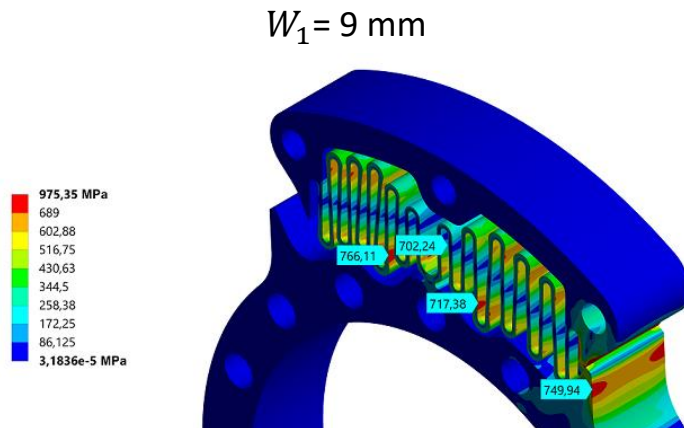
$$k_s = 60.8 \text{ Nm/rad}; \text{ Rotation up to } 3.96^\circ$$



Results



- Mechanical end Stop Analysis – First and Second Design
 - Inner Ring rotates until the moment reaction reaches 90 Nm
 - Only one spring
 - Evaluate the maximum stress



Discussion and Conclusions



- The Springs Stiffnesses are lower than the Knee quasi-stiffness
 - Parallel association of at least two springs – limited by the maximum width (18 mm)
 - Lower stiffness means that the user will feel like falling in heel strike
- The second design
 - ✓ The intermediate mass and width
 - ✓ The torsional spring constant matches the knee quasi-stiffness
 - ✓ Lower stresses with greater torque entries - more fatigue life

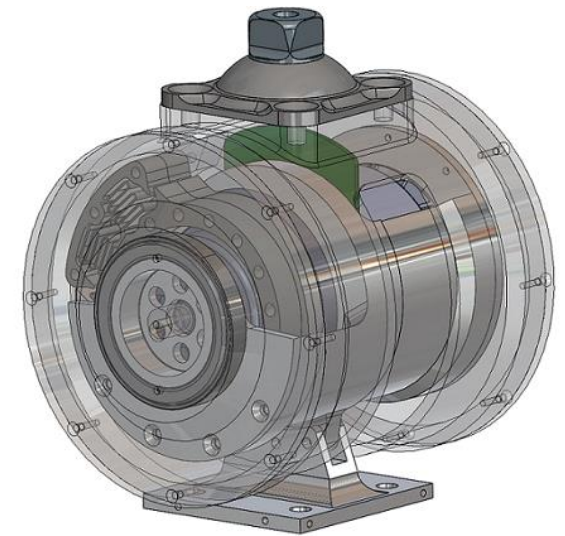
Parameters	First Design	Second Design	Third Design
W_1	9 mm	8.5 mm	8.1 mm
Number of springs	2	2	2
Maximum Rotation	3.20 °	2.50 °	3.96 °
Total Spring Mass	0.167 kg	0.153 kg	0.066 kg
Total Spring Stiffness	191 Nm/rad	250 Nm/rad	122 Nm/rad



Discussion and Conclusions



- The SEA Knee Prosthesis
 - Two parallel springs of the Second Design
 - The mass is up to 1.660 kg
- Future work
 - Manufacture and test the real torsional spring
 - Check the stiffness
 - Discover the fatigue life
 - Compare the performance of the rigid actuator and the SEA



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